

Transverse structure of the nucleon

Part 4: Advanced topics

The gauge link

Need of a gauge link

$$\Phi_{ij}(p, P, S) = \frac{1}{(2\pi)^4} \int d^4\xi e^{ip \cdot \xi} \langle P, S | \bar{\psi}_j(0) \psi_i(\xi) | P, S \rangle$$

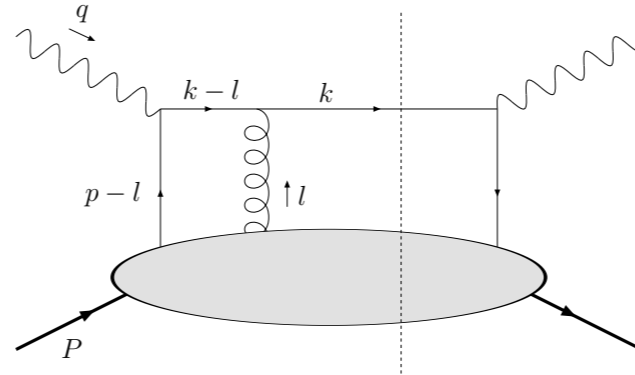
$$\psi(\xi) \rightarrow e^{i\alpha(\xi)} \psi(\xi)$$

$$\Phi_{ij}(p, P, S) = \frac{1}{(2\pi)^4} \int d^4\xi e^{ip \cdot \xi} \langle P, S | \bar{\psi}_j(0) U_{[0,\xi]} \psi_i(\xi) | P, S \rangle$$

$$U(\xi_1, \xi_2) \rightarrow e^{i\alpha(\xi_1)} U(\xi_1, \xi_2) e^{-i\alpha(\xi_2)}.$$

$$U_{[a,b]} = \mathcal{P} \exp \left[-ig \int_a^b d\eta^\mu A_\mu(\eta) \right]$$

Birth of the gauge link



(a)

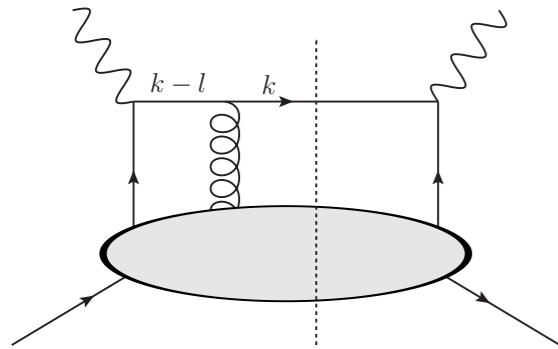
$$2MW_{\mu\nu}^{(a)} \sim \langle P, S | \bar{\psi}(0) \gamma_\mu \gamma^+ \gamma_\alpha \frac{\not{k} - \not{l} + m}{(k-l)^2 - m^2 + i\epsilon} \gamma_\nu g A^\alpha(\eta) \psi(\xi) | P, S \rangle \Big|_{\eta^+ = 0}$$

$$i \frac{\not{k} - \not{l} + m}{(k-l)^2 - m^2 + i\epsilon} \approx i \frac{k^- \gamma^+}{-2l^+ k^- + i\epsilon} \approx \frac{i}{2} \frac{\gamma^+}{-l^+ + i\epsilon}$$

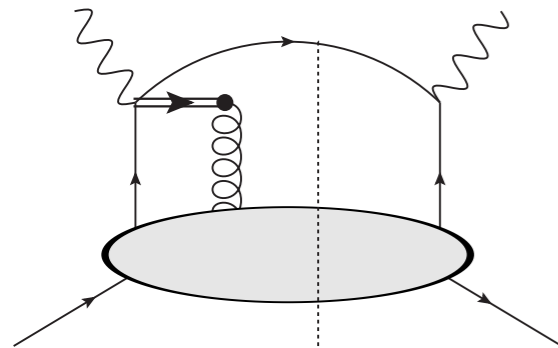
$$2MW_{\mu\nu}^{(a)} \sim \langle P, S | \bar{\psi}(0) \gamma_\mu \gamma^+ \frac{\gamma^- \gamma^+}{2} \gamma_\nu (ig) \frac{A^+(\eta)}{-l^+ + i\epsilon} \psi(\xi) | P, S \rangle \Big|_{\eta^+ = 0}$$

$$2MW_{\mu\nu}^{(a)} \sim \langle P, S | \bar{\psi}(0) \gamma_\mu \gamma^+ \gamma_\nu (-ig) \int_{\infty^-}^{\xi^-} d\eta^- A^+(\eta) \psi(\xi) | P, S \rangle \Big|_{\eta^+ = 0; \boldsymbol{\eta}_T = \boldsymbol{\xi}_T}$$

Birth of the gauge link

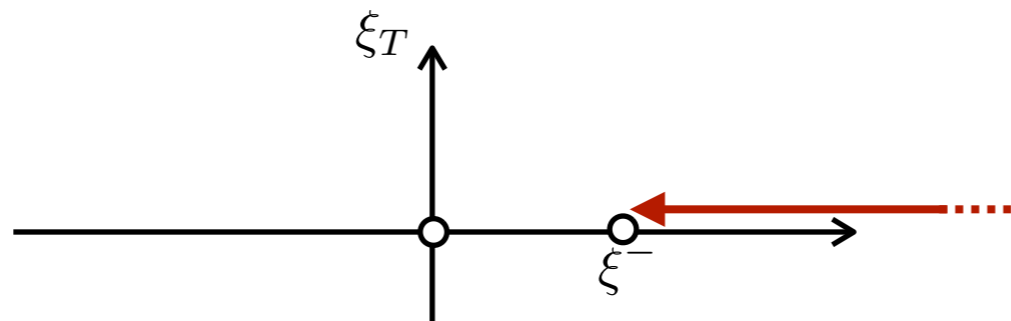


$$2MW_{\mu\nu}^{(a)} \sim \langle P, S | \bar{\psi}(0) \gamma_\mu \gamma^+ \gamma_\nu (-ig) \int_{\infty^-}^{\xi^-} d\eta^- A^+(\eta) \psi(\xi) | P, S \rangle \Big|_{\eta^+=0; \eta_T=\xi_T}$$



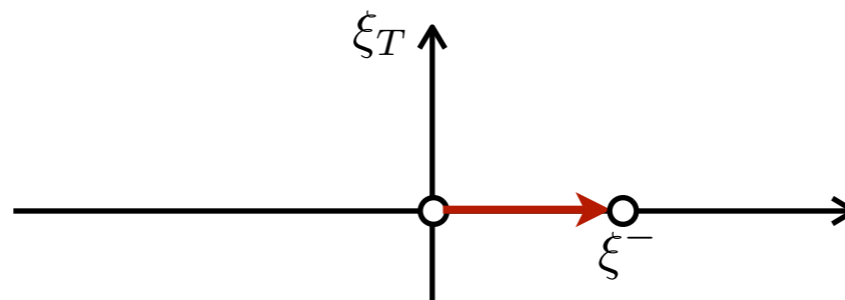
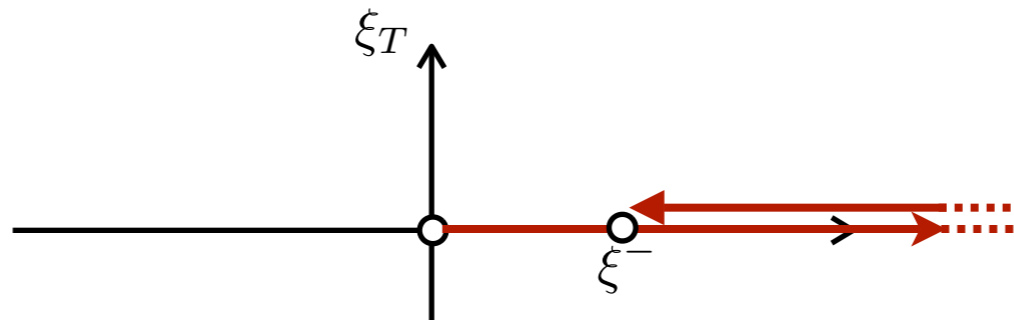
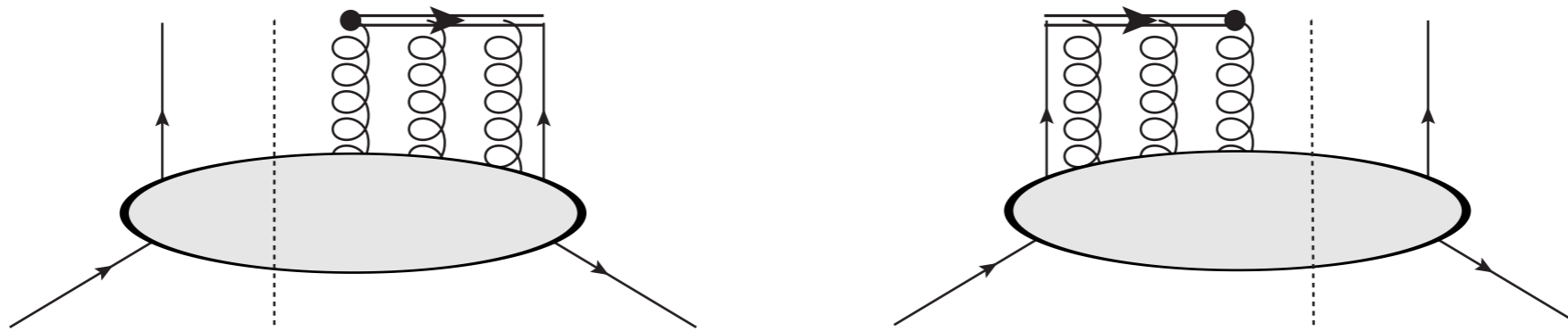
$$2MW^{\mu\nu}(q, P, S) \approx \sum_q e_q^2 \frac{1}{2} \text{Tr} [\Phi(x_B, S) \gamma^\mu \gamma^+ \gamma^\nu].$$

$$\Phi^{(a)}(x, S) \sim \langle P, S | \bar{\psi}(0) (-ig) \int_{\infty^-}^{\xi^-} d\eta^- A^+(\eta) \psi(\xi) | P, S \rangle$$

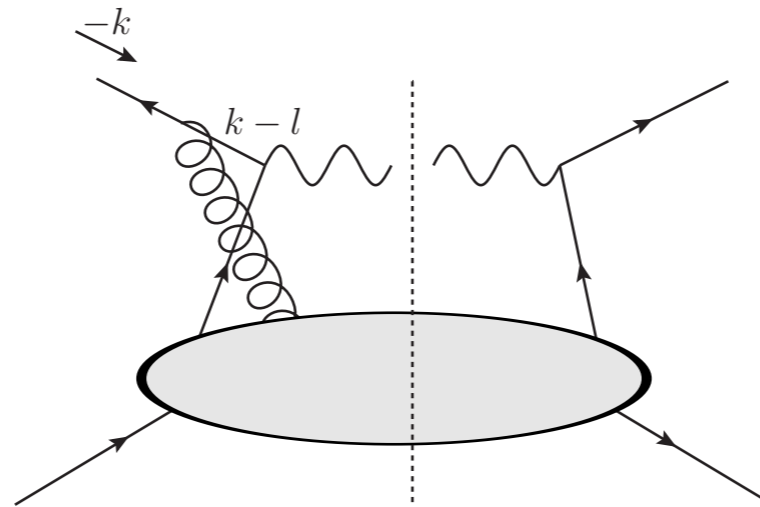


Shape of the gauge link

$$\Phi(x, S) \sim \langle P, S | \bar{\psi}(0) U_{[0, \infty^-]} U_{[\infty^-, \xi^-]} \psi(\xi) | P, S \rangle$$



Gauge link in Drell-Yan



$$2MW_{\mu\nu}^{(a)} \sim \langle P, S | \bar{\psi}(0) \gamma_\mu \gamma^+ \gamma_\alpha \frac{\not{k} - \not{l} + m}{(k-l)^2 - m^2 + i\epsilon} \gamma_\nu g A^\alpha(\eta) \psi(\xi) | P, S \rangle \Big|_{\eta^+=0}$$

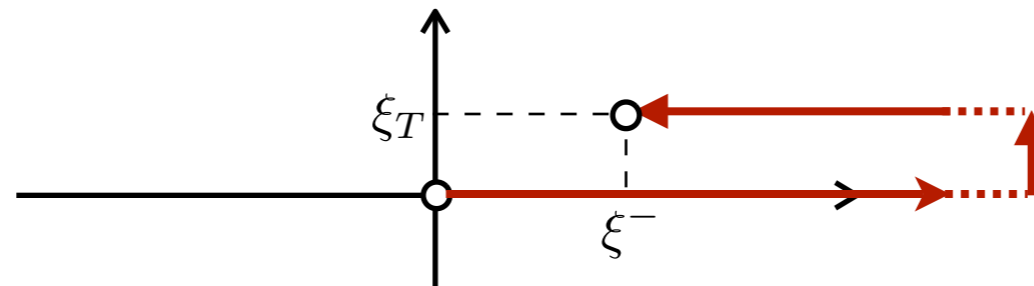
$$i \frac{\not{k} - \not{l} + m}{(k-l)^2 - m^2 + i\epsilon} \approx i \frac{-(-k)^- \gamma^+}{2l^+ (-k)^- + i\epsilon} \approx \frac{i}{2} \frac{\gamma^+}{-l^+ - i\epsilon}$$

$$2MW_{\mu\nu}^{(a)} \sim \langle P, S | \bar{\psi}(0) \gamma_\mu \gamma^+ \gamma_\nu (-ig) \int_{-\infty^-}^{\xi^-} d\eta^- A^+(\eta) \psi(\xi) | P, S \rangle \Big|_{\eta^+=0; \boldsymbol{\eta}_T = \boldsymbol{\xi}_T}$$

Gauge link for TMDs

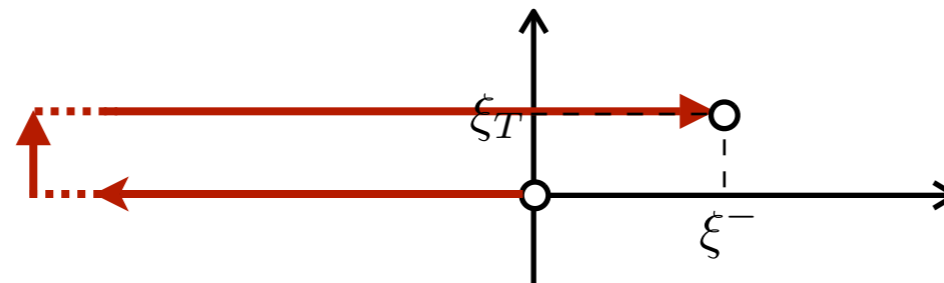
$$\Phi_{ij}(x, \mathbf{p}_T) = \int \frac{d\xi^- d^2\xi_T}{8\pi^3} e^{ip \cdot \xi} \langle P | \bar{\psi}_j(0) U_{[0, \xi]} \psi_i(\xi) | P \rangle \Big|_{\xi^+ = 0}$$

