

Part 4: Phenomenology

Unpolarized functions

Unpolarized cross section

$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2} = \frac{4\pi^2\alpha^2}{xQ^2} \frac{y}{2(1-\varepsilon)} \left(F_{UU,T}(x, z, P_{h\perp}^2, Q^2) + \varepsilon F_{UU,L}(x, z, P_{h\perp}^2, Q^2) \right),$$

Unpolarized cross section

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$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$

Unpolarized cross section

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$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$

$$\frac{y^2}{2(1-\varepsilon)} = \frac{1}{1+\gamma^2} \left(1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2 \right) \approx \left(1 - y + \frac{1}{2}y^2 \right),$$

$$\frac{y^2}{2(1-\varepsilon)} \varepsilon = \frac{1}{1+\gamma^2} \left(1 - y - \frac{1}{4}\gamma^2 y^2 \right) \approx (1 - y)$$

Convolution

$$F_{UU,T} = \mathcal{C}[f_1 D_1]$$

$$\mathcal{C}[w f D] = \sum_a x e_a^2 \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_h / z) w(\mathbf{p}_T, \mathbf{k}_T) f^a(x, p_T^2) D^a(z, k_T^2),$$

Convolution

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$$f \otimes D = x_B \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h\perp} / z) f^a(x_B, p_T^2) D^a(z, k_T^2)$$

Convolution

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$$\mathcal{C}[w f D] = \sum_a x e_a^2 \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_h / z) w(\mathbf{p}_T, \mathbf{k}_T) f^a(x, p_T^2) D^a(z, k_T^2),$$

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$$F_{UU,T} = \sum_a e_a^2 f_1^a \otimes D_1^a, \quad F_{UU,L} = \mathcal{O}\left(\frac{M^2}{Q^2}, \frac{P_{h\perp}^2}{Q^2}\right)$$

Integrated

$$\begin{aligned} x_B \int d^2 P_{h\perp} \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T & \stackrel{(2)}{=} (\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h\perp}/z) f_1^a(x_B, p_T^2) D_1^a(z, k_T^2) \\ & = x_B \int d^2 \mathbf{p}_T f_1^a(x_B, p_T^2) \int z^2 d^2 \mathbf{k}_T D_1^a(z, k_T^2) \\ & = f_1^a(x_B) D_1^a(z) \end{aligned}$$

Integrated

$$\begin{aligned} x_B \int d^2 P_{h\perp} \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T & {}^{(2)} (\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h\perp}/z) f_1^a(x_B, p_T^2) D_1^a(z, k_T^2) \\ & = x_B \int d^2 \mathbf{p}_T f_1^a(x_B, p_T^2) \int z^2 d^2 \mathbf{k}_T D_1^a(z, k_T^2) \\ & = f_1^a(x_B) D_1^a(z) \end{aligned}$$

$$F_{UU,T} = \sum_a e_a^2 f_1^a(x_B) D_1^a(z),$$

$$F_{UU,L} = \mathcal{O}(\alpha_s)$$

Fragmentation functions

For the "favored" functions

$$D_1^{u \rightarrow \pi^+} = D_1^{\bar{d} \rightarrow \pi^+} = D_1^{d \rightarrow \pi^-} = D_1^{\bar{u} \rightarrow \pi^-}, \equiv D_1^f$$

$$D_1^{u \rightarrow K^+} = D_1^{\bar{u} \rightarrow K^-}, \equiv D_1^{\text{fd}}$$

$$D_1^{\bar{s} \rightarrow K^+} = D_1^{s \rightarrow K^-} \equiv D_1^{f'}$$

for the "unfavored" functions

$$D_1^{\bar{u} \rightarrow \pi^+} = D_1^{d \rightarrow \pi^+} = D_1^{\bar{d} \rightarrow \pi^-} = D_1^{u \rightarrow \pi^-} \equiv D_1^{\text{d}},$$

$$D_1^{s \rightarrow \pi^+} = D_1^{\bar{s} \rightarrow \pi^+} = D_1^{s \rightarrow \pi^-} = D_1^{\bar{s} \rightarrow \pi^-} \equiv D_1^{\text{df}},$$

$$D_1^{\bar{u} \rightarrow K^+} = D_1^{\bar{d} \rightarrow K^+} = D_1^{d \rightarrow K^+} = D_1^{\bar{d} \rightarrow K^-} = D_1^{d \rightarrow K^-} = D_1^{u \rightarrow K^-} \equiv D_1^{\text{dd}},$$

$$D_1^{s \rightarrow K^+} = D_1^{\bar{s} \rightarrow K^-} \equiv D_1^{\text{d}'}$$

Various combinations

$$F_{UU,T}^{p/\pi^+}(x, z, P_{h\perp}^2) = \left(4 f_1^u + f_1^{\bar{d}}\right) \otimes D_1^f + \left(4 f_1^{\bar{u}} + f_1^d\right) \otimes D_1^d + \left(f_1^s + f_1^{\bar{s}}\right) \otimes D_1^{\text{df}},$$

$$F_{UU,T}^{p/\pi^-}(x, z, P_{h\perp}^2) = \left(4 f_1^{\bar{u}} + f_1^d\right) \otimes D_1^f + \left(4 f_1^u + f_1^{\bar{d}}\right) \otimes D_1^d + \left(f_1^s + f_1^{\bar{s}}\right) \otimes D_1^{\text{df}},$$

$$F_{UU,T}^{n/\pi^+}(x, z, P_{h\perp}^2) = \left(4 f_1^d + f_1^{\bar{u}}\right) \otimes D_1^f + \left(4 f_1^{\bar{d}} + f_1^u\right) \otimes D_1^d + \left(f_1^s + f_1^{\bar{s}}\right) \otimes D_1^{\text{df}}$$

$$F_{UU,T}^{n/\pi^-}(x, z, P_{h\perp}^2) = \left(4 f_1^{\bar{d}} + f_1^u\right) \otimes D_1^f + \left(4 f_1^d + f_1^{\bar{u}}\right) \otimes D_1^d + \left(f_1^s + f_1^{\bar{s}}\right) \otimes D_1^{\text{df}},$$

$$F_{UU,T}^{p/K^+}(x, z, P_{h\perp}^2) = 4 f_1^u \otimes D_1^{\text{fd}} + \left(4 f_1^{\bar{u}} + f_1^d + f_1^{\bar{d}}\right) \otimes D_1^{\text{dd}} + f_1^{\bar{s}} \otimes D_1^{\text{f}'} + f_1^s \otimes D_1^{\text{d}'},$$

$$F_{UU,T}^{p/K^-}(x, z, P_{h\perp}^2) = 4 f_1^{\bar{u}} \otimes D_1^{\text{fd}} + \left(4 f_1^u + f_1^d + f_1^{\bar{d}}\right) \otimes D_1^{\text{dd}} + f_1^s \otimes D_1^{\text{f}'} + f_1^{\bar{s}} \otimes D_1^{\text{d}'},$$

$$F_{UU,T}^{n/K^+}(x, z, P_{h\perp}^2) = 4 f_1^d \otimes D_1^{\text{fd}} + \left(4 f_1^{\bar{d}} + f_1^u + f_1^{\bar{u}}\right) \otimes D_1^{\text{dd}} + f_1^{\bar{s}} \otimes D_1^{\text{f}'} + f_1^s \otimes D_1^{\text{d}'},$$

$$F_{UU,T}^{n/K^-}(x, z, P_{h\perp}^2) = 4 f_1^{\bar{d}} \otimes D_1^{\text{fd}} + \left(4 f_1^d + f_1^u + f_1^{\bar{u}}\right) \otimes D_1^{\text{dd}} + f_1^s \otimes D_1^{\text{f}'} + f_1^{\bar{s}} \otimes D_1^{\text{d}'}$$

Valence and pions only

$$F_{UU,T}^{p/\pi^+}(x, z, P_{h\perp}^2) = 4 f_1^u \otimes D_1^f + f_1^d \otimes D_1^d,$$

$$F_{UU,T}^{p/\pi^-}(x, z, P_{h\perp}^2) = f_1^d \otimes D_1^f + 4 f_1^u \otimes D_1^d,$$

$$F_{UU,T}^{n/\pi^+}(x, z, P_{h\perp}^2) = 4 f_1^d \otimes D_1^f + f_1^u \otimes D_1^d,$$

$$F_{UU,T}^{n/\pi^-}(x, z, P_{h\perp}^2) = f_1^u \otimes D_1^f + 4 f_1^d \otimes D_1^d$$

Gaussian ansatz

$$f_1^a(x, p_T^2) = \frac{f_1^a(x)}{\pi \rho_a^2} e^{-\mathbf{p}_T^2 / \rho_a^2},$$

$$D_1^a(z, k_T^2) = \frac{D_1^a(z)}{\pi \sigma_a^2} e^{-z^2 \mathbf{k}_T^2 / \sigma_a^2}$$

Gaussian ansatz

$$f_1^a(x, p_T^2) = \frac{f_1^a(x)}{\pi \rho_a^2} e^{-\mathbf{p}_T^2 / \rho_a^2}, \quad D_1^a(z, k_T^2) = \frac{D_1^a(z)}{\pi \sigma_a^2} e^{-z^2 \mathbf{k}_T^2 / \sigma_a^2}$$

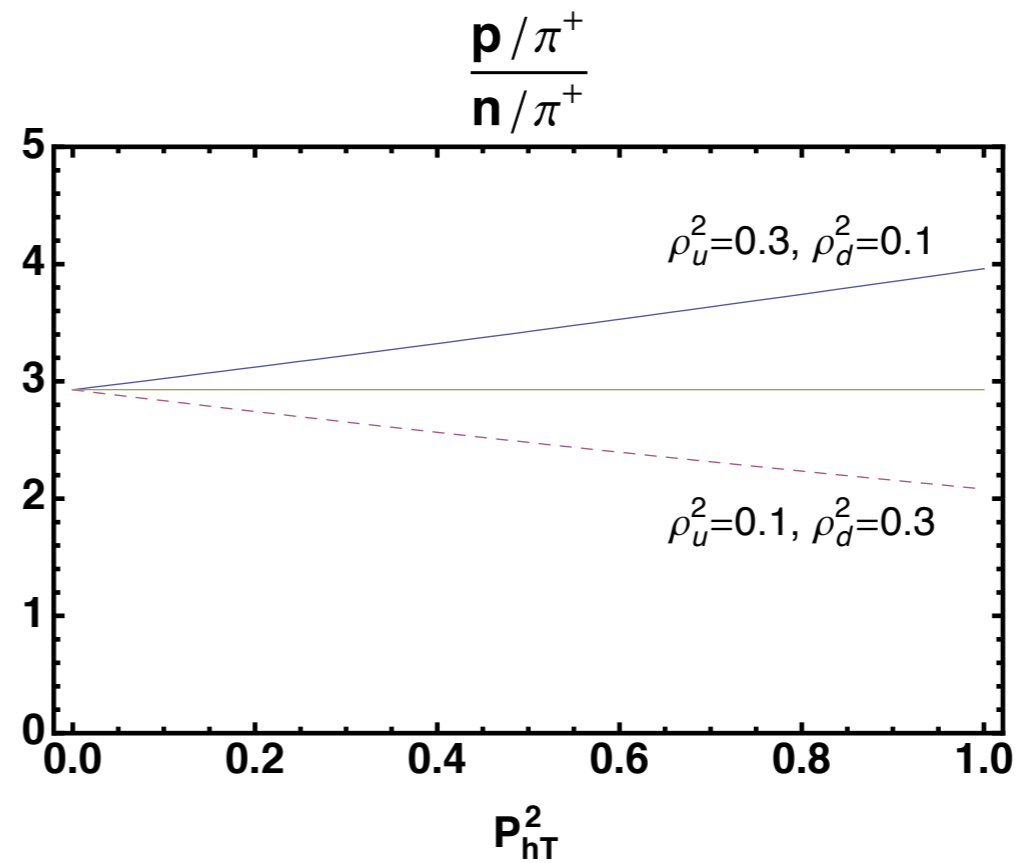
$$f_1^a \otimes D_1^a = \frac{1}{\pi(z^2 \rho_a^2 + \sigma_a^2)} e^{-\mathbf{P}_{h\perp}^2 / (z^2 \rho_a^2 + \sigma_a^2)}$$