SIDIS



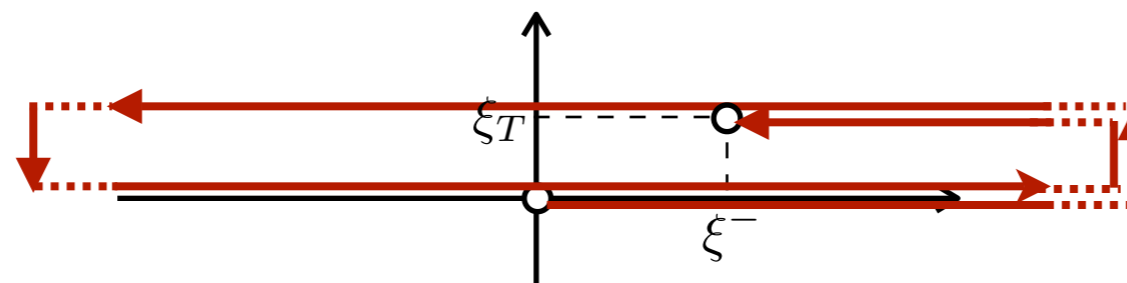
$U_{[+]}$

Drell-Yan



$U_{[-]}$

pp to hadrons

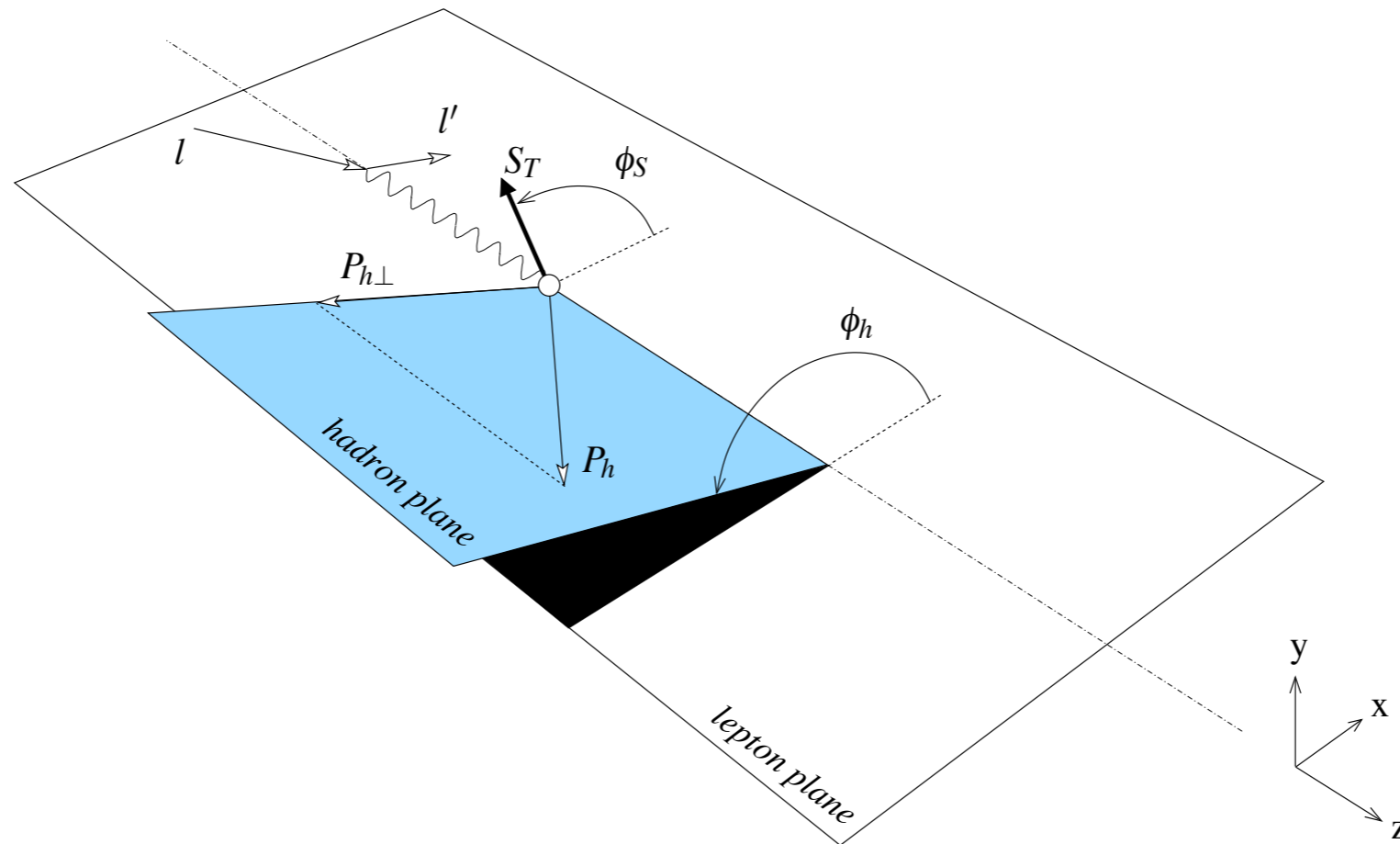


$U_{[\square]} U_{[+]}$

+ several others

High and low transverse momentum

SIDIS once again



Q = photon virtuality

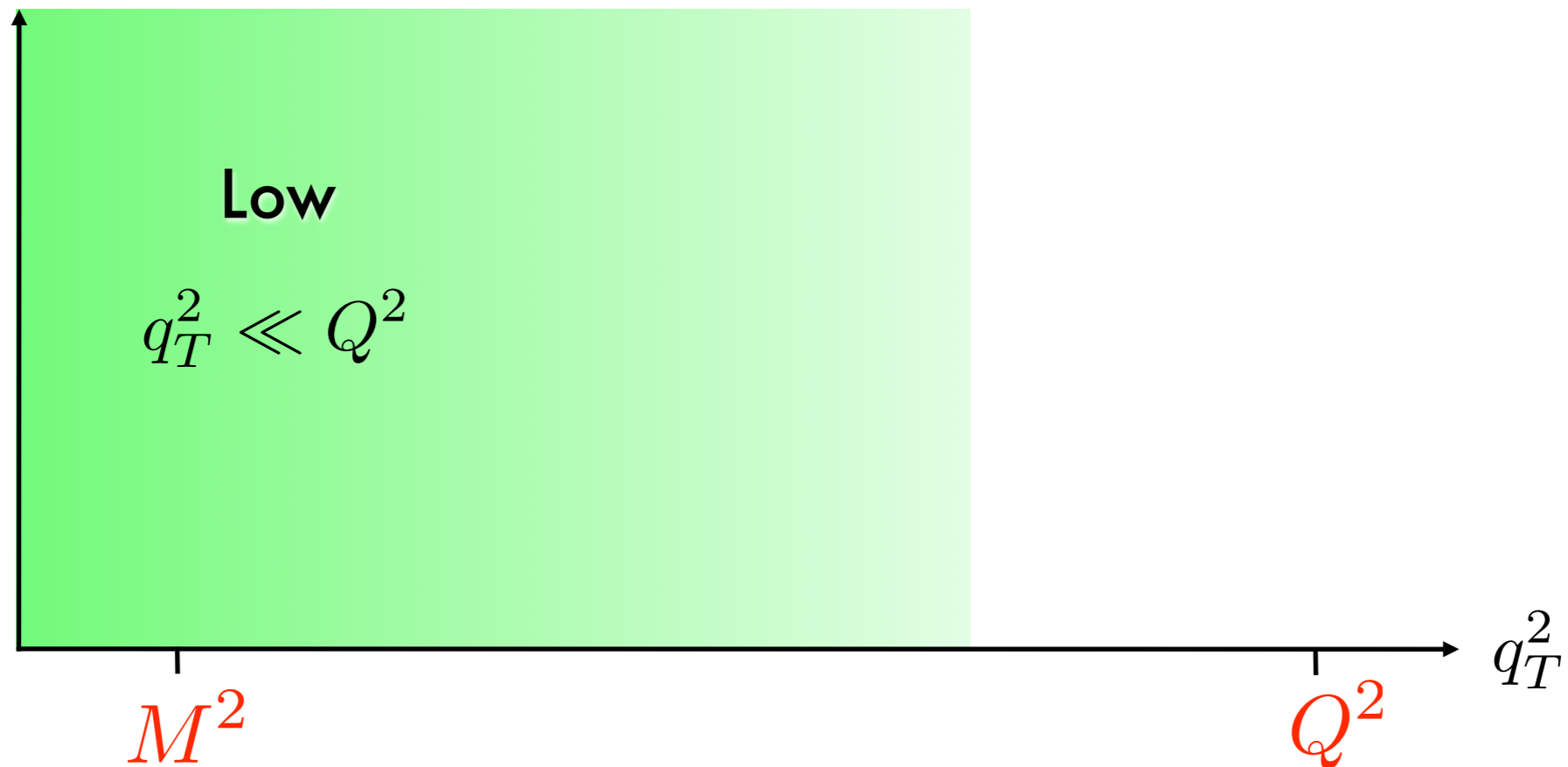
M = hadron mass

$P_{h\perp}$ = hadron transverse momentum

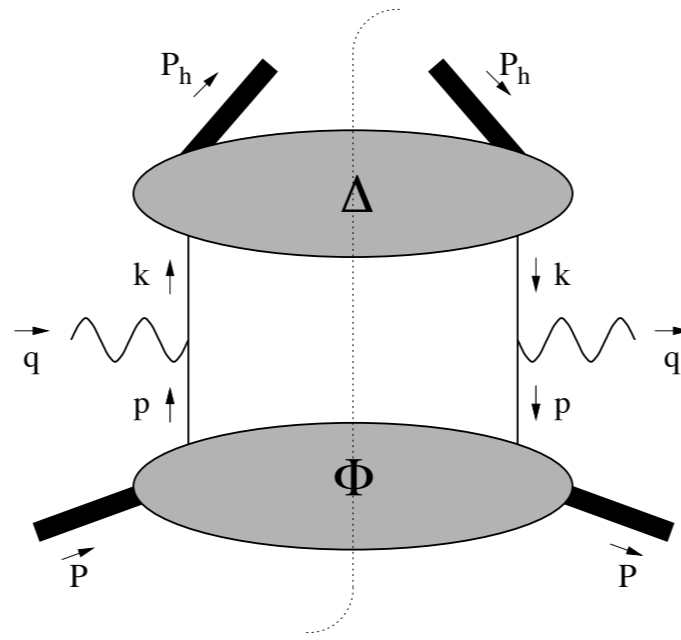
$$q_T^2 \approx P_{h\perp}^2 / z^2$$

Low and high transverse momentum

AB, D. Boer, M. Diehl, P.J. Mulders, JHEP 08 (08)



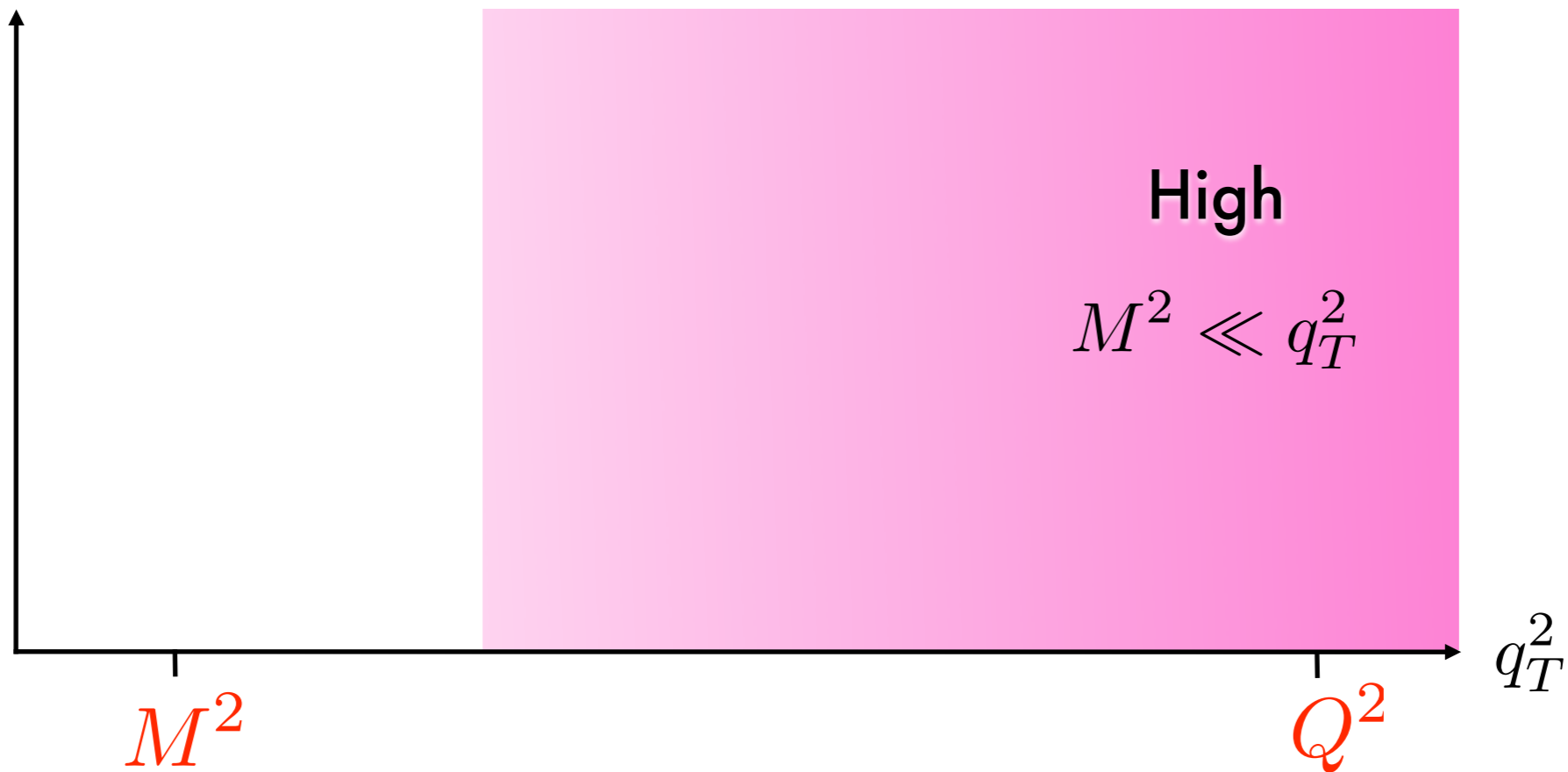
Example of low-transverse momentum result



$$F_{UU,T} = \mathcal{C}[f_1 D_1]$$

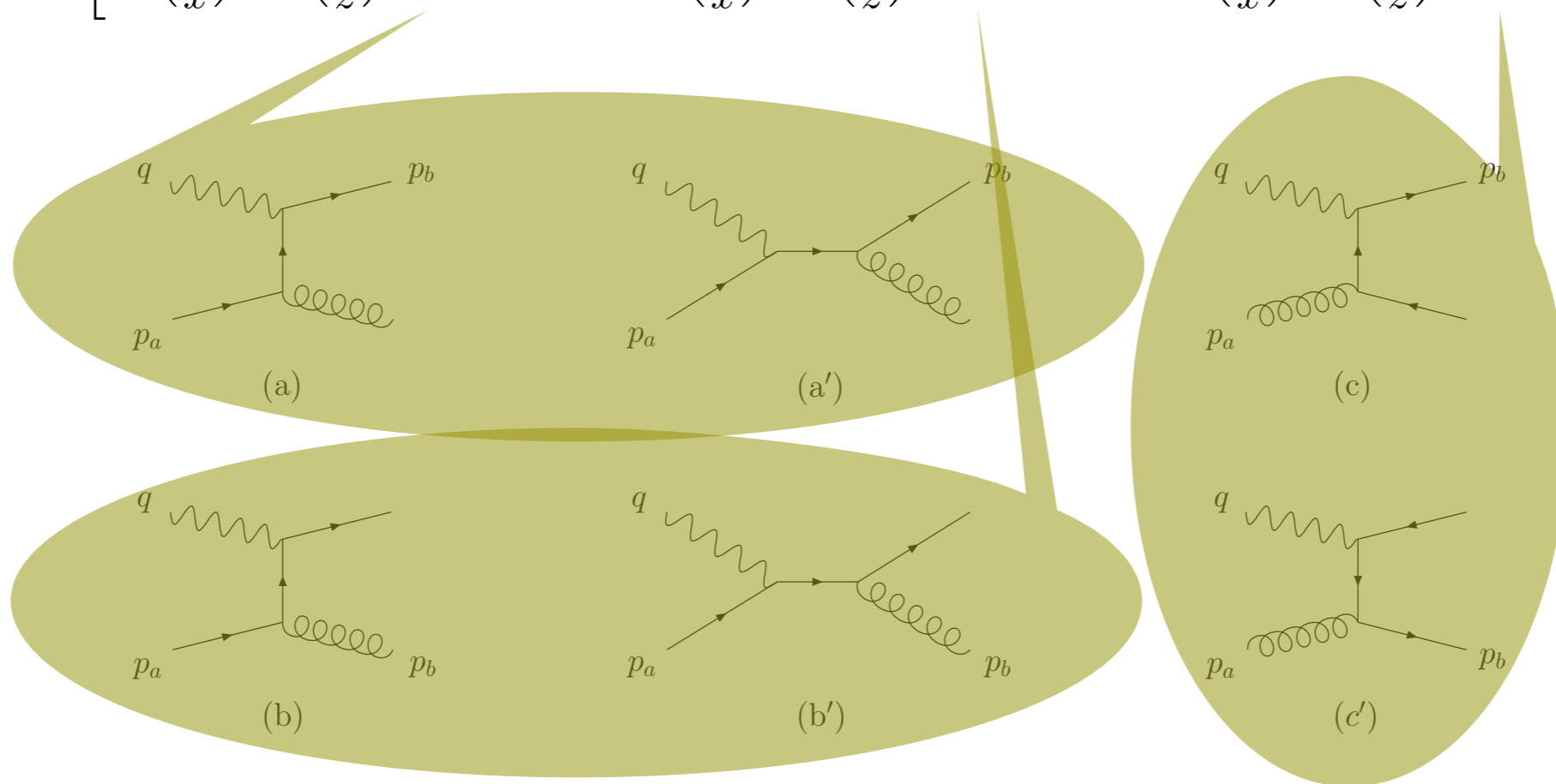
$$\mathcal{C}[wfD] = \sum_a x e_a^2 \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h\perp}/z) w(\mathbf{p}_T, \mathbf{k}_T) f^a(x, p_T^2) D^a(z, k_T^2),$$