Interesting ratio

$$\sigma_f^2 = \sigma_d^2 = 0.3 \text{ GeV}^2$$

$$f_1^u / f_1^d \approx 0.25$$

$$D_1^f / D_1^f \approx 0.40$$



Experimental access

Drell-Yan

$$\frac{d\sigma}{dq_T^2} \sim \sum_q e_q^2 f_1^q(x, p_T^2) \otimes f_1^{\bar{q}}(\bar{x}, \bar{p}_T^2)$$

Experimental access

Drell-Yan

$$\frac{d\sigma}{dq_T^2} \sim \sum_q e_q^2 f_1^q(x, p_T^2) \otimes f_1^{\bar{q}}(\bar{x}, \bar{p}_T^2)$$

Semi-inclusive
DIS

$$\frac{d\sigma}{dq_T^2} \sim \sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)$$

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$$\frac{d\sigma}{dq_T^2} \sim \sum_q e_q^2 f_1^q(x, p_T^2) \otimes f_1^{\bar{q}}(\bar{x}, \bar{p}_T^2)$$

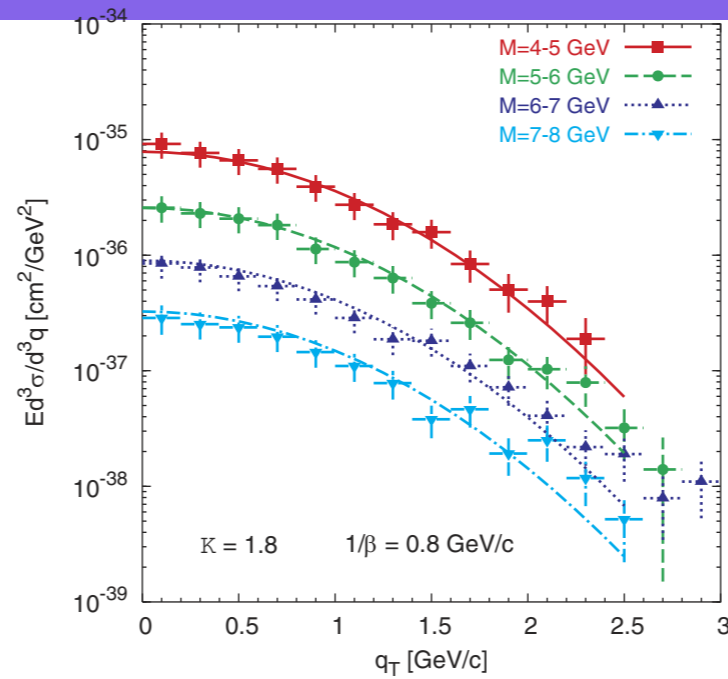
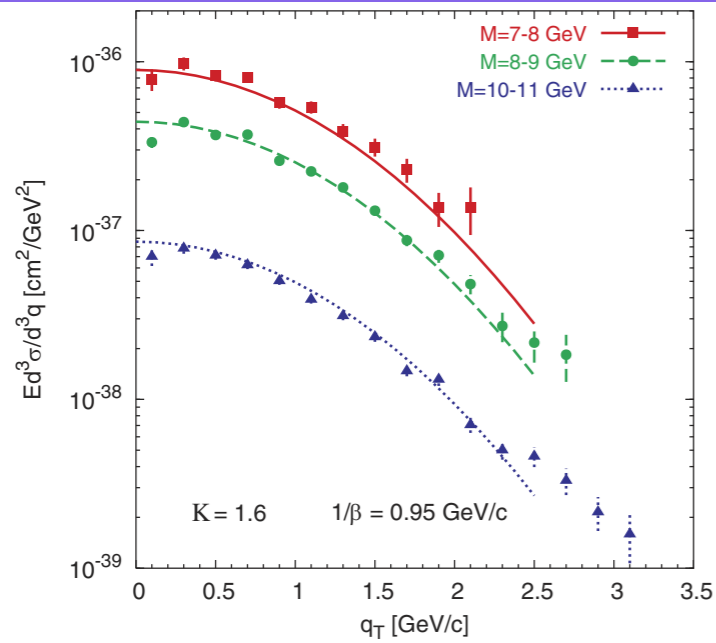
Semi-inclusive
DIS

$$\frac{d\sigma}{dq_T^2} \sim \sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)$$

electron-positron
annihilation

$$\frac{d\sigma}{dq_T^2} \sim \sum_q e_q^2 D_1^q(z, k_T^2) \otimes D_1^{\bar{q}}(\bar{z}, \bar{k}_T^2)$$

Available studies



Gaussians

D'Alesio, Murgia, PRD70 (04)

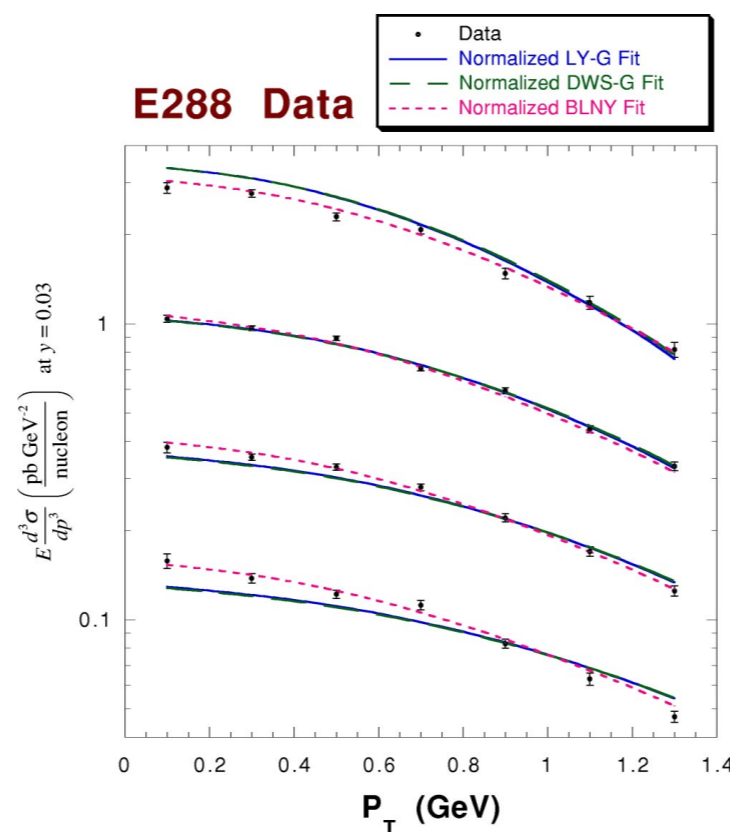
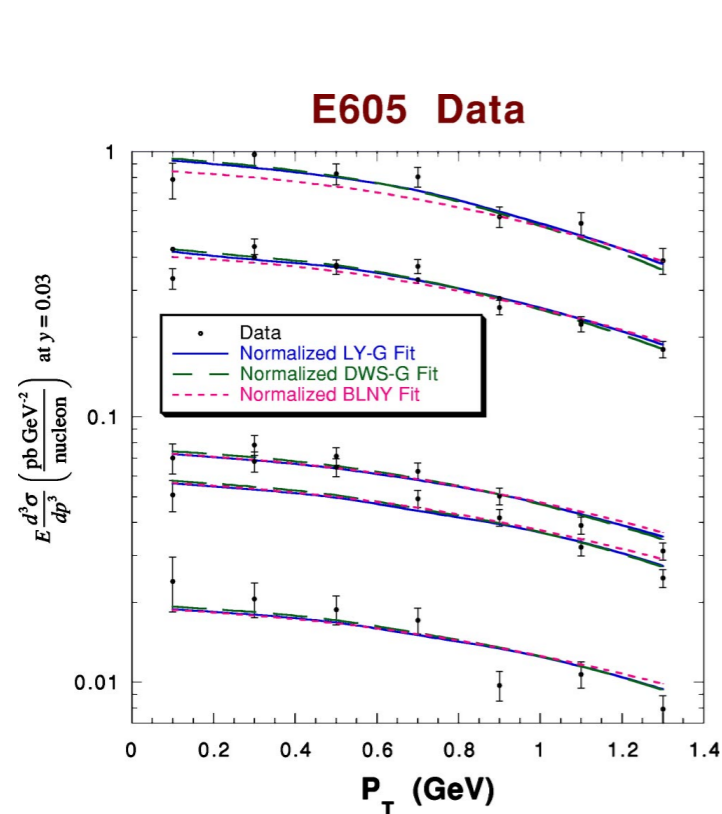
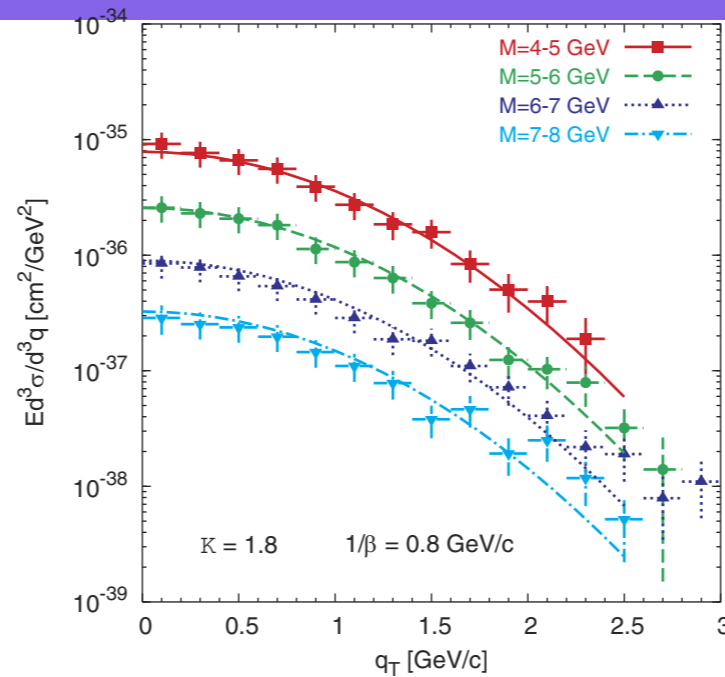
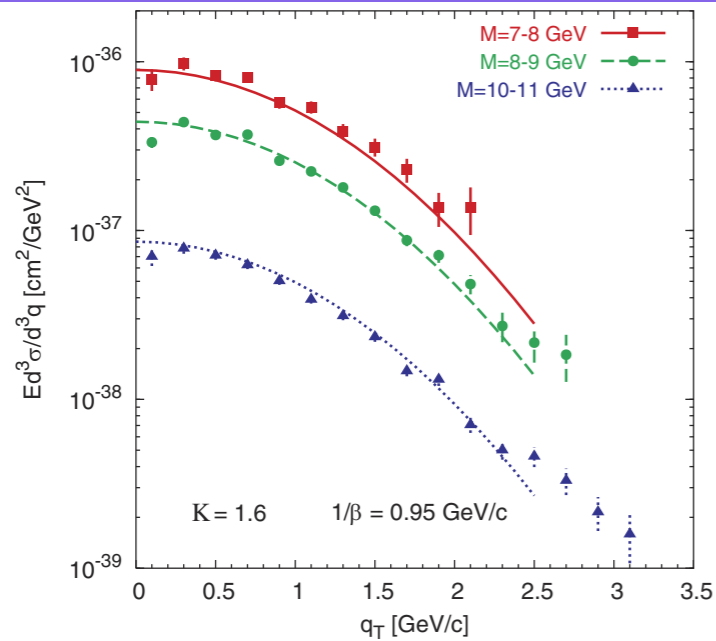
Available studies

Gaussians

D'Alesio, Murgia, PRD70 (04)

Gaussians
+ kT resummation

Landry, Brock, Nadolsky, Yuan, PRD67 (03)



Nonperturbative part

- In b space

$$\exp \left[-g_2 b^2 \ln \left(\frac{Q}{2Q_0} \right) - g_1 b^2 + g_1 g_3 b^2 \ln(100x_A x_B) \right]$$

$$g_1 = 0.21 \pm 0.01 \text{ GeV}^2,$$

$$g_2 = 0.68 \pm 0.02 \text{ GeV}^2,$$

$$g_3 = -0.60^{+0.05}_{-0.04} \text{ GeV}^2.$$

$$Q_0 = 1.6 \text{ GeV}.$$

111 data points
(Drell-Yan)

Brock, Landry, Nadolsky, Yuan, PRD67 (03)

Transversity

Asymmetry

$$F_{UT}^{\sin(\phi_h + \phi_s)} = \mathcal{C} \left[-\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M_h} h_1 H_1^\perp \right]$$

$$F_{UT}^{\sin(\phi_h + \phi_s)} = \sum_a e_a^2 h_1 \otimes \left(-\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M_h} H_1^\perp \right)$$