Low and high transverse momentum

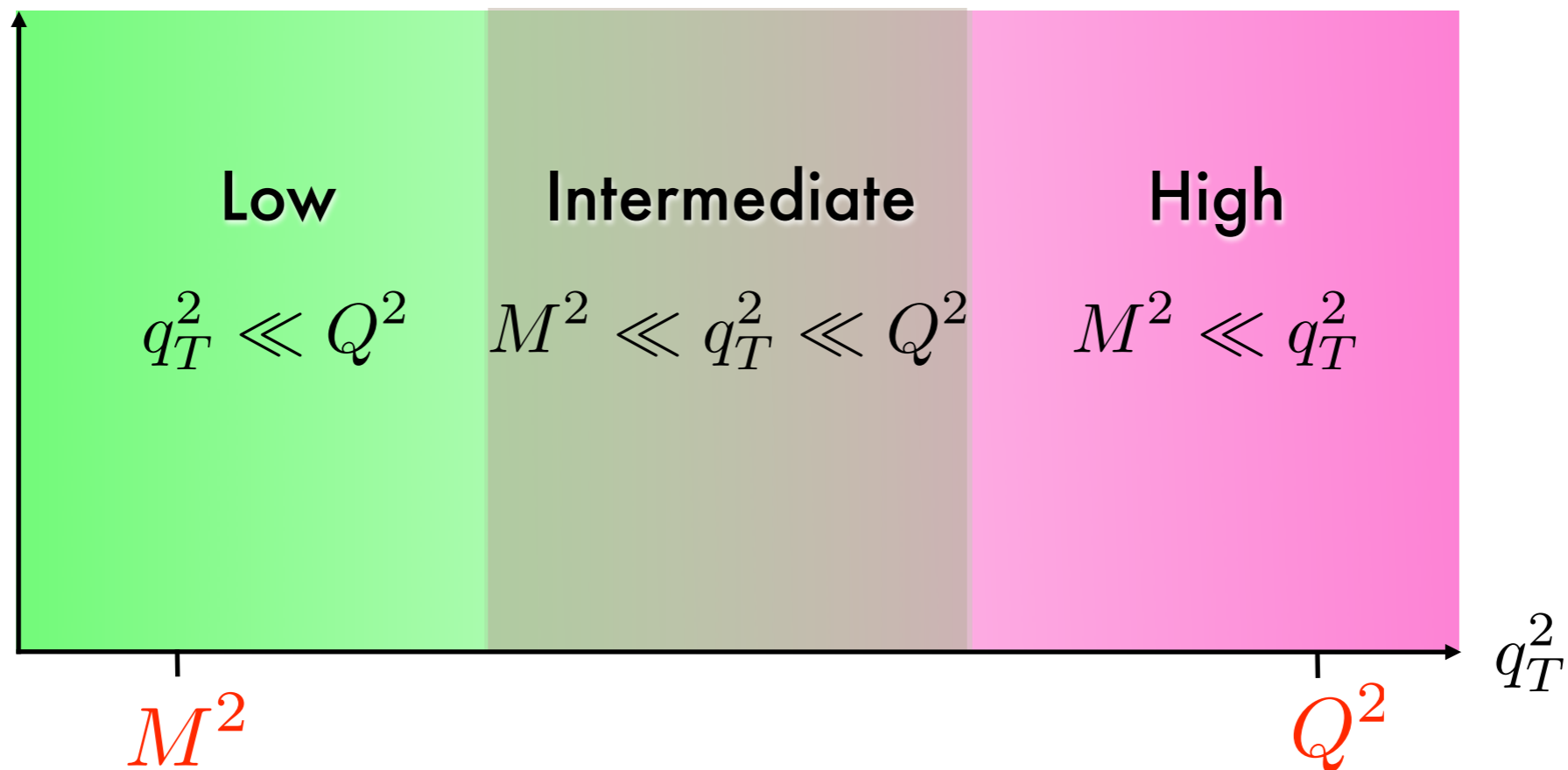


Example of high-transverse momentum result

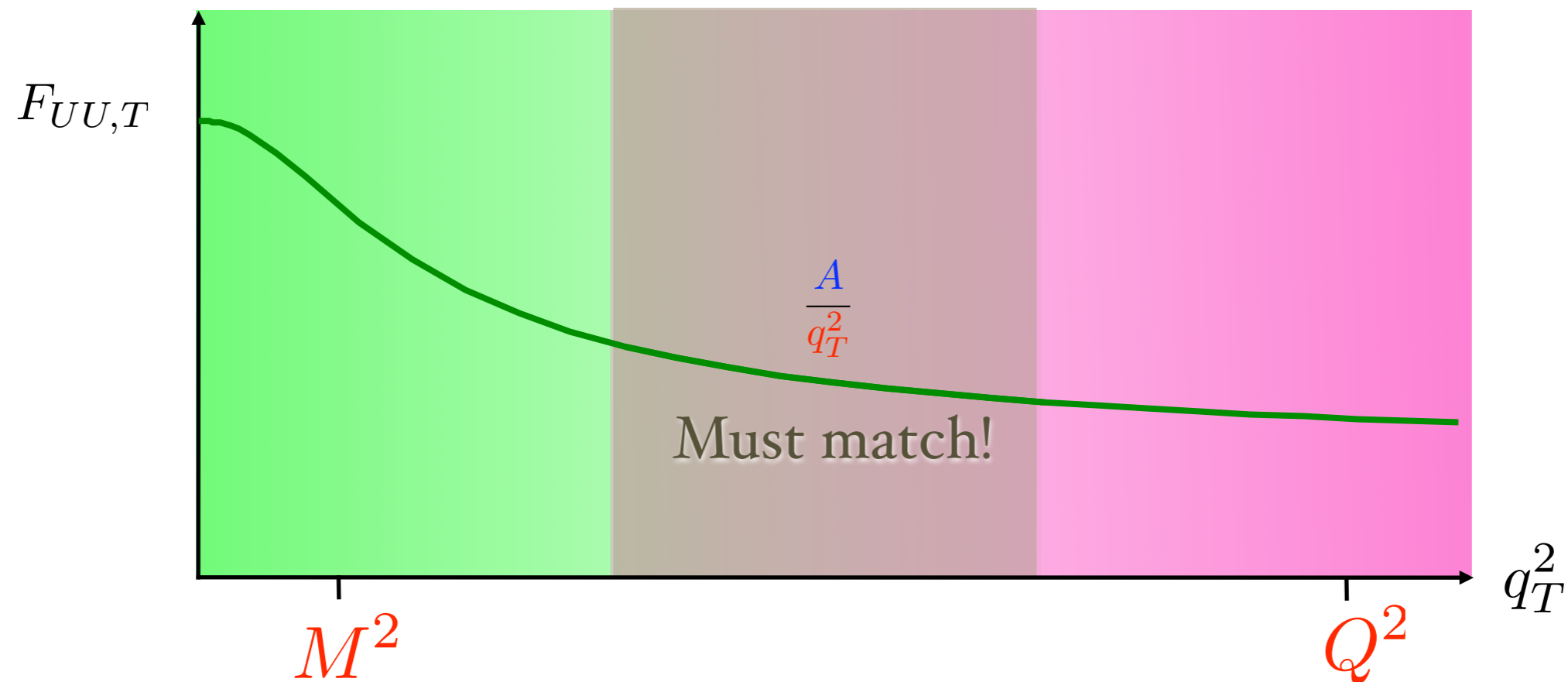
$$F_{UU,T} = \frac{1}{Q^2} \frac{\alpha_s}{(2\pi z)^2} \sum_a x e_a^2 \int_x^1 \frac{\hat{x}}{\hat{x}} \int_z^1 \frac{\hat{z}}{\hat{z}} \delta\left(\frac{q_T^2}{Q^2} - \frac{(1-\hat{x})(1-\hat{z})}{\hat{x}\hat{z}}\right) \\ \times \left[f_1^a\left(\frac{x}{\hat{x}}\right) D_1^a\left(\frac{z}{\hat{z}}\right) C_{UU,T}^{(\gamma^* q \rightarrow qg)} + f_1^a\left(\frac{x}{\hat{x}}\right) D_1^g\left(\frac{z}{\hat{z}}\right) C_{UU,T}^{(\gamma^* q \rightarrow gq)} + f_1^g\left(\frac{x}{\hat{x}}\right) D_1^a\left(\frac{z}{\hat{z}}\right) C_{UU,T}^{(\gamma^* g \rightarrow q\bar{q})} \right]$$



Low and high transverse momentum

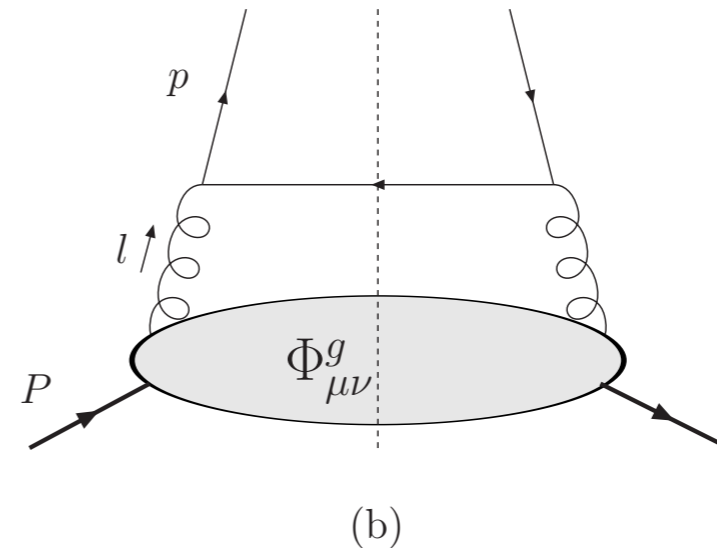
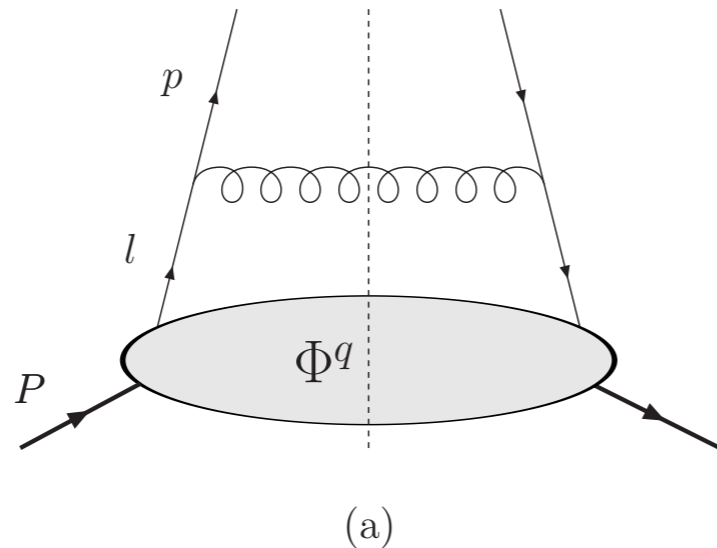


$F_{UU,T}$ structure function



The leading high- q_T part is just the “tail” of the leading low- q_T part

Perturbative corrections to TMDs



$$f_1^q(x, p_T^2) = \frac{\alpha_s}{2\pi^2} \frac{1}{p_T^2} \left[\frac{L(\eta^{-1})}{2} f_1^q(x) - C_F f_1^q(x) + (P_{qq} \otimes f_1^q + P_{qg} \otimes f_1^g)(x) \right],$$

$$F_{UU,T} = \frac{1}{q_T^2} \frac{\alpha_s}{2\pi^2 z^2} \sum_a x e_a^2 \left[f_1^a(x) D_1^a(z) L\left(\frac{Q^2}{q_T^2}\right) + f_1^a(x) (D_1^a \otimes P_{qq} + D_1^g \otimes P_{gq})(z) \right. \\ \left. + (P_{qq} \otimes f_1^a + P_{qg} \otimes f_1^g)(x) D_1^a(z) \right]$$

Large log,
needs resummation

where $L\left(\frac{Q^2}{q_T^2}\right) = 2C_F \ln \frac{Q^2}{q_T^2} - 3C_F$

DGLAP splitting
functions

Other TMDs

$$x f^\perp \sim \frac{1}{\mathbf{p}_T^2} \alpha_s \mathcal{F}[f_1],$$

...

$$f_{1T}^\perp \sim \frac{M^2}{\mathbf{p}_T^4} \alpha_s \mathcal{F}[f_{1T}^{\perp(1)}, \dots],$$

...

$$x f_L^\perp \sim \frac{1}{\mathbf{p}_T^2} \alpha_s^2 \mathcal{F}[g_1],$$

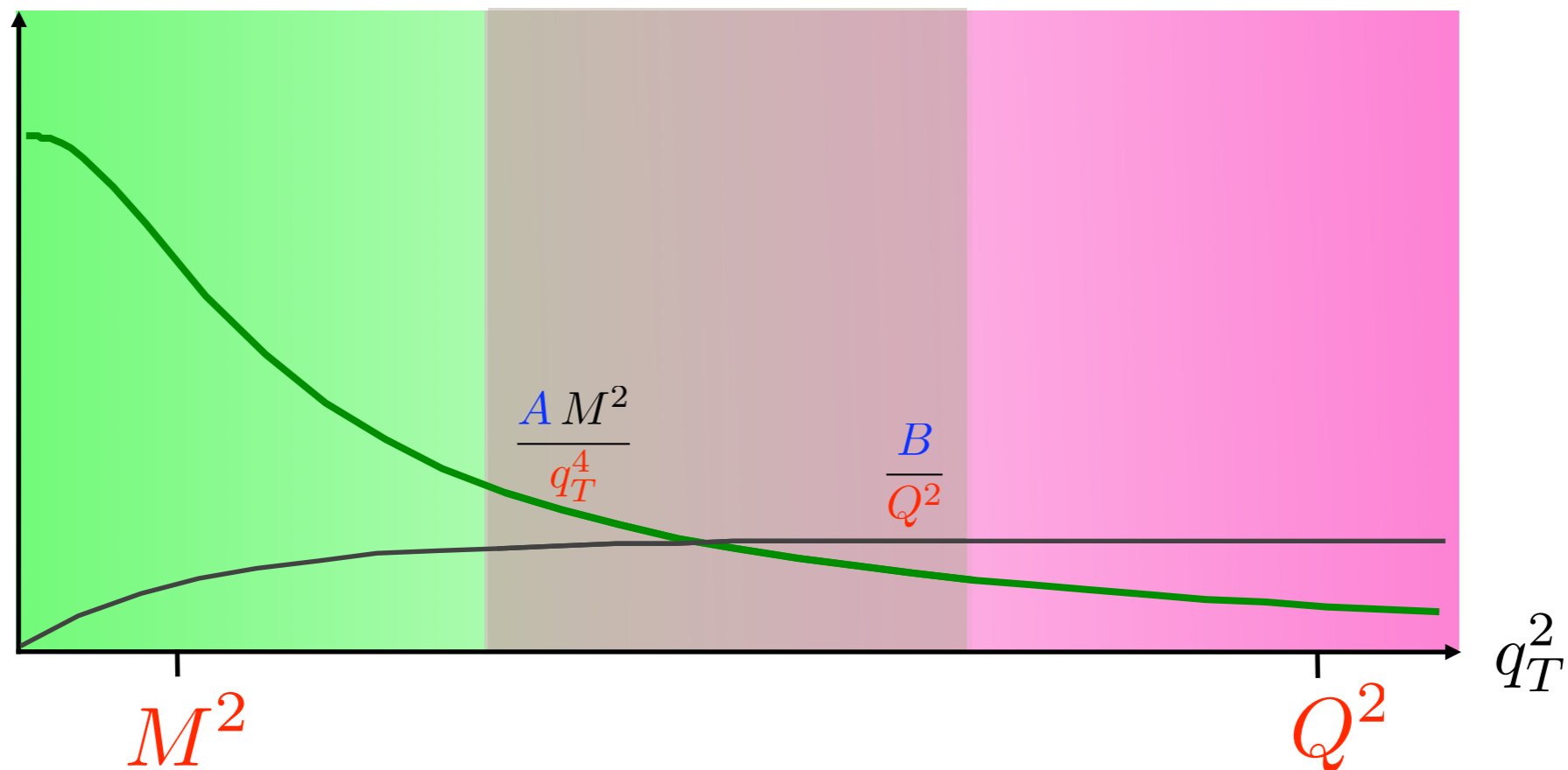
...

$$h_{1T}^\perp \sim \frac{M^2}{\mathbf{p}_T^4} \alpha_s^2 \mathcal{F}[h_1],$$

...