Collins asymmetries

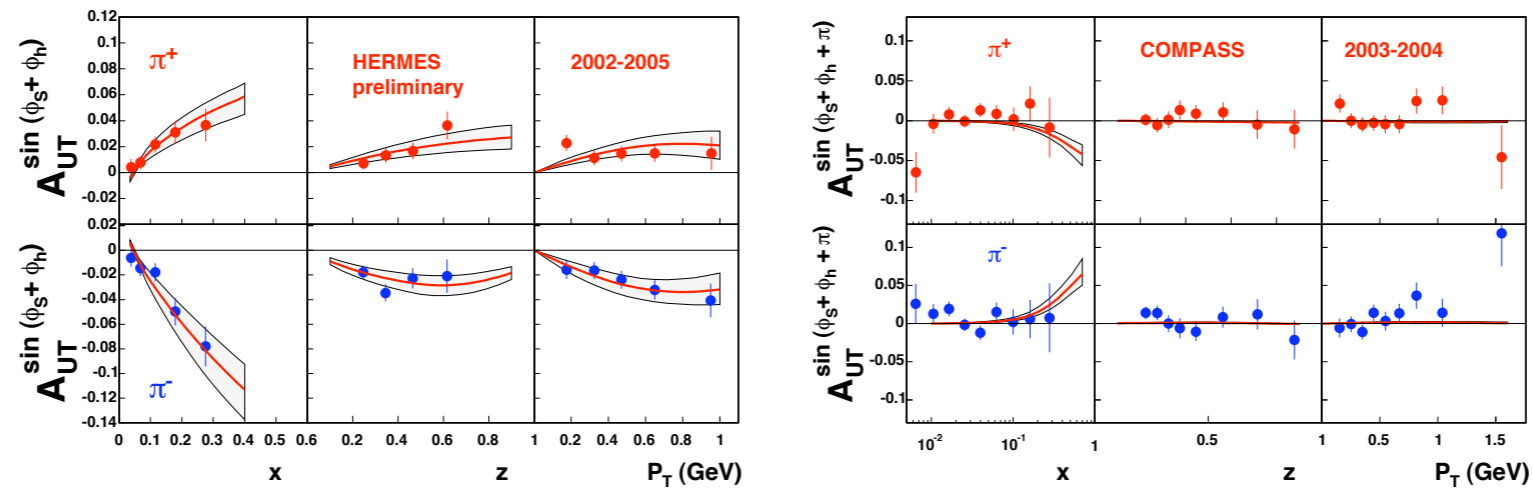


Figure 2: Fits of HERMES [4] and COMPASS [5] data. The shaded area corresponds to the uncertainty in the parameter values, see Ref. [3].

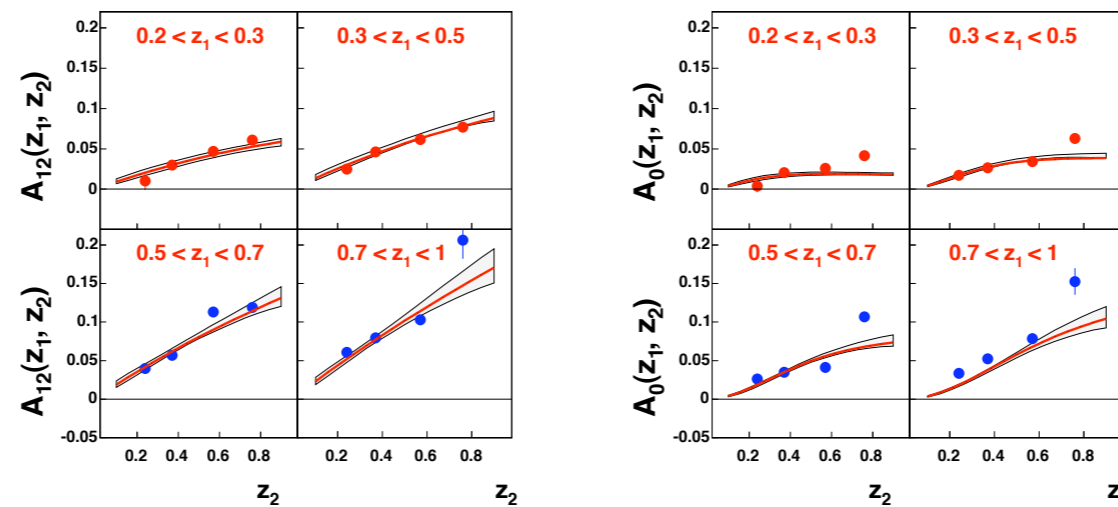


Figure 3: Left panel: fit of the BELLE [6] data on the A_{12} asymmetry ($\cos(\varphi_1 + \varphi_2)$ method). Right panel: predictions for the A_0 BELLE asymmetry ($\cos(2\varphi_0)$ method).

Transversity and Collins

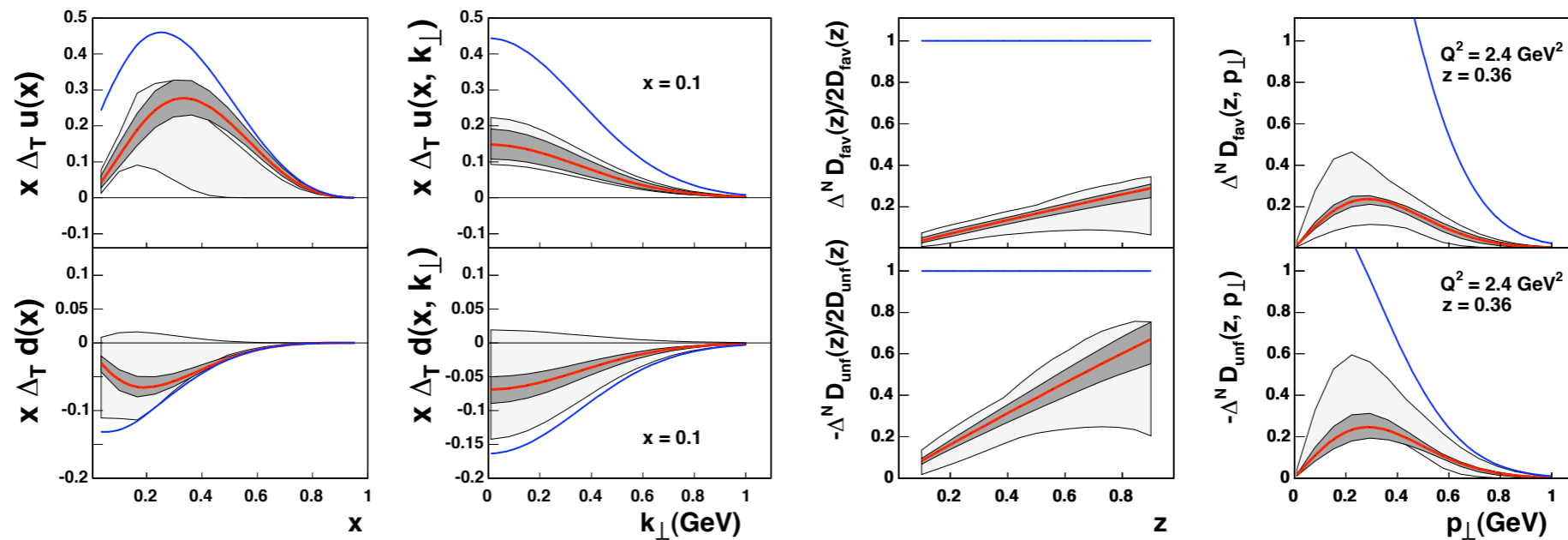
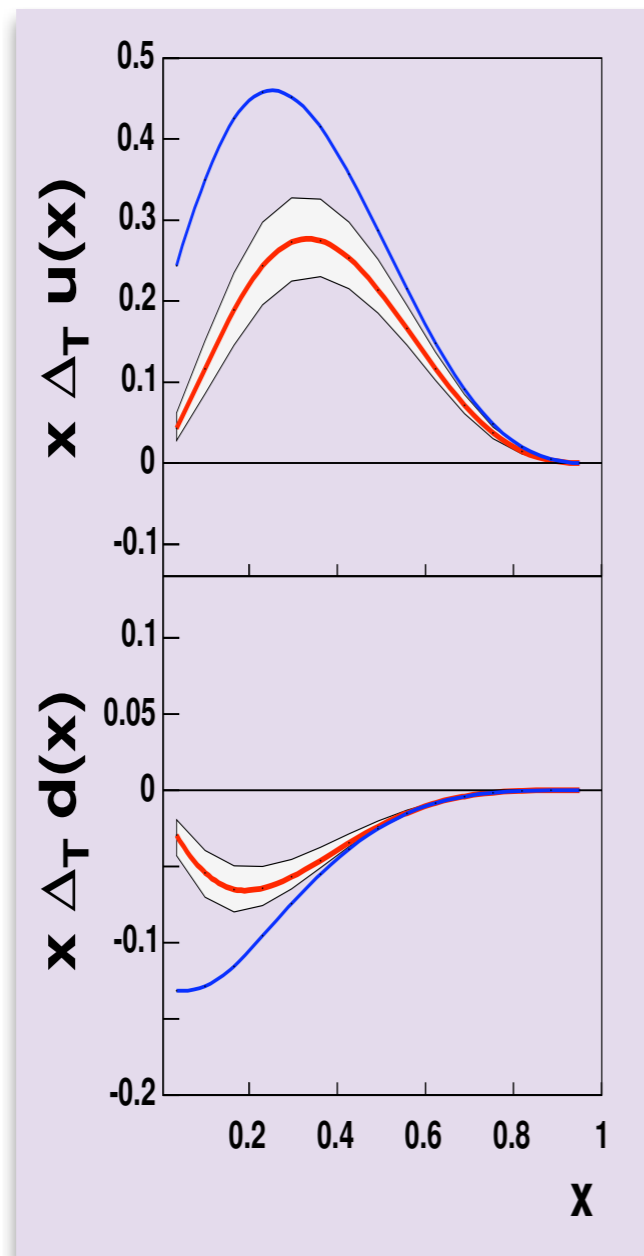


Figure 1: Left panel: the transversity distribution functions for u and d flavours as determined by our global fit; we also show the Soffer bound (highest or lowest lines) and the (wider) bands of our previous extraction [3]. Right panel: favoured and unfavoured Collins fragmentation functions as determined by our global fit; we also show the positivity bound and the (wider) bands as obtained in Ref. [3].

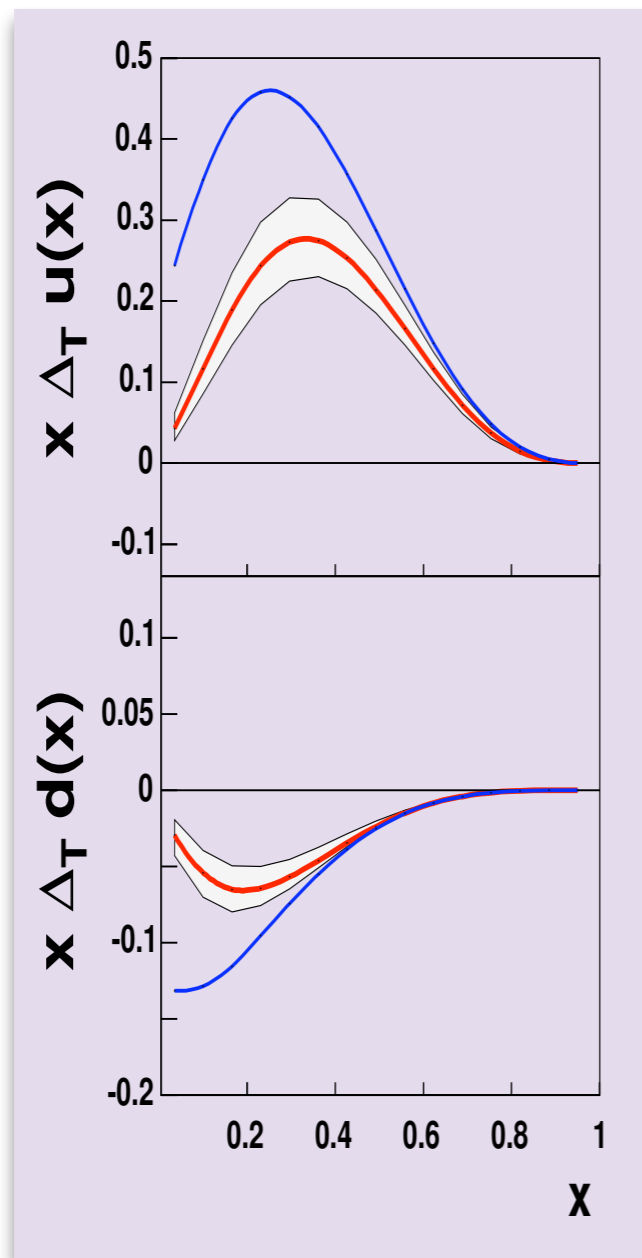
Transversity



A. Prokudin, talk at DIS08 (extraction by Anselmino et al.)

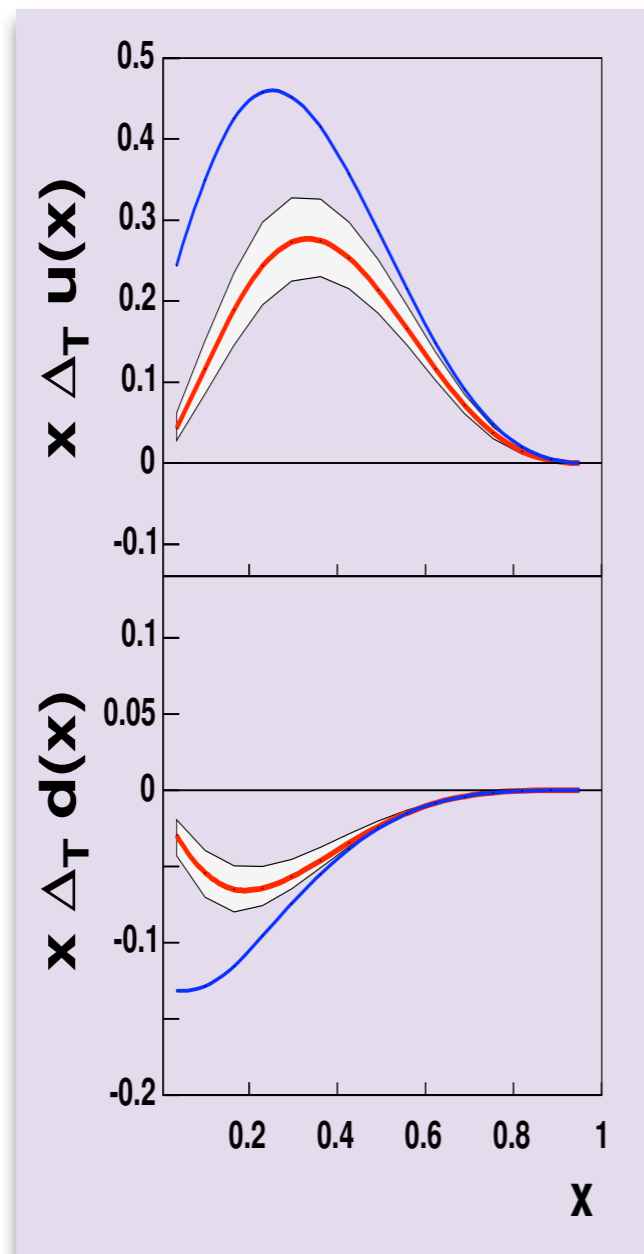
Transversity

- Data from HERMES, COMPASS, BELLE



A. Prokudin, talk at DIS08 (extraction by Anselmino et al.)

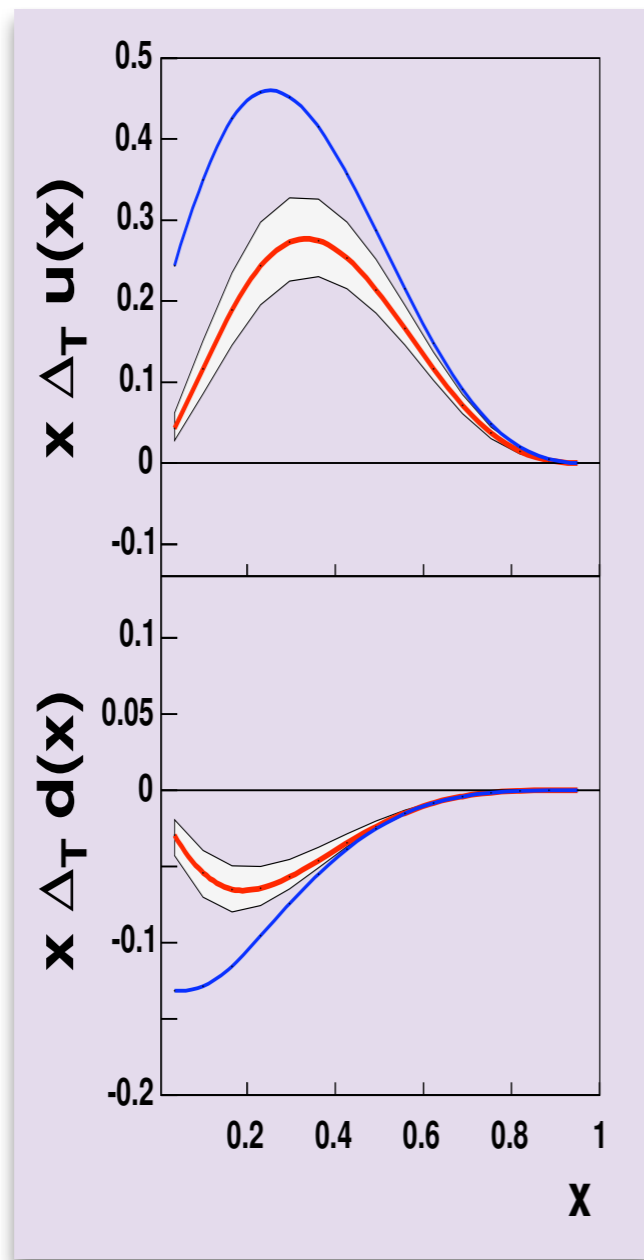
Transversity



- Data from HERMES, COMPASS, BELLE
- 96 data points (some correlations -- cf. 467 points for Δq fits)

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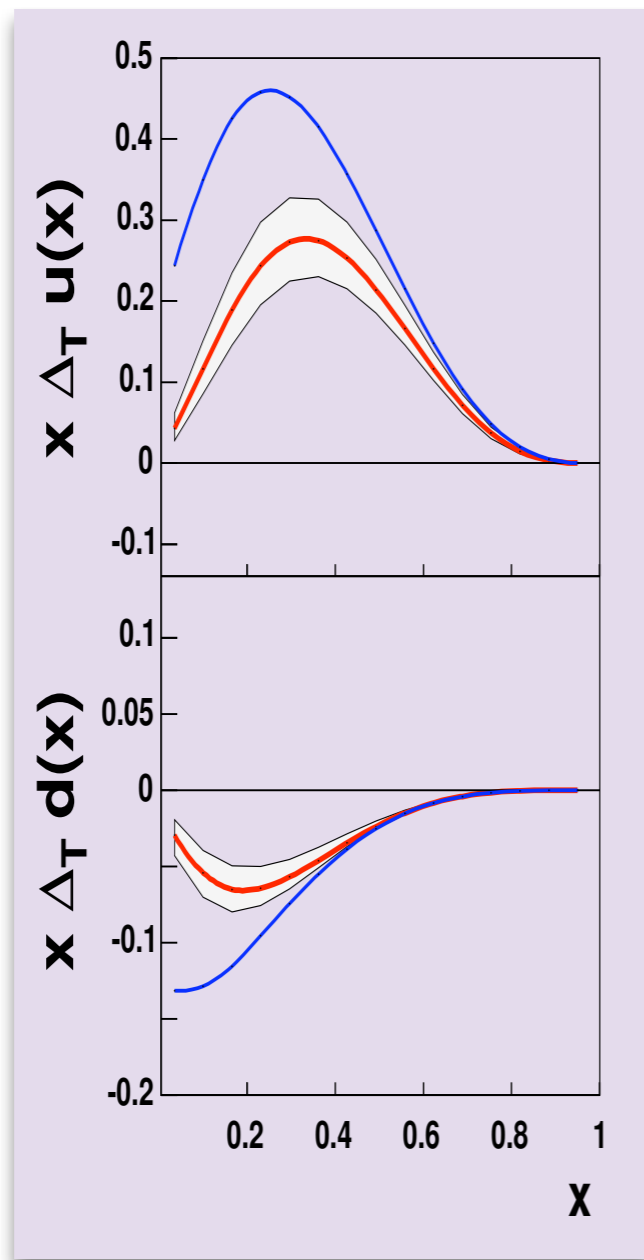
Transversity



- Data from HERMES, COMPASS, BELLE
- 96 data points (some correlations -- cf. 467 points for Δq fits)
- no sys errors taken into account

A. Prokudin, talk at DIS08 (extraction by Anselmino et al.)

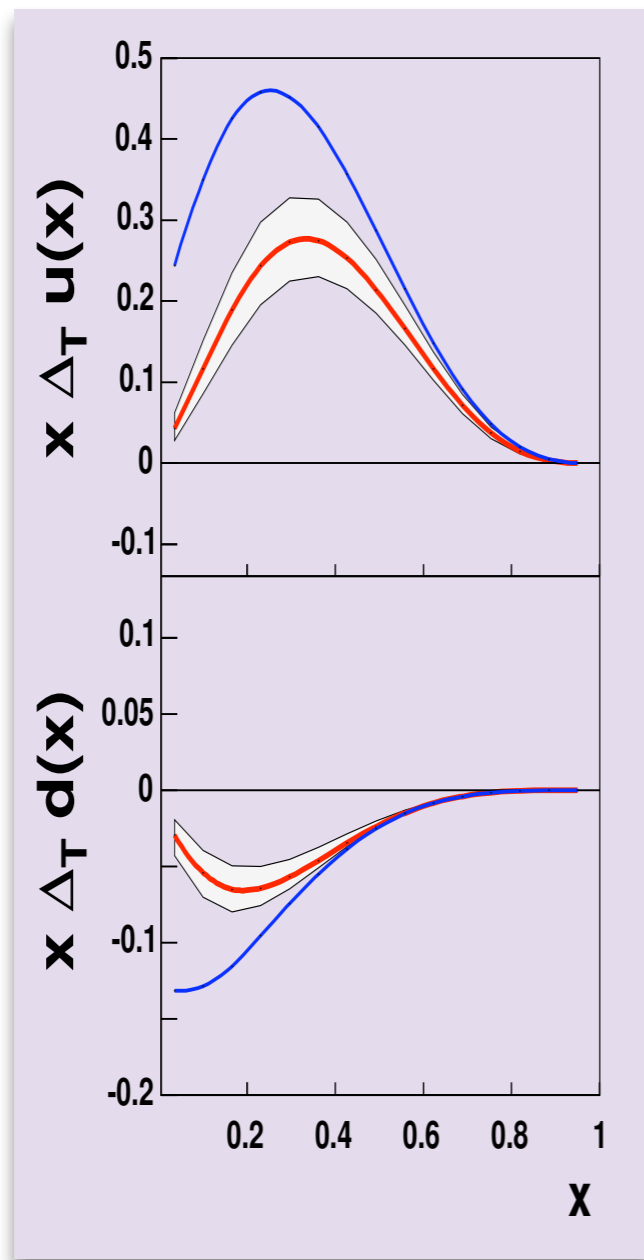
Transversity



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- $\chi^2 \approx 1.4$

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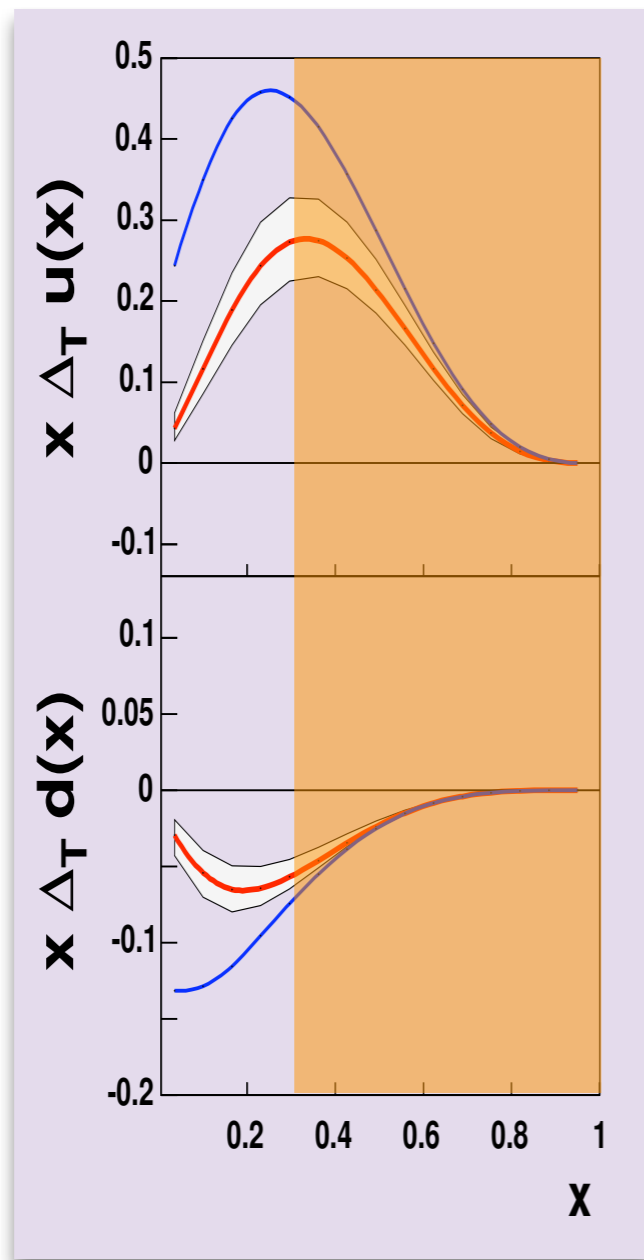
Transversity