Expected mismatch

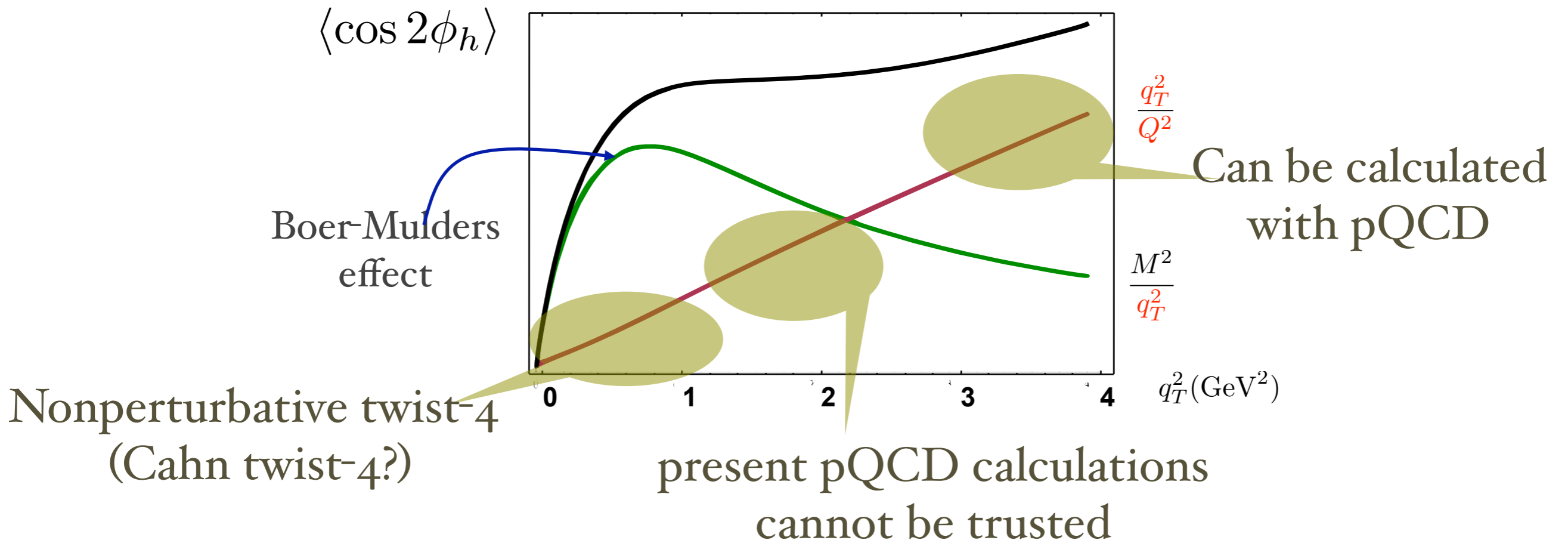
The leading terms in the two expansions
CANNOT and MUST not match!



Two distinct mechanisms are involved

Cos 2Φ asymmetry

see also Barone, Prokudin, Ma 0804.3024



All structure functions

AB, D. Boer, M. Diehl, P.J. Mulders, JHEP 08 (08)

observable	low- q_T calculation			high- q_T calculation			powers match
	twist	order	power	twist	order	power	
$F_{UU,T}$	2	α_s	$1/q_T^2$	2	α_s	$1/q_T^2$	yes
$F_{UU,L}$	4			2	α_s	$1/Q^2$?
$F_{UU}^{\cos \phi_h}$	3	α_s	$1/(Q q_T)$	2	α_s	$1/(Q q_T)$	yes
$F_{UU}^{\cos 2\phi_h}$	2	α_s	$1/q_T^4$	2	α_s	$1/Q^2$	no
$F_{LU}^{\sin \phi_h}$	3	α_s^2	$1/(Q q_T)$	2	α_s^2	$1/(Q q_T)$	yes
$F_{UL}^{\sin \phi_h}$	3	α_s^2	$1/(Q q_T)$				
$F_{UL}^{\sin 2\phi_h}$	2	α_s	$1/q_T^4$				
F_{LL}	2	α_s	$1/q_T^2$	2	α_s	$1/q_T^2$	yes
$F_{LL}^{\cos \phi_h}$	3	α_s	$1/(Q q_T)$	2	α_s	$1/(Q q_T)$	yes
$F_{UT,T}^{\sin(\phi_h - \phi_S)}$	2	α_s	$1/q_T^3$	3	α_s	$1/q_T^3$	yes
$F_{UT,L}^{\sin(\phi_h - \phi_S)}$	4			3	α_s	$1/(Q^2 q_T)$?
$F_{UT}^{\sin(\phi_h + \phi_S)}$	2	α_s	$1/q_T^3$	3	α_s	$1/q_T^3$	yes
$F_{UT}^{\sin(3\phi_h - \phi_S)}$	2	α_s^2	$1/q_T^3$	3	α_s	$1/(Q^2 q_T)$	no
$F_{UT}^{\sin \phi_S}$	3	α_s	$1/(Q q_T^2)$	3	α_s	$1/(Q q_T^2)$	yes
$F_{UT}^{\sin(2\phi_h - \phi_S)}$	3	α_s	$1/(Q q_T^2)$	3	α_s	$1/(Q q_T^2)$	yes
$F_{LT}^{\cos(\phi_h - \phi_S)}$	2	α_s	$1/q_T^3$				
$F_{LT}^{\cos \phi_S}$	3	α_s	$1/(Q q_T^2)$				
$F_{LT}^{\cos(2\phi_h - \phi_S)}$	3	α_s	$1/(Q q_T^2)$				

conjectures!



Evolution equations

Collinear evolution of transversity

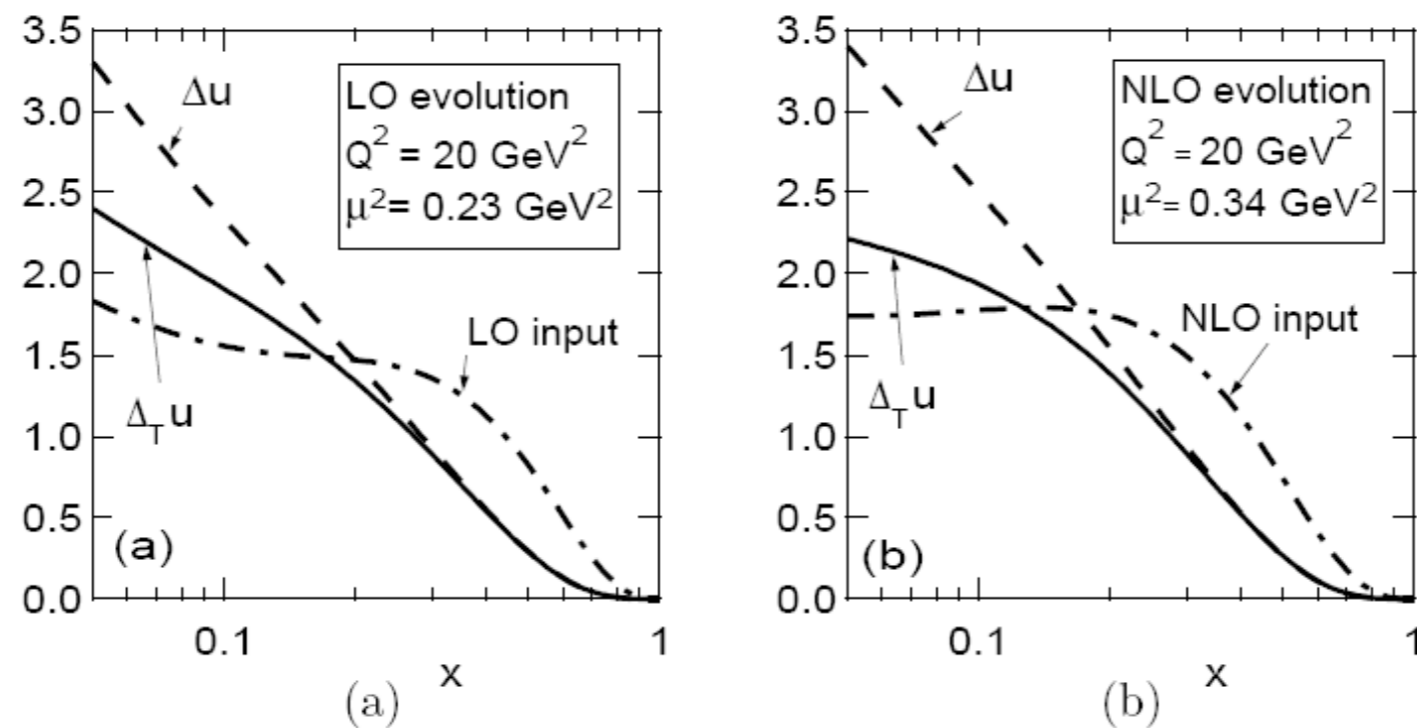
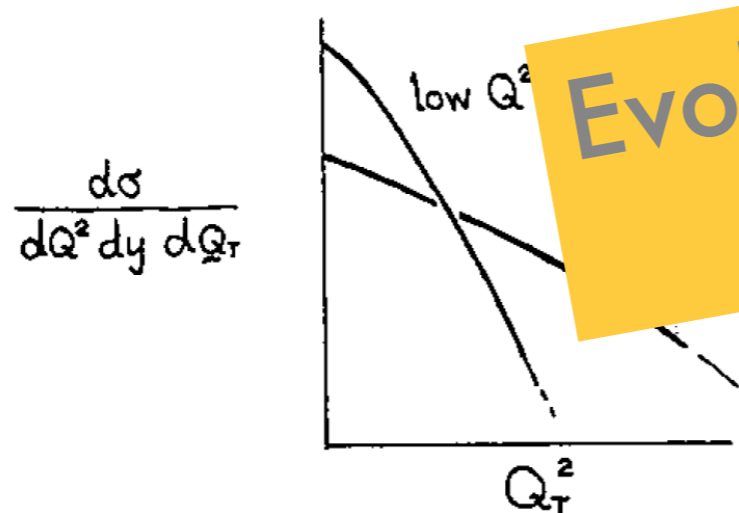


Fig. 19. Comparison of the Q^2 -evolution of $\Delta_T u(x, Q^2)$ and $\Delta u(x, Q^2)$ at (a) LO and (b) NLO, from [72].

Barone, Drago, Ratcliffe, PR 359 (2002)

Hayashigaki, Kanazawa, Koike, PRD56 (97)

TMDs evolution

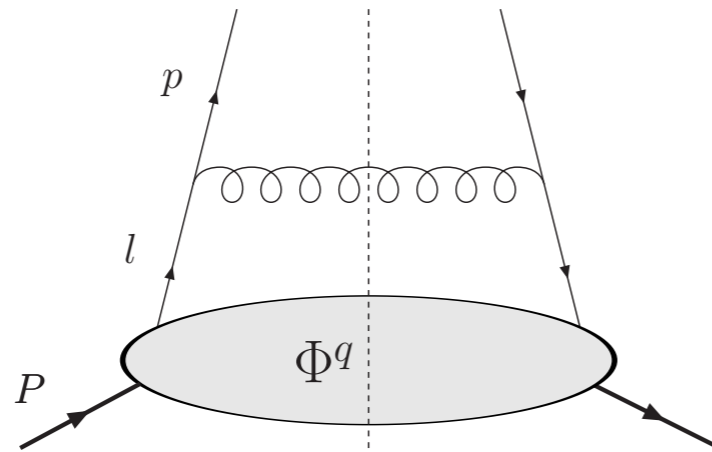


Evolution equations for TMDs are NOT standard DGLAP

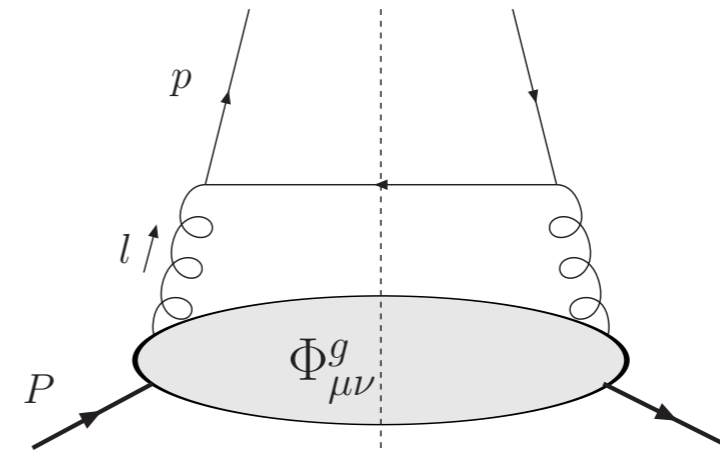
*Collins, Soper, Sterman, talk at Fermilab
Workshop on Drell-Yan Process, Batavia, Ill.,
Oct 7-8, 1982*

Fig 3 Broadening of the Q_T distribution

Perturbative corrections to TMDs



(a)



(b)

$$f_1^q(x, p_T^2) = \frac{\alpha_s}{2\pi^2} \frac{1}{p_T^2} \left[\frac{L(\eta^{-1})}{2} f_1^q(x) - C_F f_1^q(x) + (P_{qq} \otimes f_1^q + P_{qg} \otimes f_1^g)(x) \right],$$

$$F_{UU,T} = \frac{1}{q_T^2} \frac{\alpha_s}{2\pi^2 z^2} \sum_a x e_a^2 \left[f_1^a(x) D_1^a(z) L\left(\frac{Q^2}{q_T^2}\right) + f_1^a(x) (D_1^a \otimes P_{qq} + D_1^g \otimes P_{gq})(z) \right. \\ \left. + (P_{qq} \otimes f_1^a + P_{qg} \otimes f_1^g)(x) D_1^a(z) \right]$$

Large log,
needs resummation

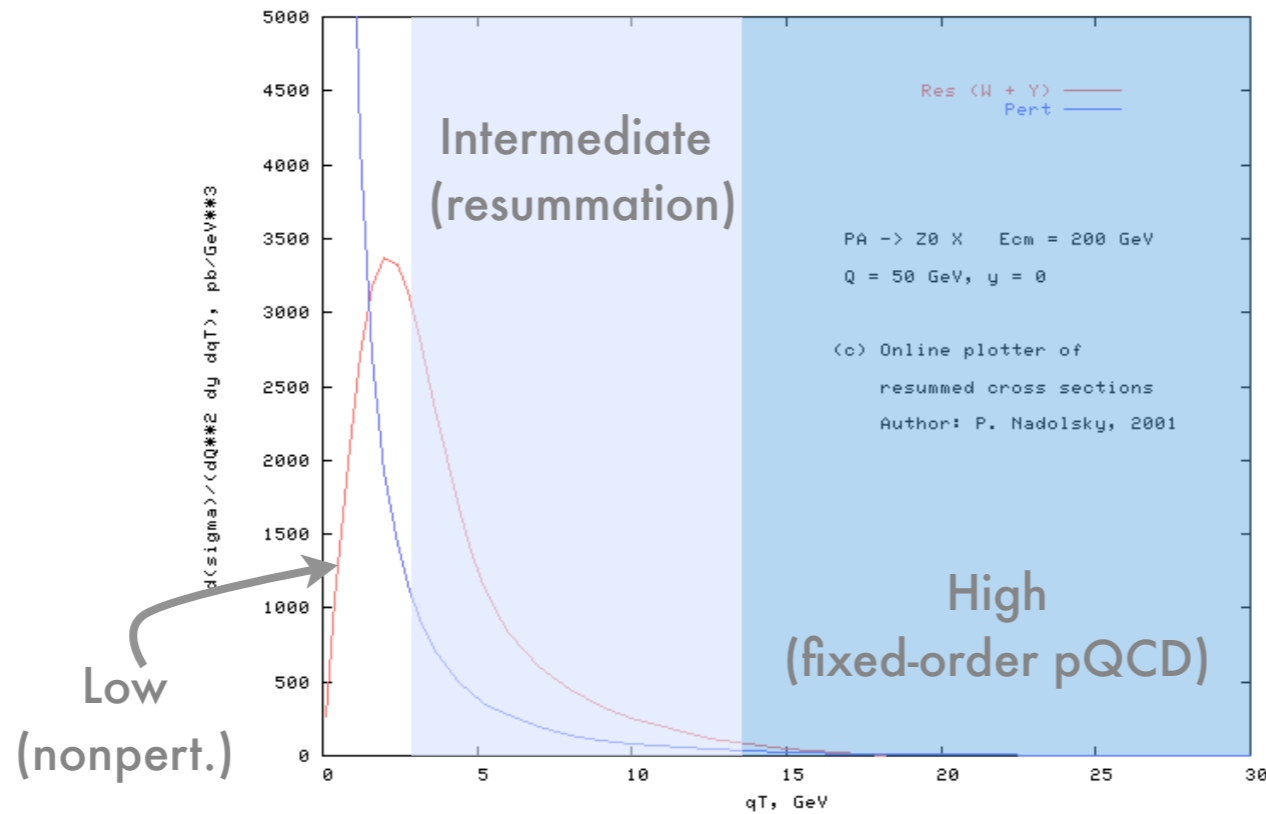
where $L\left(\frac{Q^2}{q_T^2}\right) = 2C_F \ln \frac{Q^2}{q_T^2} - 3C_F$

DGLAP splitting
functions

Resummation results

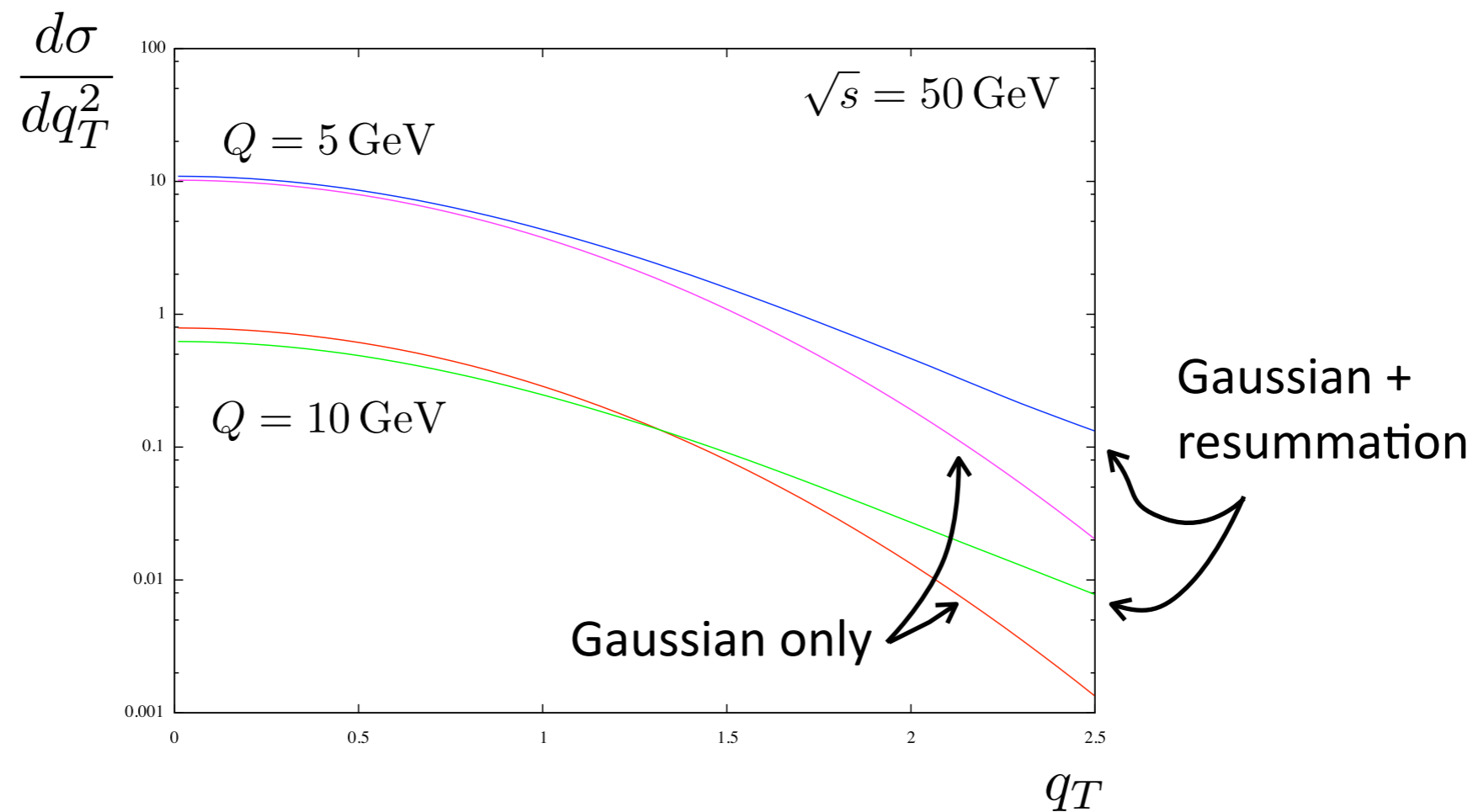
$$F_{UU,T}(x, z, b, Q^2) = x \sum_a e_a^2 \left[(f_1^i \otimes C_{ia}) (C_{aj} \otimes D_1^j) e^{-S} e^{-S_{NP}} \right]$$

collinear PDF and FF calculable with pQCD nonperturbative part of TMDs



$$F_{UU,T}(x, z, q_T^2, Q^2) = x \sum_a e_a^2 \frac{d}{dq_T^2} \left[(f_1^i \otimes C_{ia}) (C_{aj} \otimes D_1^j) e^{-S} (1 - e^{-S_{NP}}) \right]$$

Example of resummation effects



Leading-log formula

Ellis, Veseli, NPB 511 (98)

$$F_{UU,T}(x, z, q_T^2, Q^2) = x \sum_a e_a^2 \frac{d}{dq_T^2} \left[f_1^a(x; [q_T^2]) D_1^a(z; [q_T^2]) e^{-S} (1 - e^{-S_{NP}}) \right]$$

$$S(q_T^2, Q^2) = - \int_{q_T^2}^{Q^2} \frac{d\mu^2}{\mu^2} \frac{\alpha_S(\mu^2)}{2\pi} 2C_F \log \frac{Q^2}{\mu^2}$$

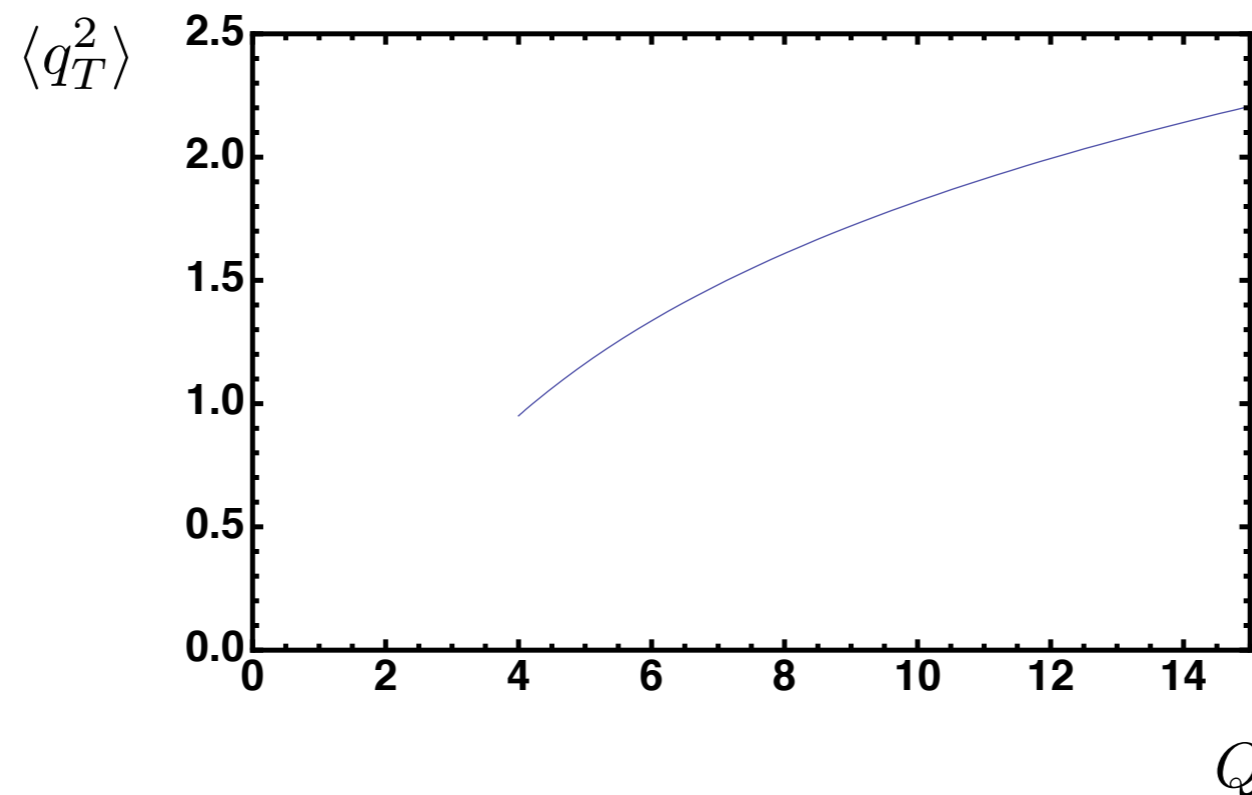
$$\alpha_S(\mu^2) = \frac{4\pi}{\beta_0 \log(\mu^2/\Lambda^2)}$$

Nonperturbative part

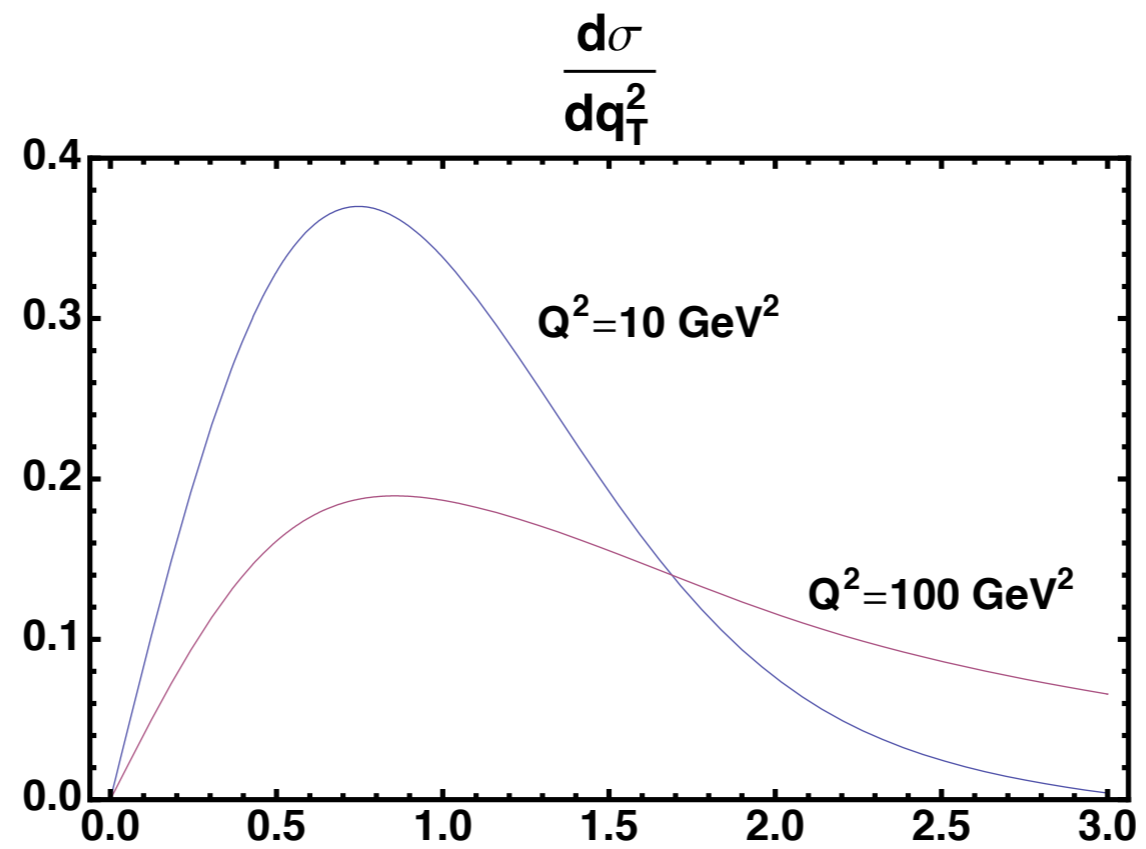
Kulesza, Stirling, JHEP 12 (03)

$$S_{NP} = -\frac{q_T^2}{\langle q_T^2 \rangle}$$

$$\frac{1}{\langle q_T^2 \rangle} = 0.20 + 0.95 \log\left(\frac{Q}{3.2}\right) + 1.56 \log\left(\frac{\sqrt{s}}{19.4}\right)$$



Leading-log evolution



Evolution of Sivers function

$$f_1^{\text{NS}}(x, p_T^2) = \frac{\alpha_s}{2\pi^2} \frac{1}{p_T^2} \left[\left(\frac{L(\eta^{-1})}{2} - C_F \right) f_1^{\text{NS}}(x) + (P_{qq} \otimes f_1^{\text{NS}}) \right]$$

$$\frac{p_T^2}{2M^2} f_{1T}^{\perp \text{NS}}(x, p_T^2) = \frac{\alpha_s}{2\pi^2} \frac{M}{p_T^2} \left[\left(\frac{L(\eta^{-1})}{2} - C_F \right) f_{1T}^{\perp(1)\text{NS}}(x) + \dots \right]$$

$$F_{UU,T} = \frac{1}{q_T^2} \frac{\alpha_s}{2\pi^2 z^2} \sum_a x e_a^2 \left[f_1^a(x) D_1^a(z) L\left(\frac{Q^2}{q_T^2}\right) + \dots \right]$$

$$\frac{q_T}{M} F_{UT,T}^{\sin(\phi_h - \phi_s)} = \frac{1}{q_T^2} \frac{\alpha_s}{2\pi^2 z^2} \sum_a x e_a^2 \left[-f_{1T}^{\perp(1)a}(x) D_1^a(z) L\left(\frac{Q^2}{q_T^2}\right) + \dots \right] \text{ ?}$$

Collins asymmetry, b space analysis

D. Boer, NPB 806 (08)

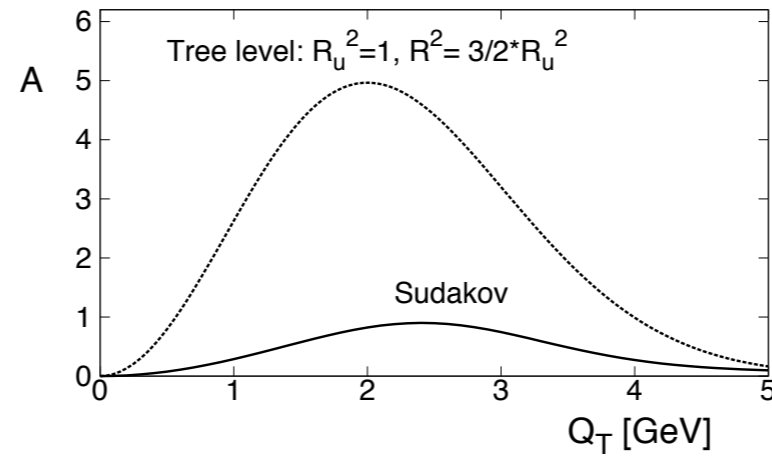


FIG. 6: The asymmetry factor $\mathcal{A}(Q_T)$ at $Q = 10$ GeV (solid curve) and the tree level quantity $\mathcal{A}^{(0)}(Q_T)$ using $R_u^2 = 1 \text{ GeV}^{-2}$ and $R^2/R_u^2 = 3/2$. Both factors are given in units of M^2 .