- Data from HERMES, COMPASS, BELLE
- 96 data points (some correlations -- cf. 467 points for Δq fits)
- no sys errors taken into account
- $\chi^2 \approx 1.4$
- Statistical uncertainty only ($\Delta\chi^2 \approx 17$)

A. Prokudin, talk at DIS08 (extraction by Anselmino et al.)

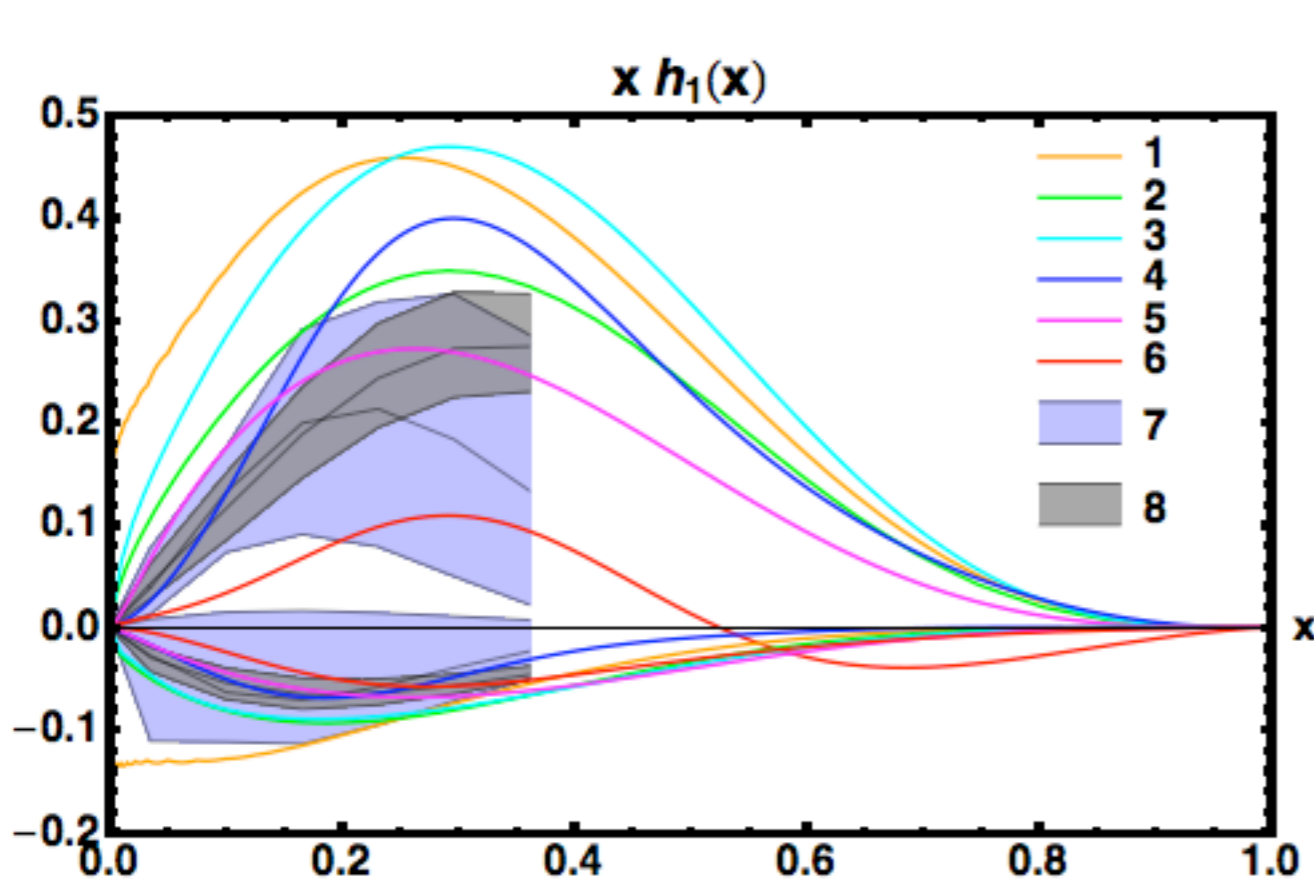
Transversity



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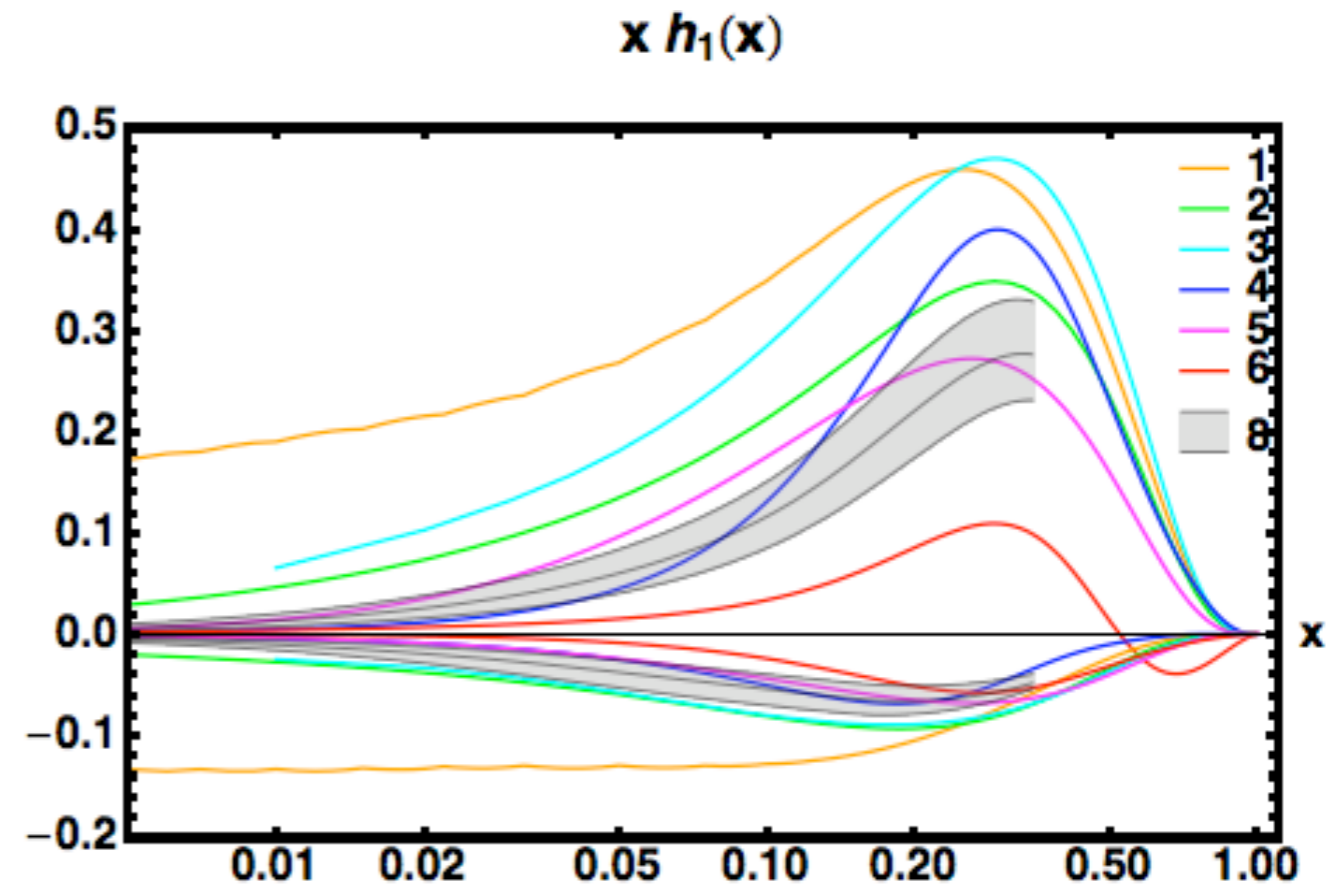
Comparison with models



[1] Soffer et al. PRD 65 (02)

[2] Korotkov et al. EPJC 18 (01)

[3] Schweitzer et al., PRD 64 (01)

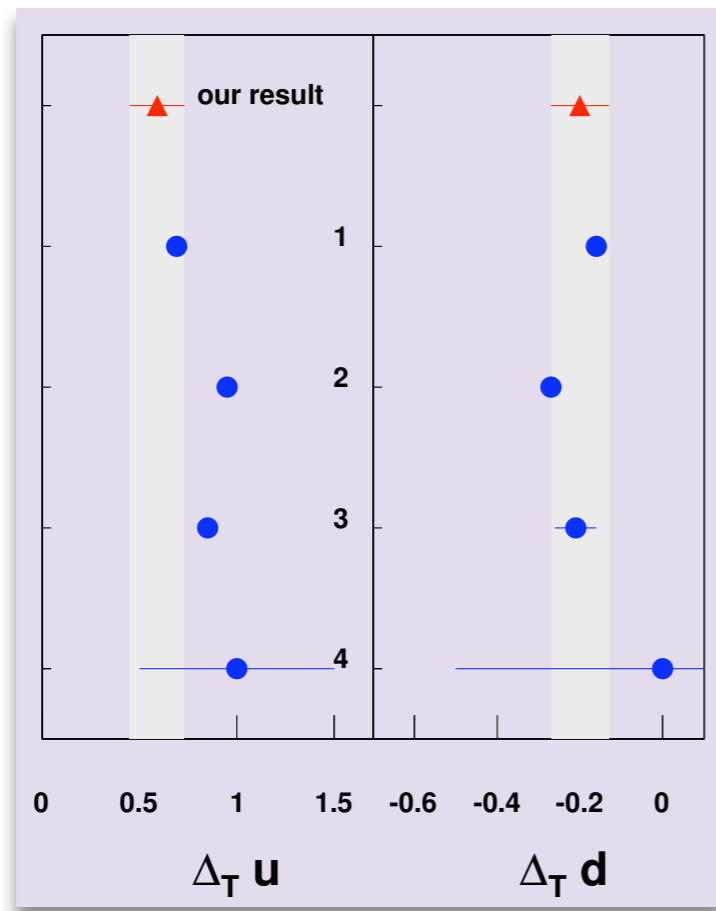


[4] Wakamatsu, PLB 509 (01)

[5] Pasquini et al., PRD 72 (05)

[6] Bacchetta, Conti, Radici, PRD 78 (08)