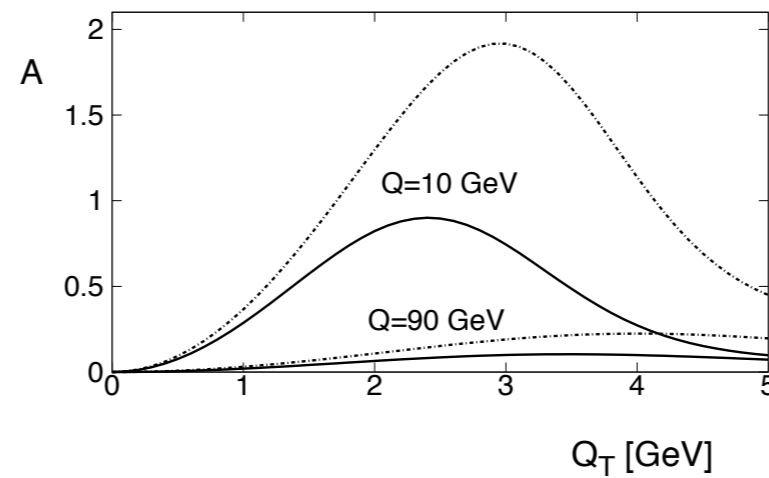


FIG. 5: The asymmetry factor $\mathcal{A}(Q_T)$ (in units of M^2) at $Q = 10$ GeV and $Q = 90$ GeV. The solid curves are obtained with the method explained in the text; the dashed-dotted curves are from the earlier analysis of Ref. [64].

Evolution of transverse moment of Sivers function

Vogelsang, Yuan, talk at SPIN08

Kang, Qiu, arXiv:0811.3101 [hep-ph]

$$\frac{\partial f_1^{\text{NS}}(x, \mu^2)}{\partial \ln \mu^2} = \frac{\alpha_s(\mu^2)}{2\pi} \int_x^1 \frac{d\xi}{\xi} f_1^{\text{NS}}(\xi, \mu^2) P_{qq}(z) \Big|_{z=x/\xi}$$

$$\begin{aligned} \frac{\partial \mathcal{T}_{q,F}(x, x, \mu_F)}{\partial \ln \mu_F^2} = & \frac{\alpha_s}{2\pi} \int_x^1 \frac{d\xi}{\xi} \left\{ P_{qq}(z) \mathcal{T}_{q,F}(\xi, \xi, \mu_F) \right. \\ & + \frac{C_A}{2} \left[\frac{1+z^2}{1-z} [\mathcal{T}_{q,F}(\xi, x, \mu_F) - \mathcal{T}_{q,F}(\xi, \xi, \mu_F)] + z \mathcal{T}_{q,F}(\xi, x, \mu_F) \right] \\ & \left. + \frac{C_A}{2} [\mathcal{T}_{\Delta q,F}(x, \xi, \mu_F)] \right\}, \end{aligned} \quad \mathcal{T}_F(x, x) \equiv 2M f_{1T}^{\perp(1)}(x)$$

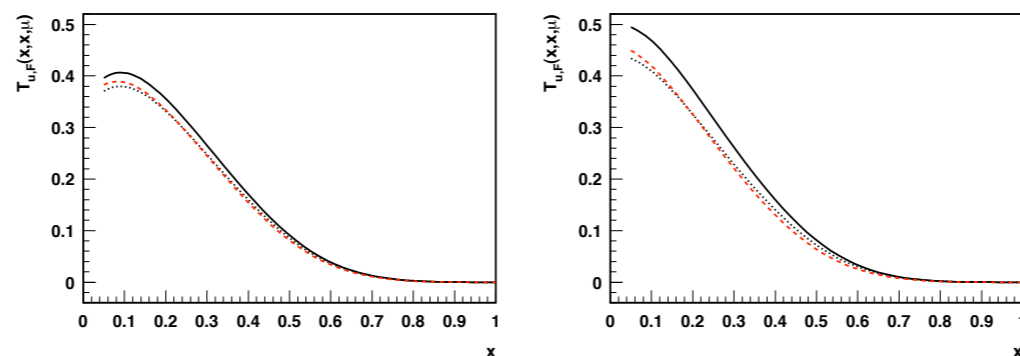
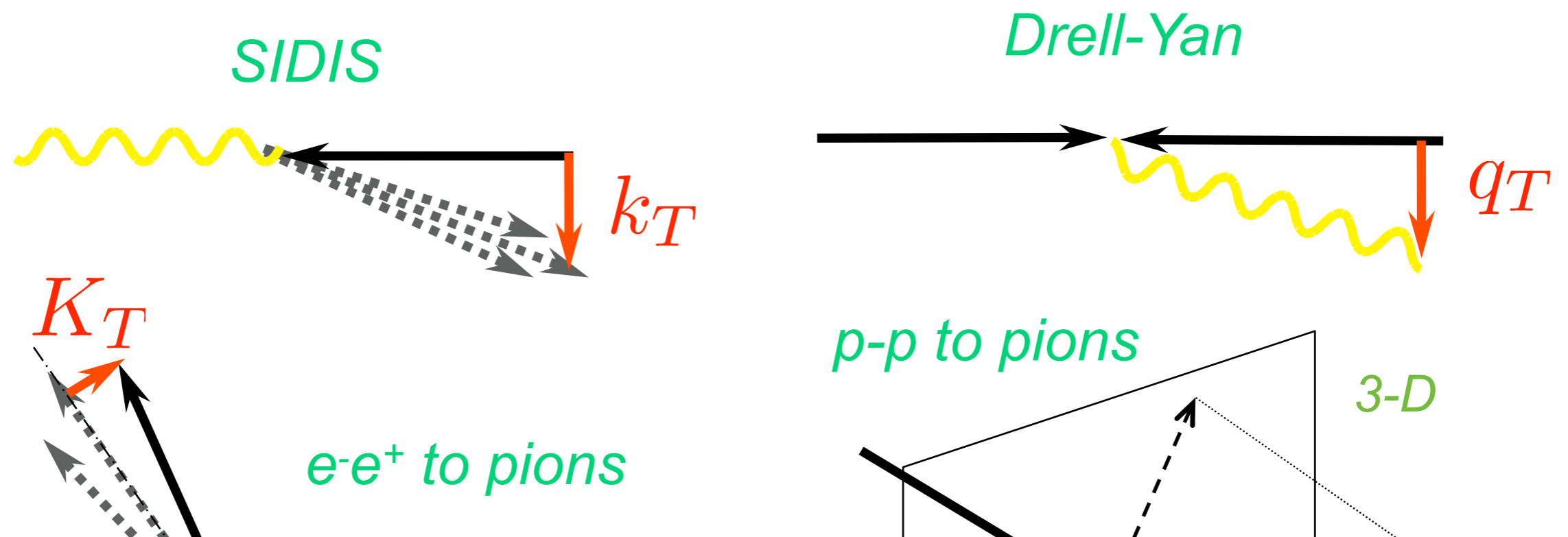


FIG. 12: Twist-3 up-quark-gluon correlation $T_{u,F}(x, x, \mu_F)$ as a function of x at $\mu_F = 4$ GeV (left) and $\mu_F = 10$ GeV (right). The factorization scale dependence is a solution of the flavor non-singlet evolution equation in Eq. (99). Solid and dotted curves correspond to $\sigma = 1/4$ and $1/8$, while the dashed curve is obtained by keeping only the DGLAP evolution kernel $P_{qq}(z)$ in Eq. (99).

Factorization and universality

Different processes

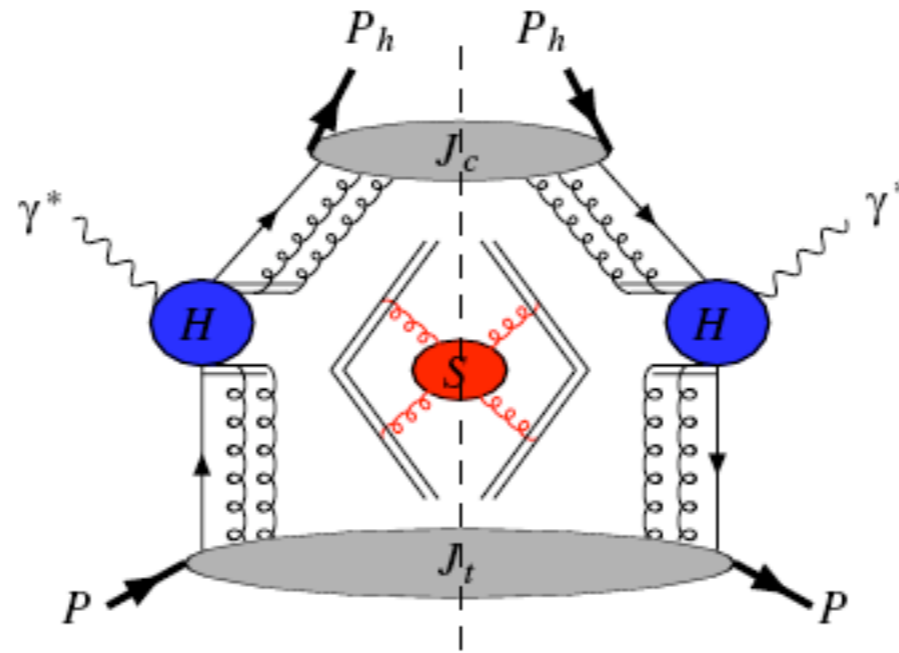


Whenever we measure transverse-momentum effects, we need k_T -factorization and we need transverse momentum dependent (or unintegrated) parton distributions

Collins, Soper, NPB 193 (81)

R_T

k_T factorization



$$F_{UU,T}(x, z, P_{h\perp}^2, Q^2) = C [f_1 D_1]$$

$$= \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T d^2 \mathbf{l}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T + \mathbf{l}_T - \mathbf{P}_{h\perp}/z)$$

$$x \sum_a e_a^2 f_1^a(x, p_T^2, \mu^2) D_1^a(z, k_T^2, \mu^2) U(l_T^2, \mu^2) H(Q^2, \mu^2)$$

TMD PDF

TMD FF

Soft factor

Hard part

Collins, Soper, NPB 193 (81)

Ji, Ma, Yuan, PRD 71 (05)

Consequences

- The real part of the gauge link remains unchanged
- The imaginary part changes sign
- Observables sensitive to the imaginary part (e.g. single spin asymmetries) acquire an extra minus sign (generalization of universality)

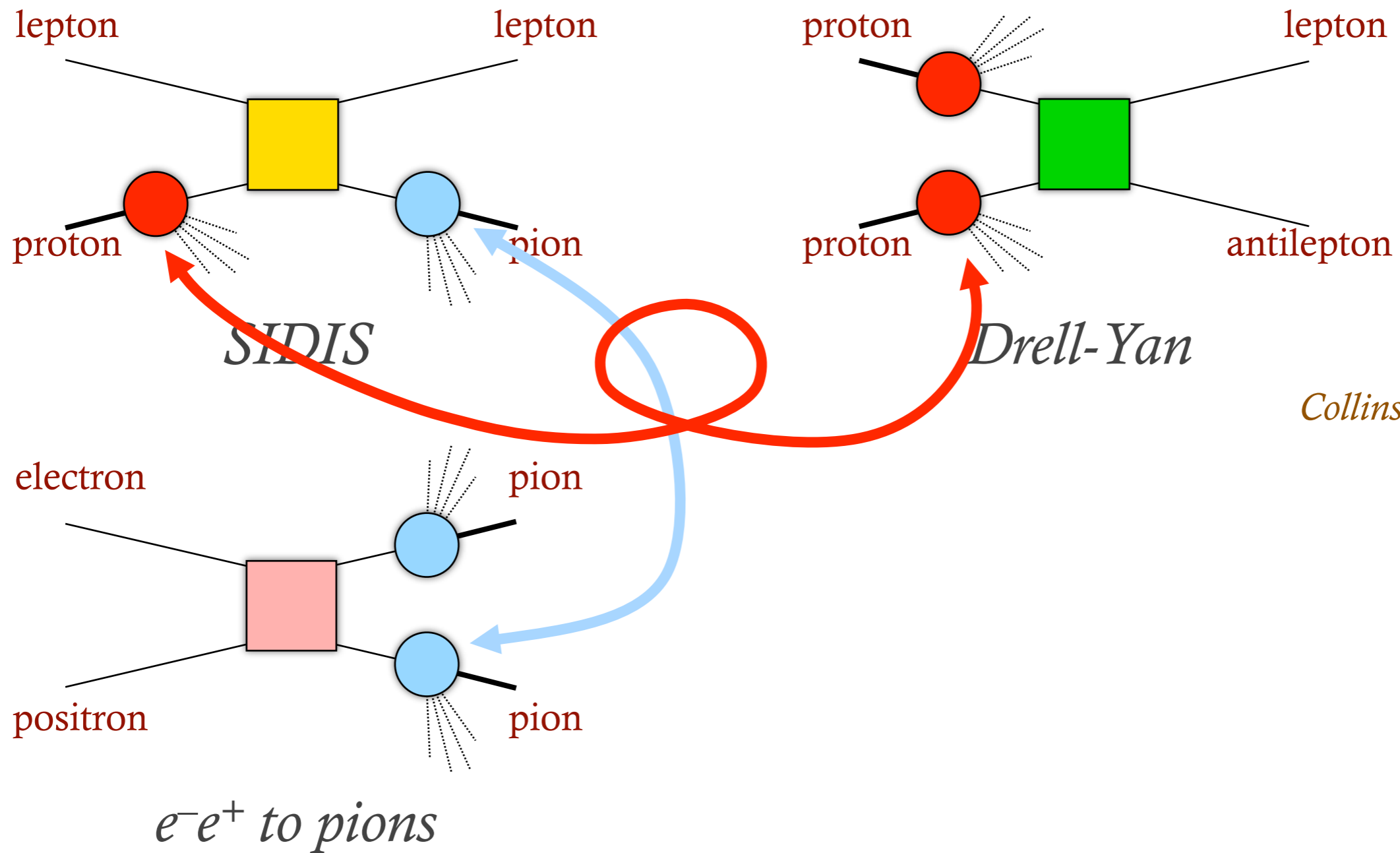
$$d\sigma_{DIS} = H_{DIS} \otimes f$$

$$d\sigma_{DY} = H_{DY} \otimes f$$

$$d\sigma_{DIS}^{\uparrow} - d\sigma_{DIS}^{\downarrow} = K_{DIS} \otimes g$$

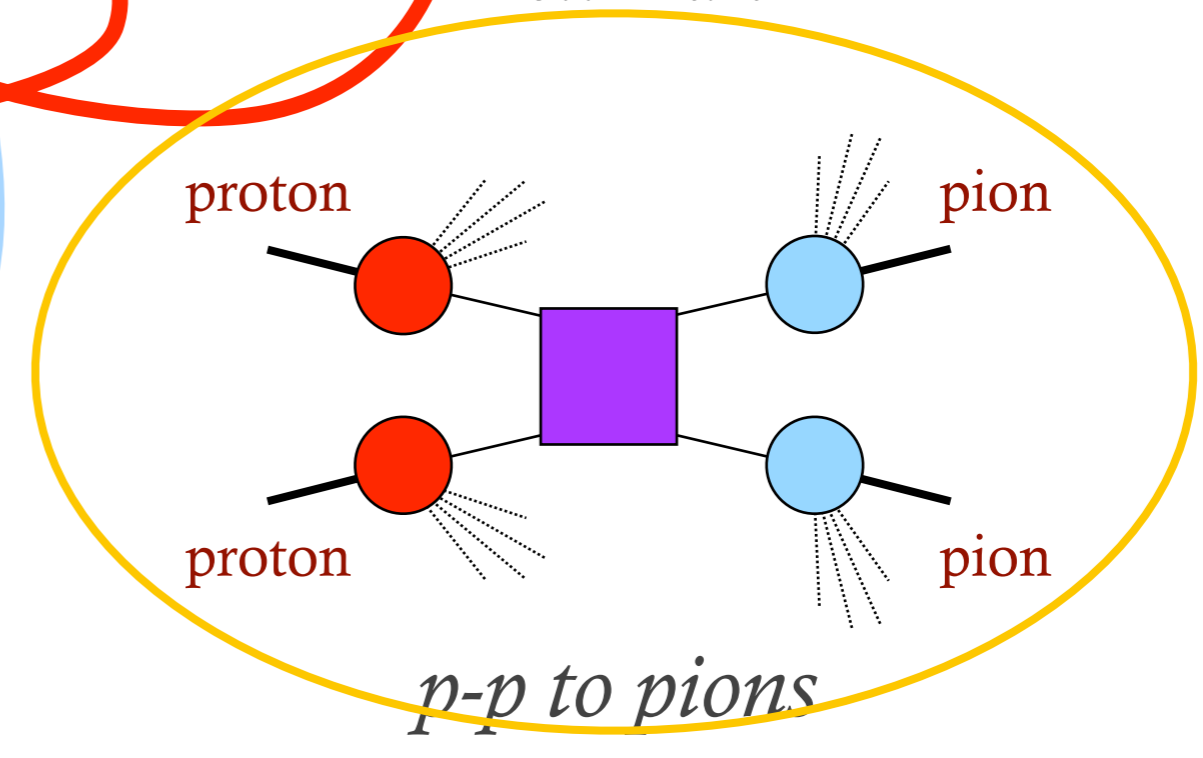
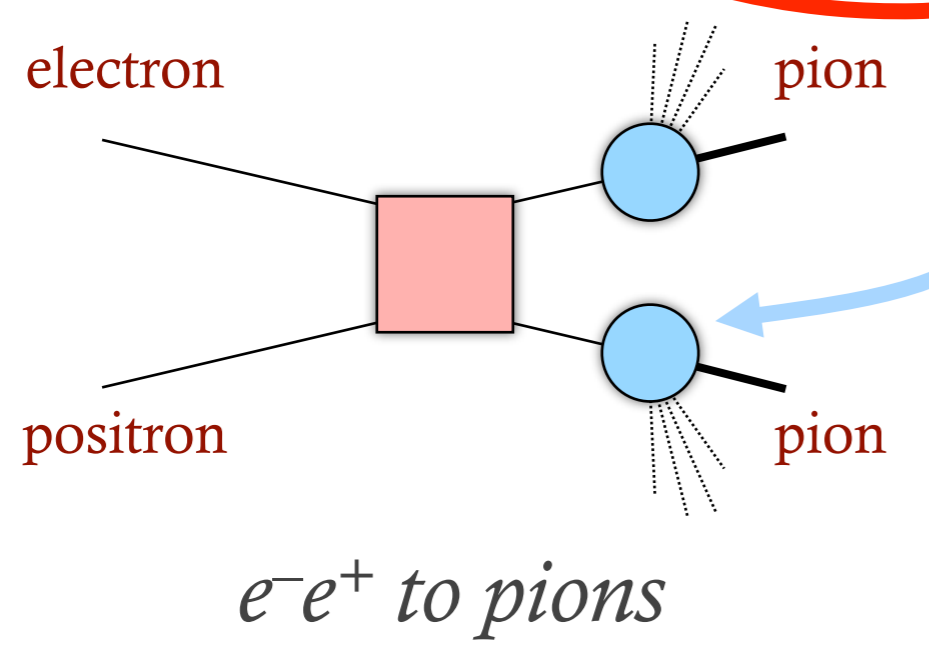
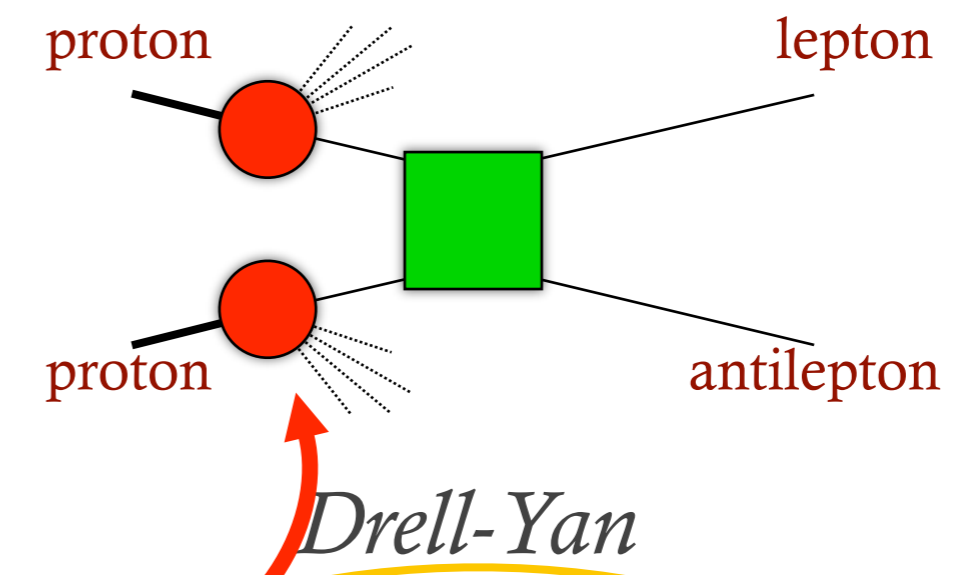
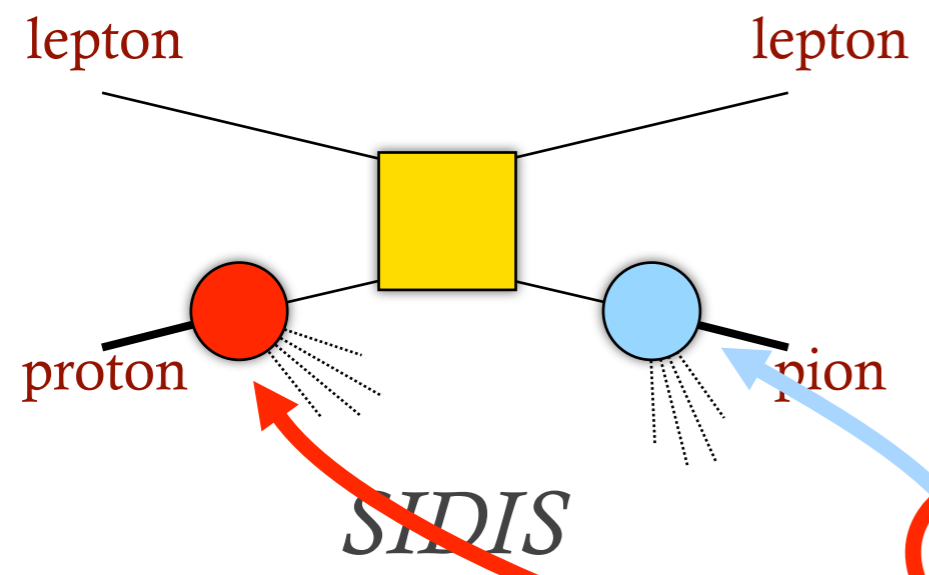
$$d\sigma_{DIS}^{\uparrow} - d\sigma_{DIS}^{\downarrow} = -K_{DY} \otimes g$$

Generalized universality



Collins, PLB 536 (02)

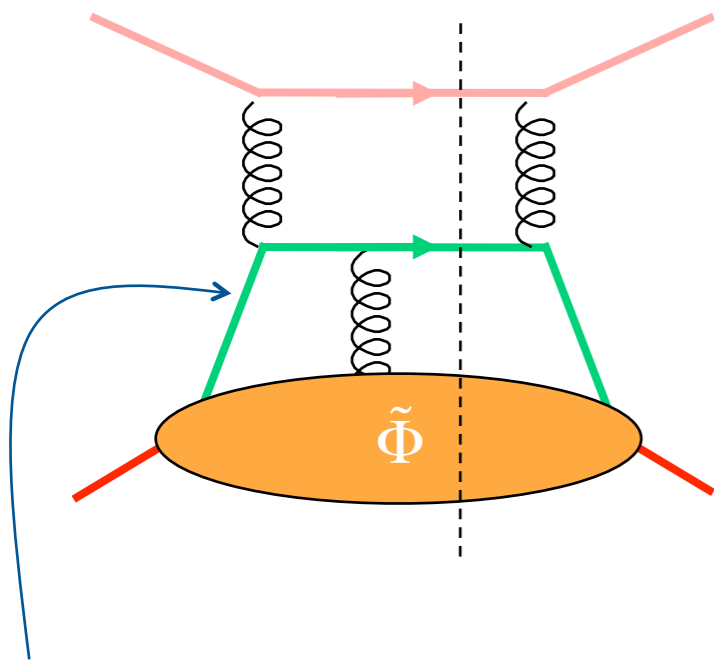
Hadrons to hadrons



A slightly more complex example

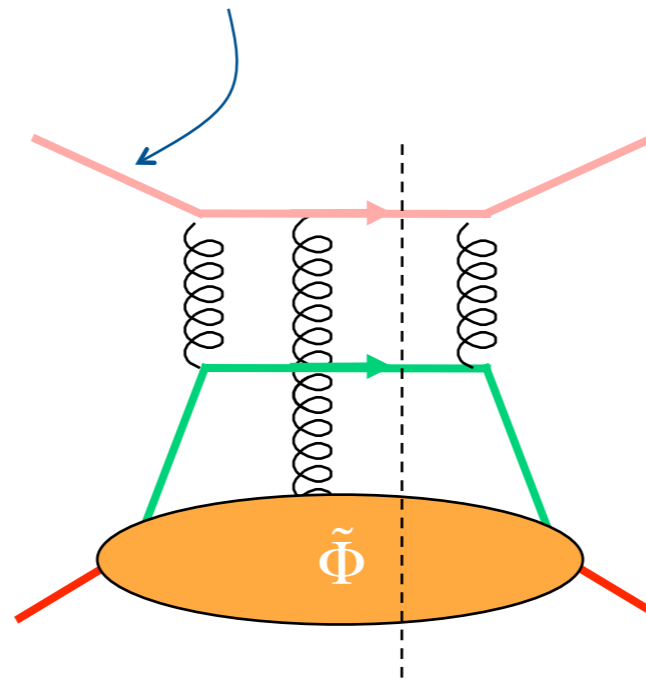
parton with charge g_2

Collins, Qiu, PRD 75 (07)

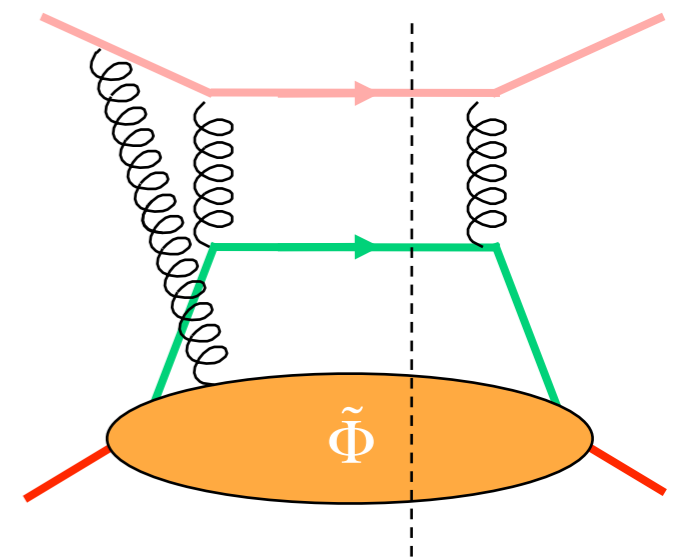


parton with charge g_1

$$\frac{g_1}{[-l^+ + i\epsilon]}$$



$$\frac{g_2}{[-l^+ + i\epsilon]}$$



$$-\frac{g_2}{[-l^+ + i\epsilon]}$$

Consequences

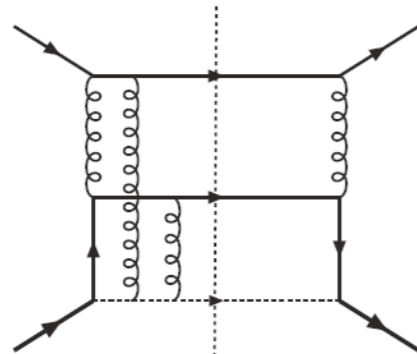
$$\frac{g_1}{[-l^+ + i\epsilon]} + \frac{g_2}{[-l^+ + i\epsilon]} - \frac{g_2}{[-l^+ + i\epsilon]} = -i\pi(2g_2 + g_1)\delta(l^+) - PV\frac{g_1}{l^+}$$

- Up to this order, the real part is unchanged, the imaginary part gets more than just a simple sign change and depends on the charge of ANOTHER parton!
- Still possible to get around it: PDFs could still be universal, but the ones sensitive to the imaginary part (those involved in single spin asymmetries) have to be multiplied by $g_1/(2g_2+g_1)$

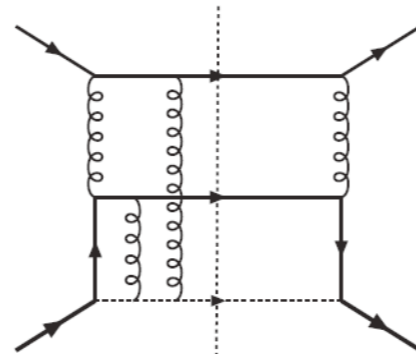
Two-gluon exchange

Collins, 0708.4410 [hep-ph]

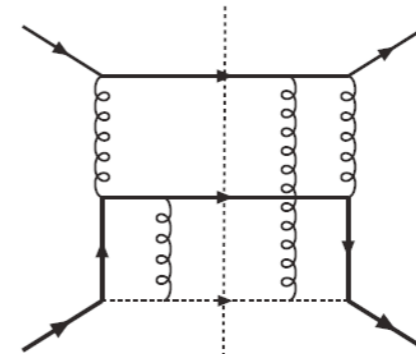
Vogelsang, Yuan, 0708.4398 [hep-ph]



(a)

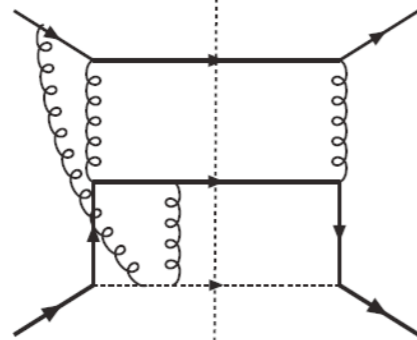


(b)