Tensor charge



[our result] Anselmino et al. DIS 08

*[1] Diquark spectator model,
Cloet, Bentz, Thomas, PLB 659 (08)*

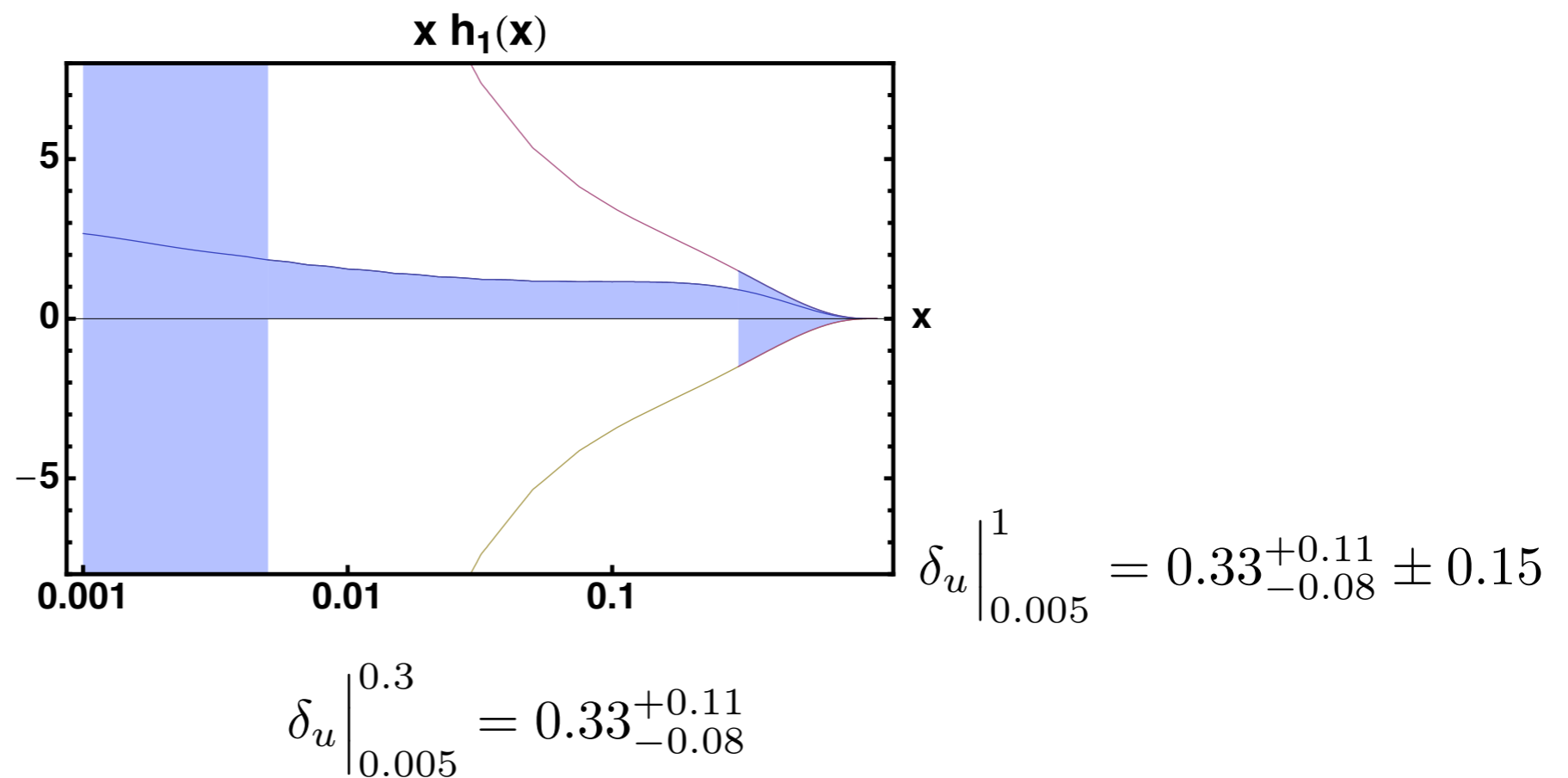
*[2] Chiral quark soliton model,
Wakamatsu, PLB 653 (07)*

*[3] Lattice QCD,
Goekeler et al. PLB 627 (05)*

*[4] QCD sum rules,
He, Ji, PRD 52 (95)*

The first x -moments of the transversity distribution – related to the tensor charge, and defined as $\Delta_T q \equiv \int_0^1 dx \Delta_T q(x)$ – are found to be $\Delta_T u = 0.59^{+0.14}_{-0.13}$, $\Delta_T d = -0.20^{+0.05}_{-0.07}$ at $Q^2 = 0.8 \text{ GeV}^2$.

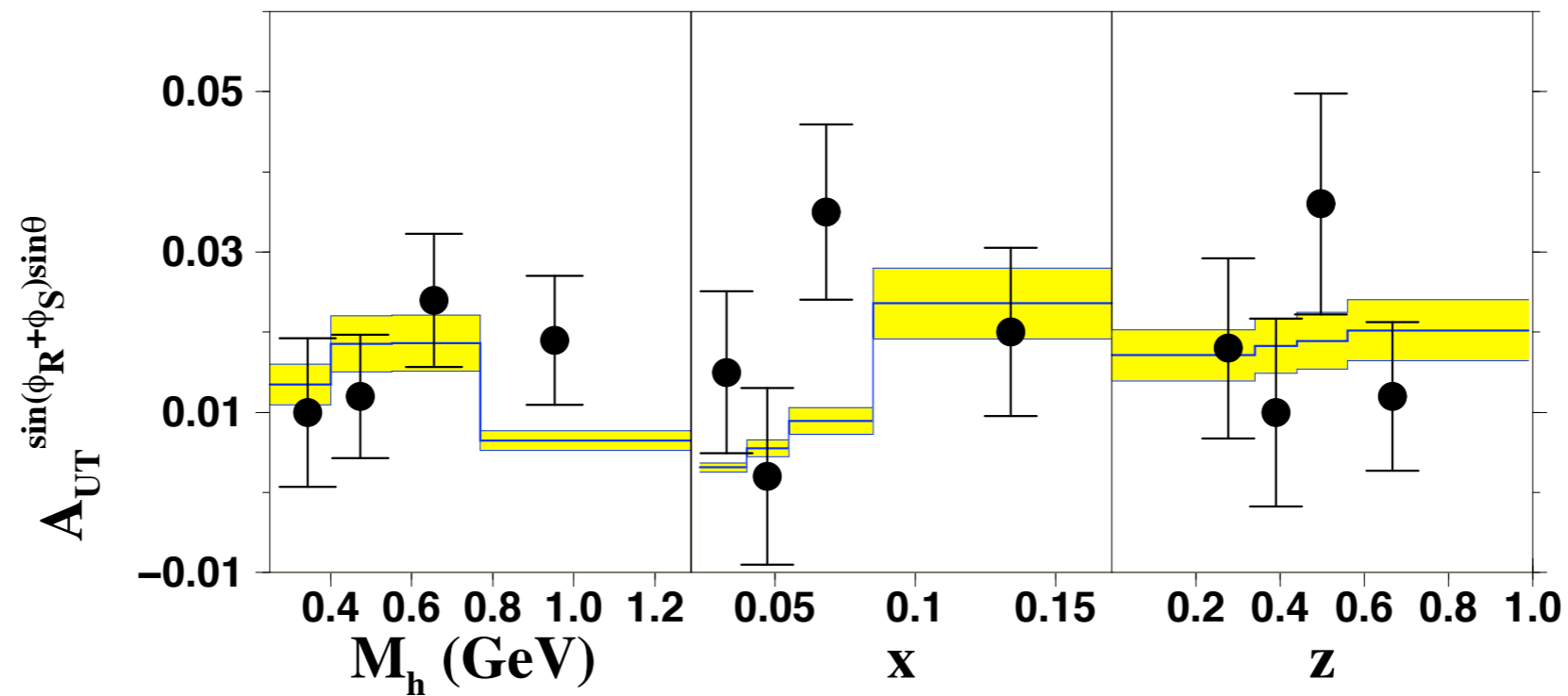
Tensor charge: extremes



$$\delta_u \Big|_{0.001}^1 = 0.33_{-0.08}^{+0.11} (\text{stat}) \pm 0.15 (\text{sys, high } x) \pm 0.14 (\text{sys, low } x)$$

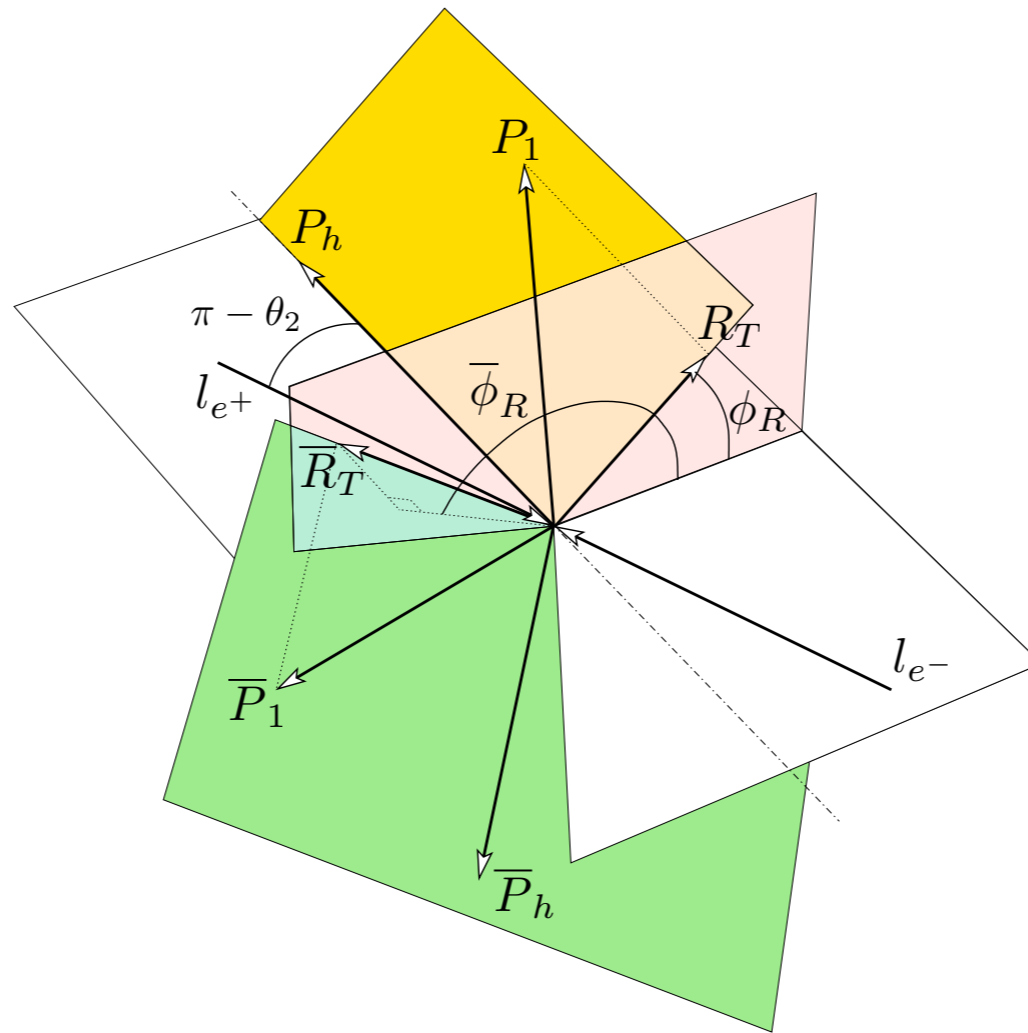
$$\delta_d \Big|_{0.001}^1 = -0.14_{-0.06}^{+0.04} (\text{stat}) \pm 0.02 (\text{sys, high } x) \pm 0.12 (\text{sys, low } x)$$