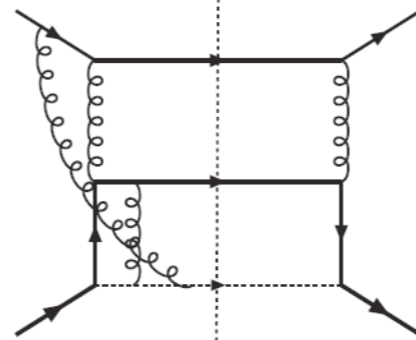


(c)

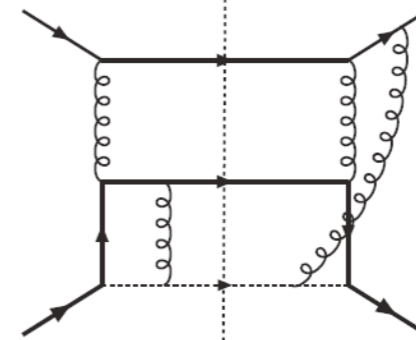
+ more



(d)



(e)



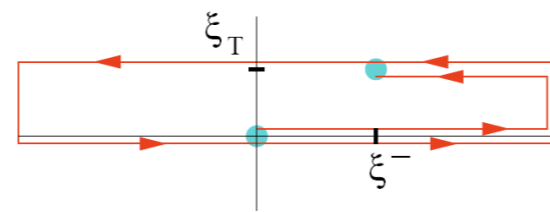
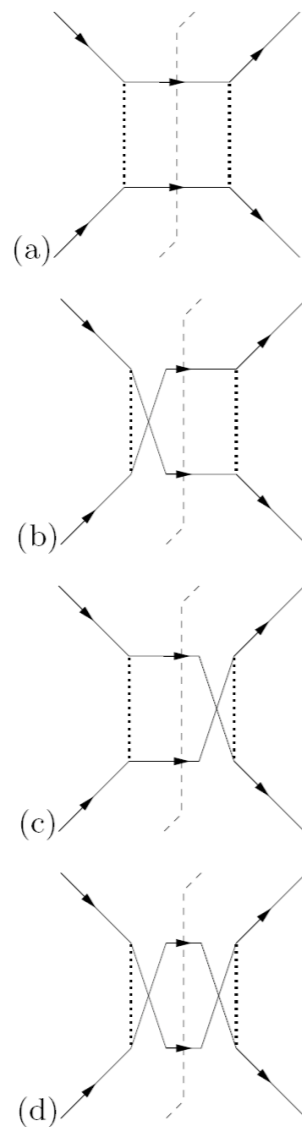
(f)

$$g_1^2 \left[\frac{1}{k_1^+ k_2^+} + (-i\pi)^2 \delta(k_1^+) \delta(k_2^+) \right] + \dots$$

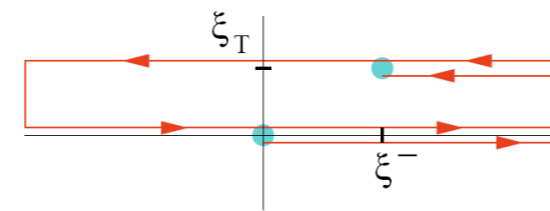
$$+ 4 (g_1 g_2 + g_2^2) (-i\pi)^2 \delta(k_1^+) \delta(k_2^+) .$$

Breaking of universality, and not only in single-spin asymmetries

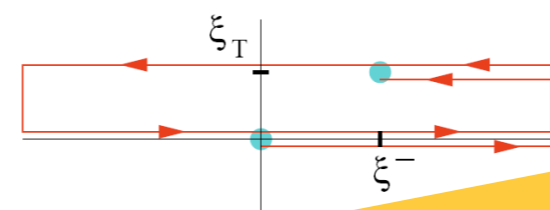
A forest of gauge links



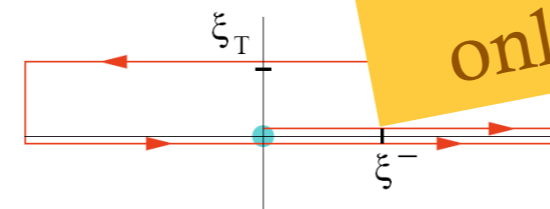
$$\text{Tr} (u_{g_1}^{[\square]}) u_{g_2}^{[+]}$$



$$u_g^{[\square]} u_g^{[+]}$$



$$u_g^{[\square]} u_g^{[+]}$$



$$\text{Tr} (u_g^{[\square]}) u_g^{[+]}$$

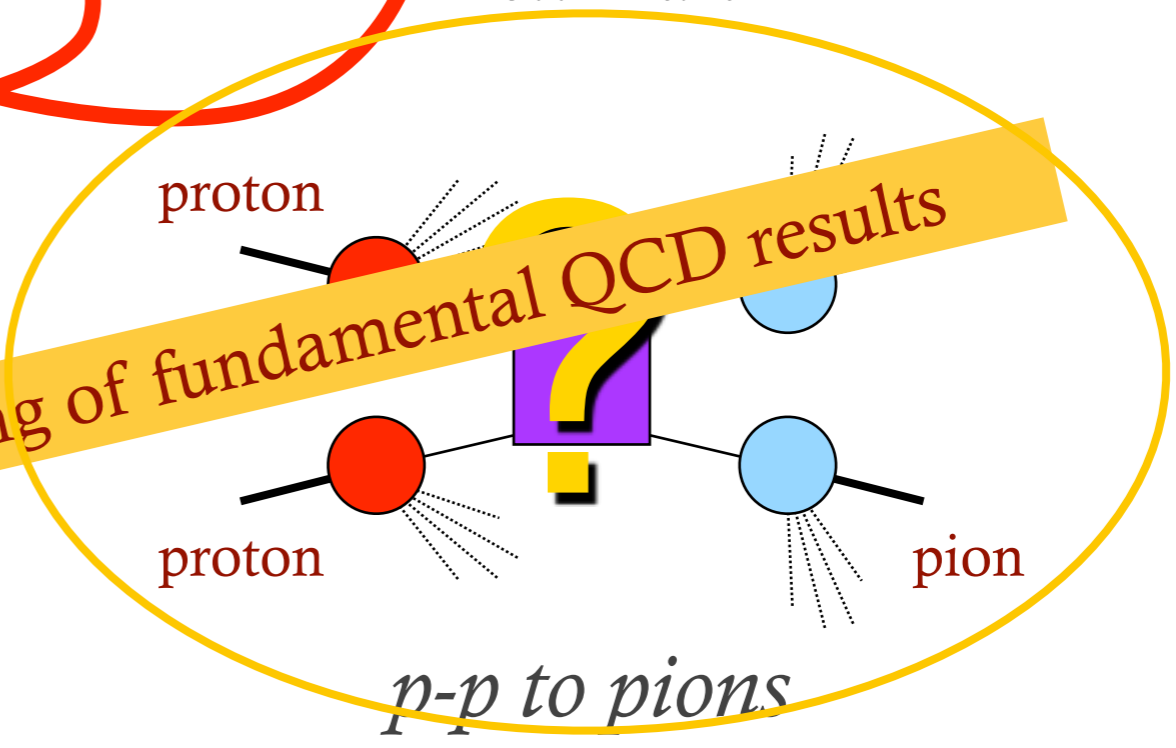
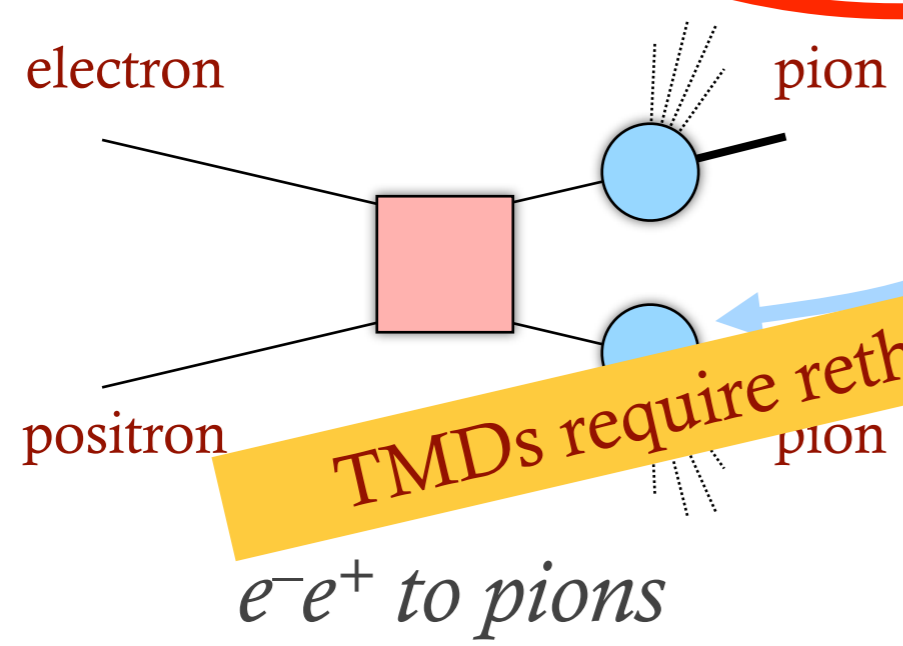
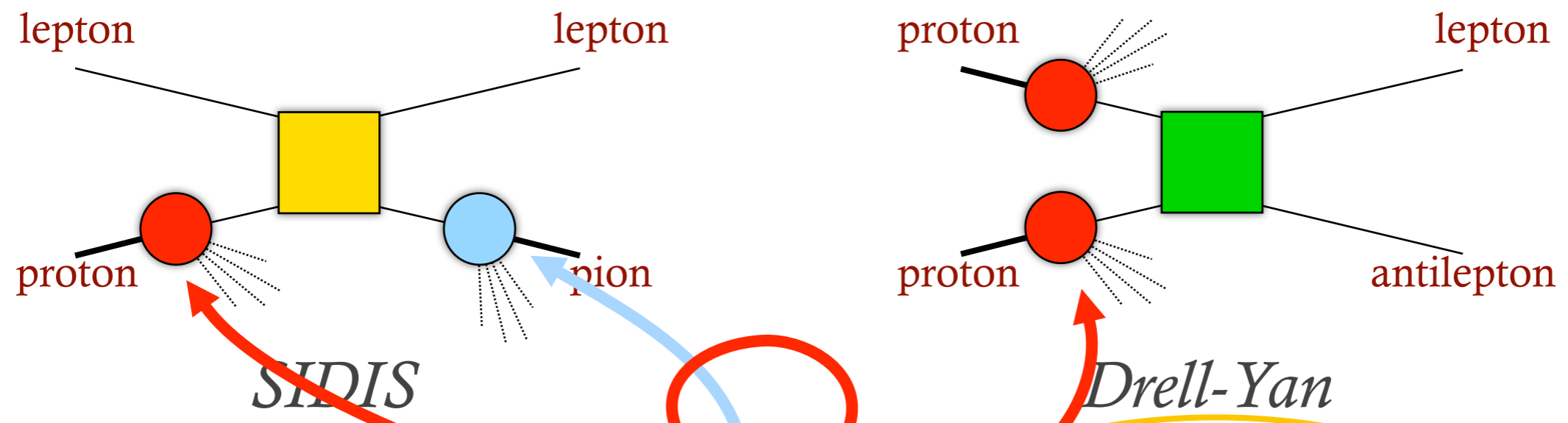
Breaking of universality, and not only in single-spin asymmetries

Bomhof, Mulders, Pijlman, PLB 596 (04)

Collins, Qiu, PRD 75 (07)

Vogelsang, Yuan, PRD76 (07)

Hadrons to hadrons



TMDs require rethinking of fundamental QCD results

Weighted asymmetries

$$\int \frac{d\sigma_{DIS}}{dq_T} dq_T = H_{DIS} \otimes f$$

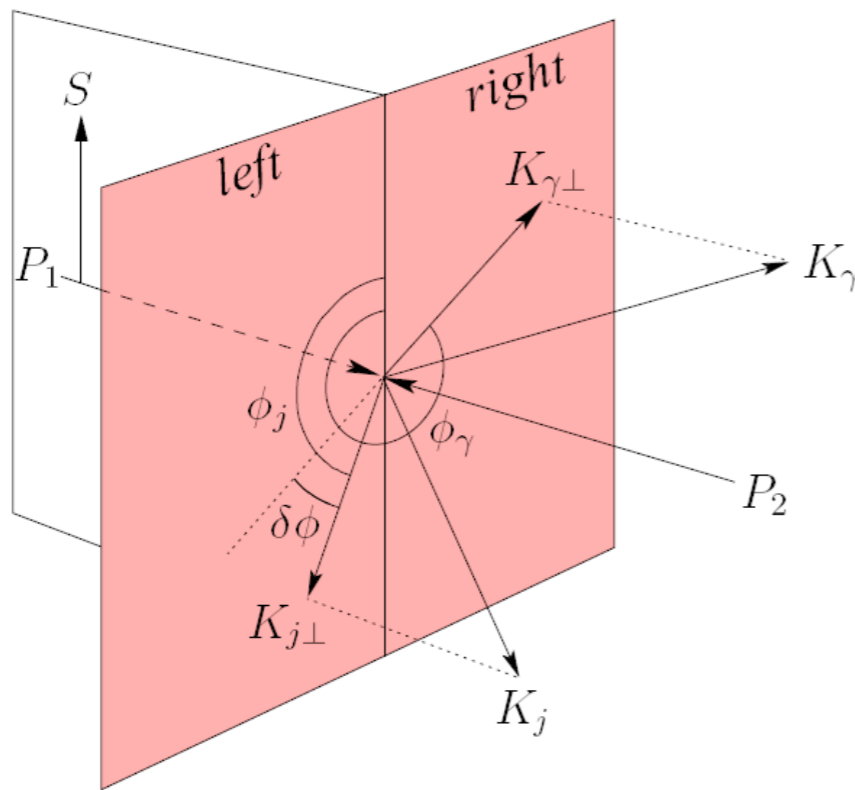
$$\int \frac{d\sigma_{pp}}{dq_T} dq_T = H_{pp} \otimes f$$

$$\int q_T \frac{d\sigma_{DIS}}{dq_T} dq_T = K_{DIS} \otimes g$$

$$\int q_T \frac{d\sigma_{pp}}{dq_T} dq_T = K_{pp} \otimes g' = C K_{pp} \otimes g$$

Weighted asymmetries

A.B., D'Alesio, Bomhof, Mulders, Murgia, PRL99 (07)



“Standard” universality

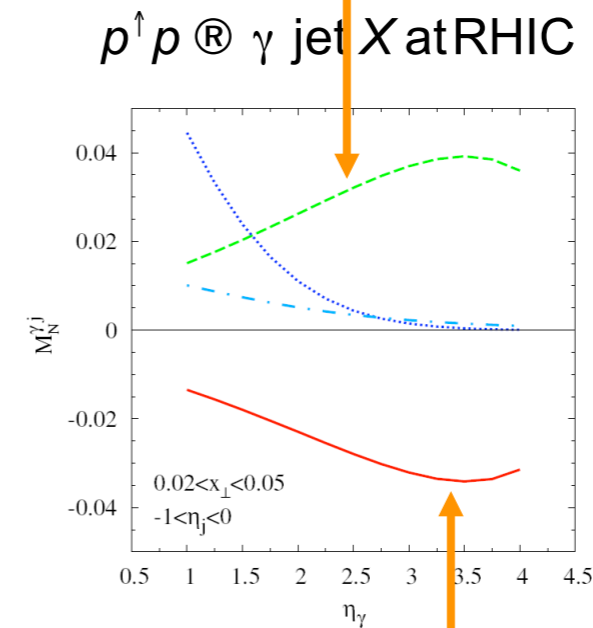


FIG. 5: Prediction for the azimuthal moment $M_N^{\gamma j}$ at $\sqrt{s} = 200$ GeV, as a function of η_γ , integrated over $-1 \leq \eta_j \leq 0$ and $0.02 \leq x_\perp \leq 0.05$. Solid line: using gluonic-pole cross sections. Dashed line: using standard partonic cross sections. Dotted line: maximum contribution from the gluon Sivers function (absolute value). Dot-dashed line: maximum contribution from the Boer-Mulders function (absolute value).

“Generalized” universality