Dihadron functions: DIS

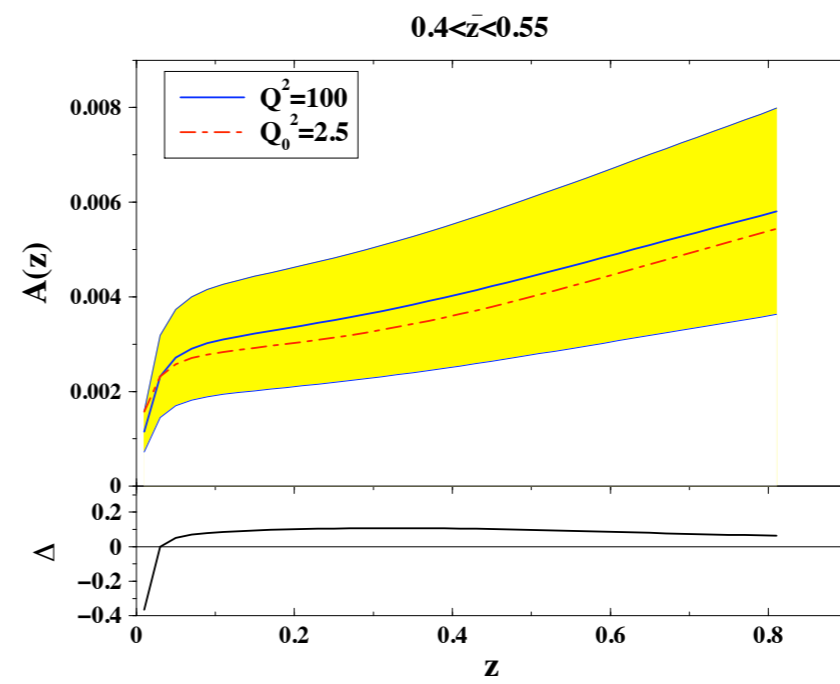
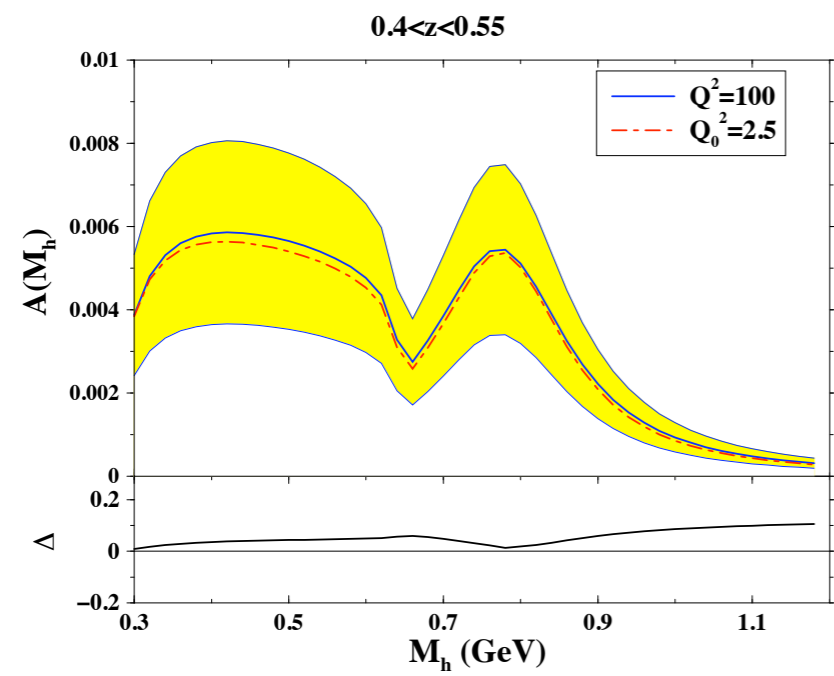


$$A_{UT}^{\sin(\phi_{R\perp} + \phi_S)\sin\theta} = -\frac{(1-y)}{(1-y + \frac{y^2}{2})} \frac{1}{2} \sqrt{1 - 4\frac{M_\pi^2}{M_{\pi\pi}^2}} \frac{\sum_q e_q^2 h_1^q(x) H_{1,q}^{\triangleleft,sp}(z, M_{\pi\pi})}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_{\pi\pi})}$$

Dihadron functions: e^+e^-



$$A(\cos \theta_2, z, M_h^2, \bar{z}, \bar{M}_h^2) = \frac{\sin^2 \theta_2}{1 + \cos^2 \theta_2} \frac{\pi^2}{32} \frac{|\mathbf{R}| |\bar{\mathbf{R}}|}{M_h \bar{M}_h} \frac{\sum_q e_q^2 H_{1,q}^{\triangleleft sp}(z, M_h^2) \bar{H}_{1,q}^{\triangleleft sp}(\bar{z}, \bar{M}_h^2)}{\sum_q e_q^2 D_{1,q}(z, M_h^2) \bar{D}_{1,q}(\bar{z}, \bar{M}_h^2)}$$

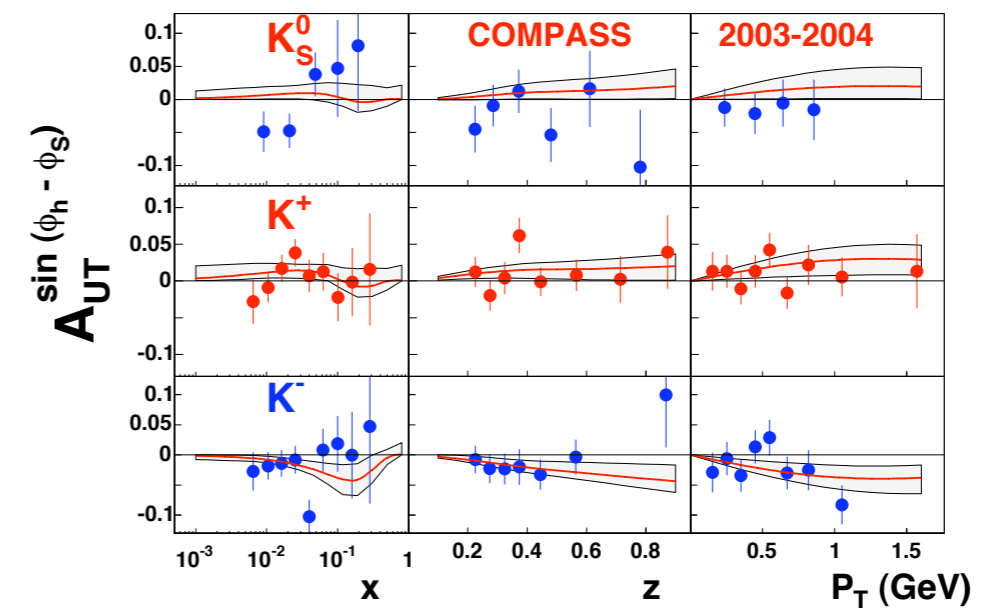
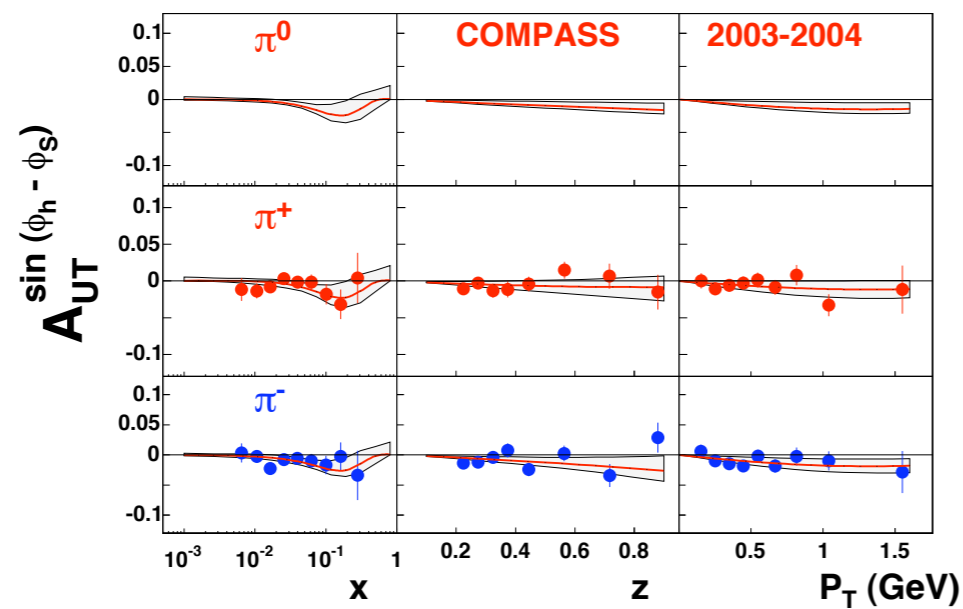
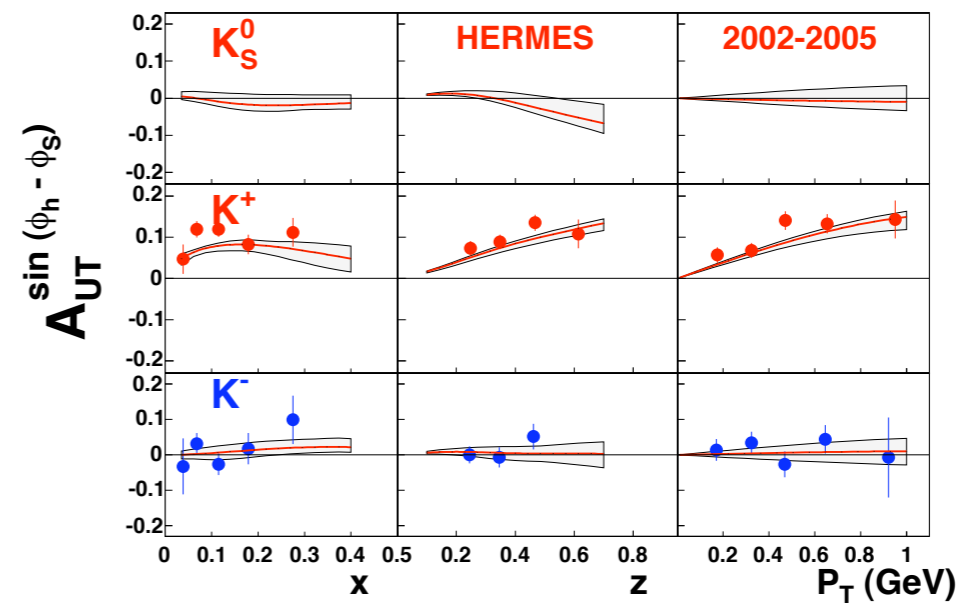
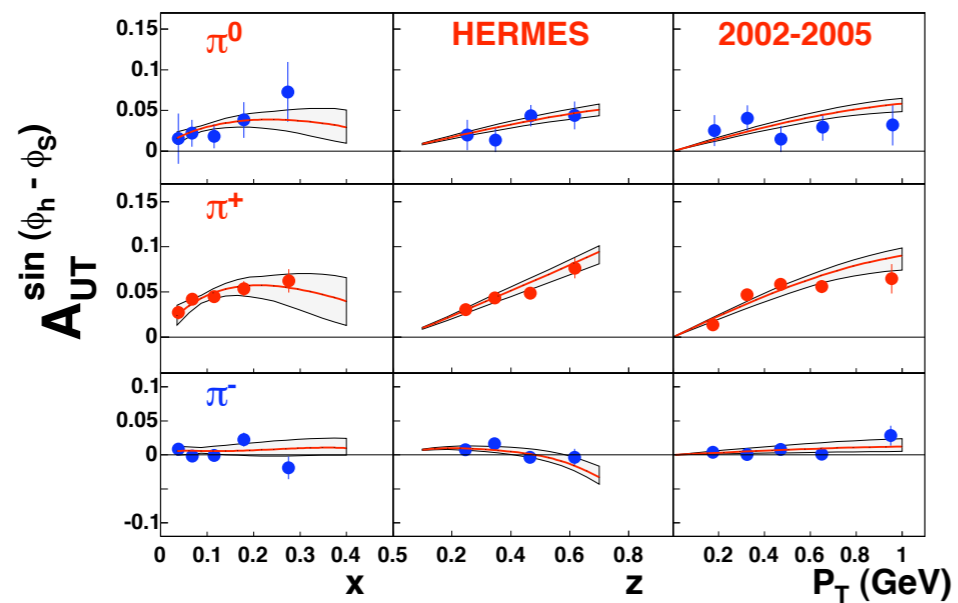


Overview of observables

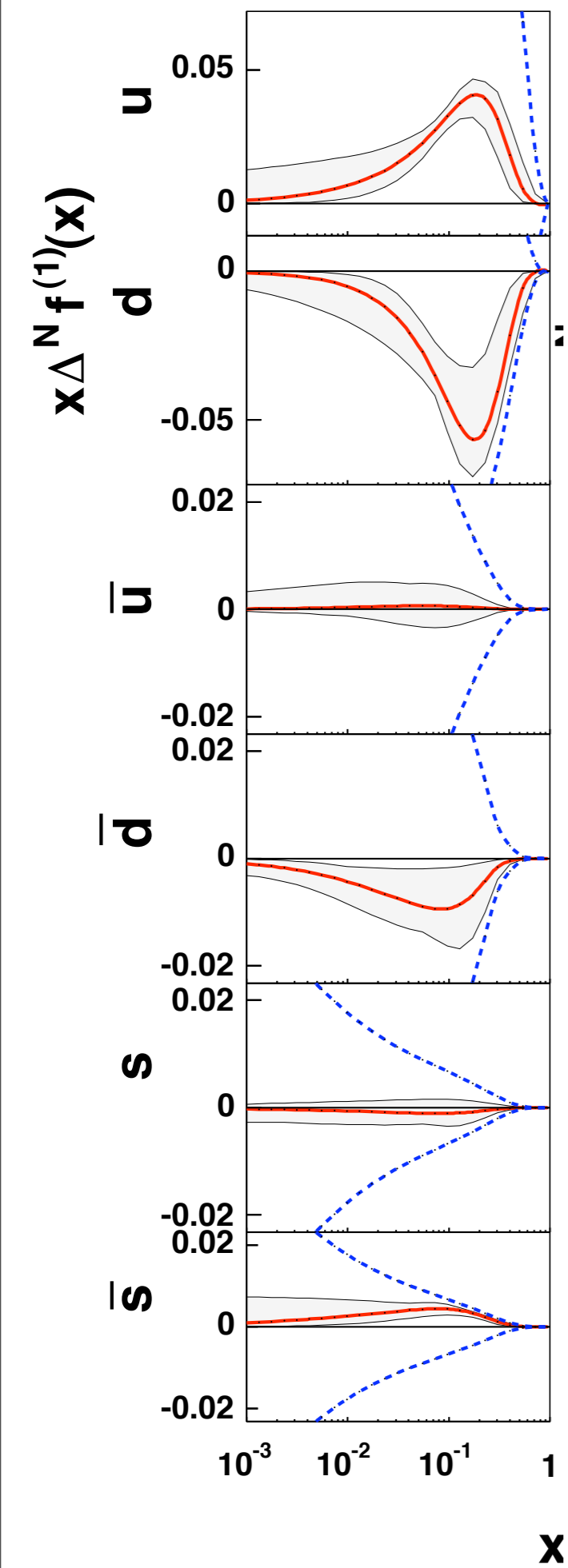
	Process	Experiment	Observable	Grade
	$I p^\uparrow \rightarrow I \pi X$	Hermes, Compass, JLab, EIC	$h_1 \otimes H_1^\perp$	★★★★
			$h_1 \tilde{H}$	★★
	$I p^\uparrow \rightarrow I(\pi\pi)X$	Hermes, Compass, JLab@12GeV, EIC	$h_1 H_1^\times$	★★★
	$I p^\uparrow \rightarrow I \Lambda X$	Hermes, Compass, JLab@12GeV, EIC	$h_1 H_1$	★
Doubly polarized	$p^\uparrow (p/\bar{p})^\uparrow \rightarrow I \bar{I} X$	Rhic	$h_1 \bar{h}_1$	★
		JParc		★★★
		Pax		★★★★★
$p^\uparrow (p/\bar{p})^\uparrow \rightarrow \pi X$	Rhic	$h_1 h_1 D_1$	★★	
	JParc		★★★	
	Pax		★★★★★	
Singly polarized	$(p/\bar{p}/\pi) p^\uparrow \rightarrow (\pi\pi) X$	Rhic, JParc Compass, Panda	$f_1 h_1 H_1^\times$	★★★
	$(p/\bar{p}/\pi) p^\uparrow \rightarrow \Lambda X$	Rhic, JParc Compass, Panda	$f_1 h_1 H_1$	★
	$(\pi/\bar{p}) p^\uparrow \rightarrow I \bar{I} X$	Compass, JParc, Panda	$h_1^\perp \otimes h_1$	★★
	$(p/\bar{p}/\pi) p^\uparrow \rightarrow j(j/\gamma) X$	Rhic, Compass, JParc, Panda	$h_1^\perp \otimes h_1$	★★
	$\rightarrow \pi(j/\gamma) X$		$f_1 \otimes h_1 \otimes H_1^\perp$	★
	$\rightarrow (\pi/j/\gamma) X$		$h_1^\perp \otimes h_1 \otimes D_1$	★

Sivers

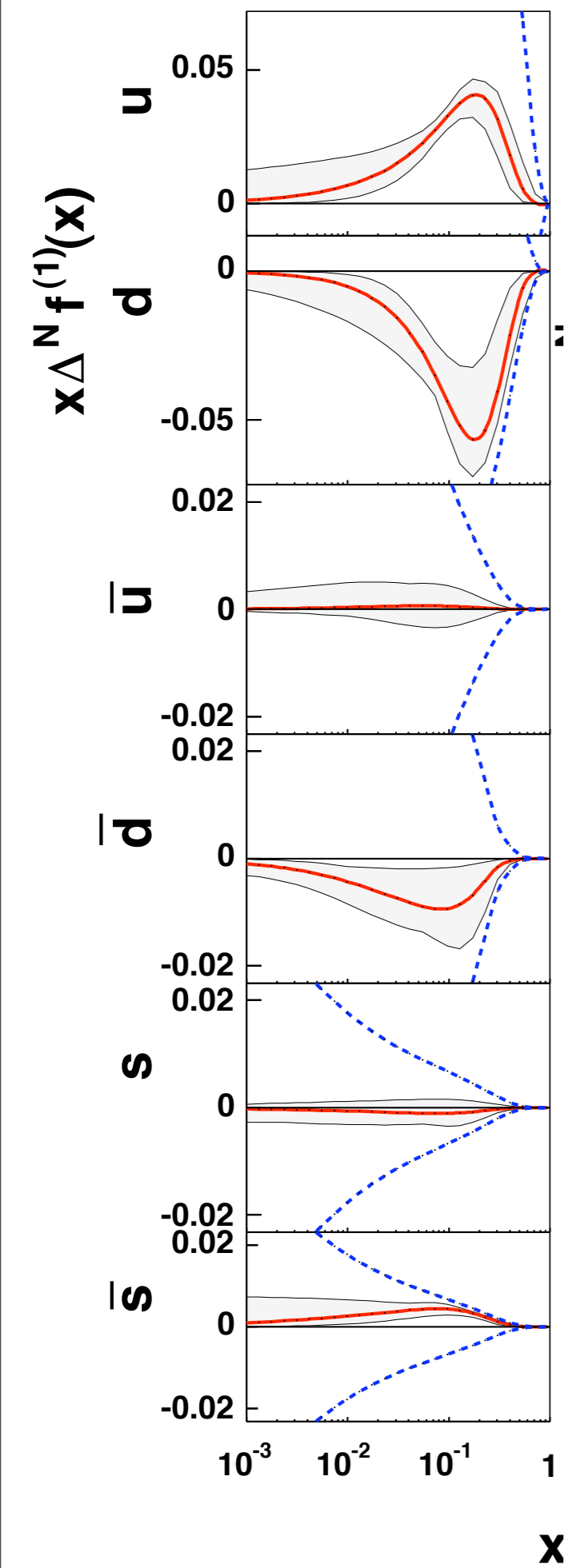
Data



Sivers functions

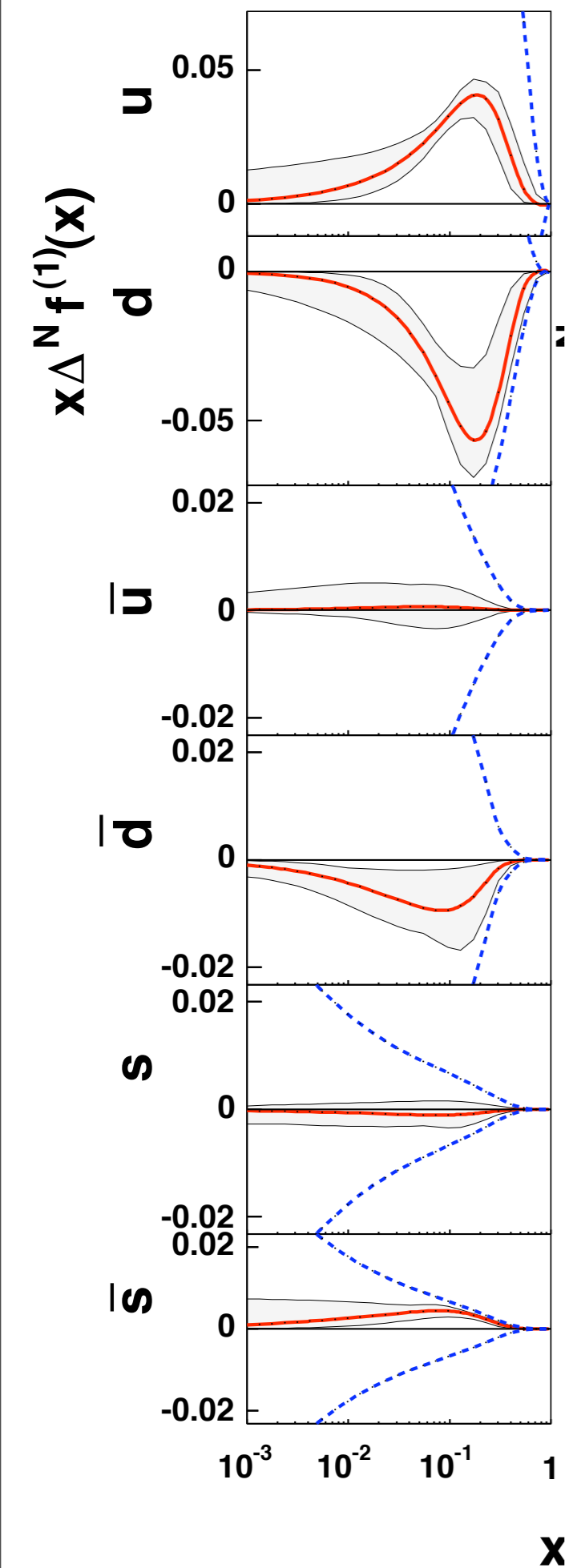


Sivers functions



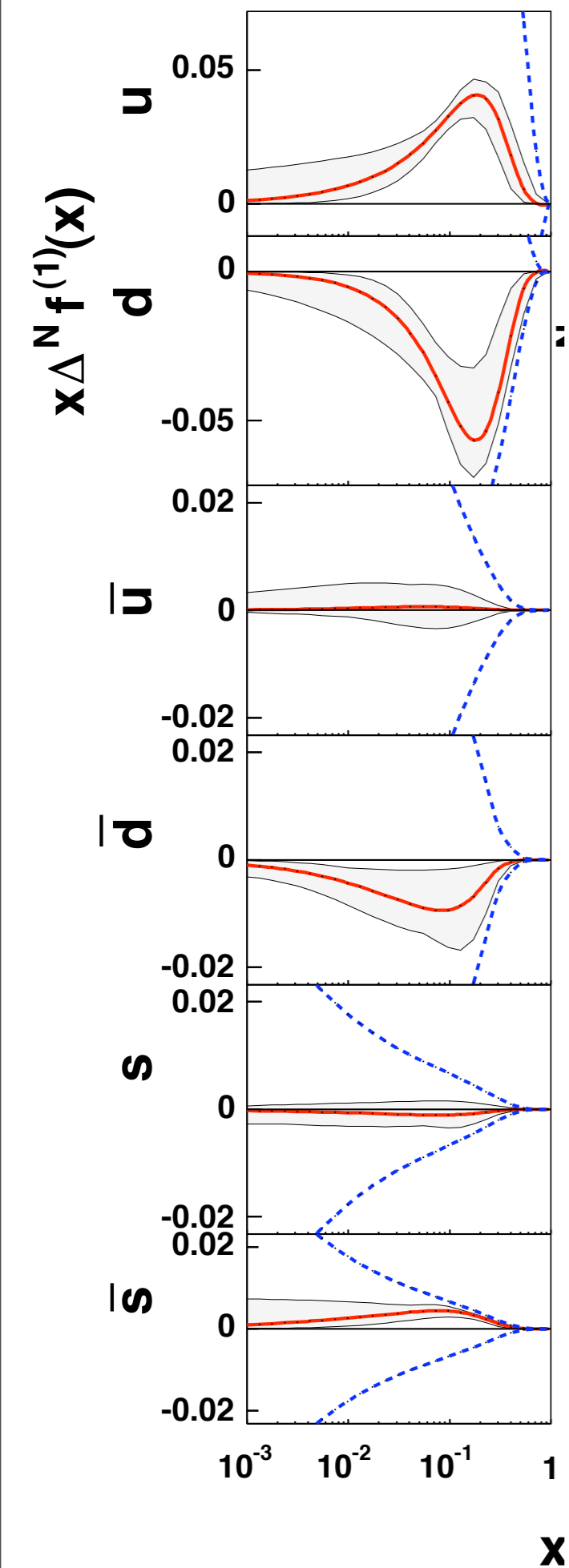
- Data from HERMES, COMPASS

Sivers functions



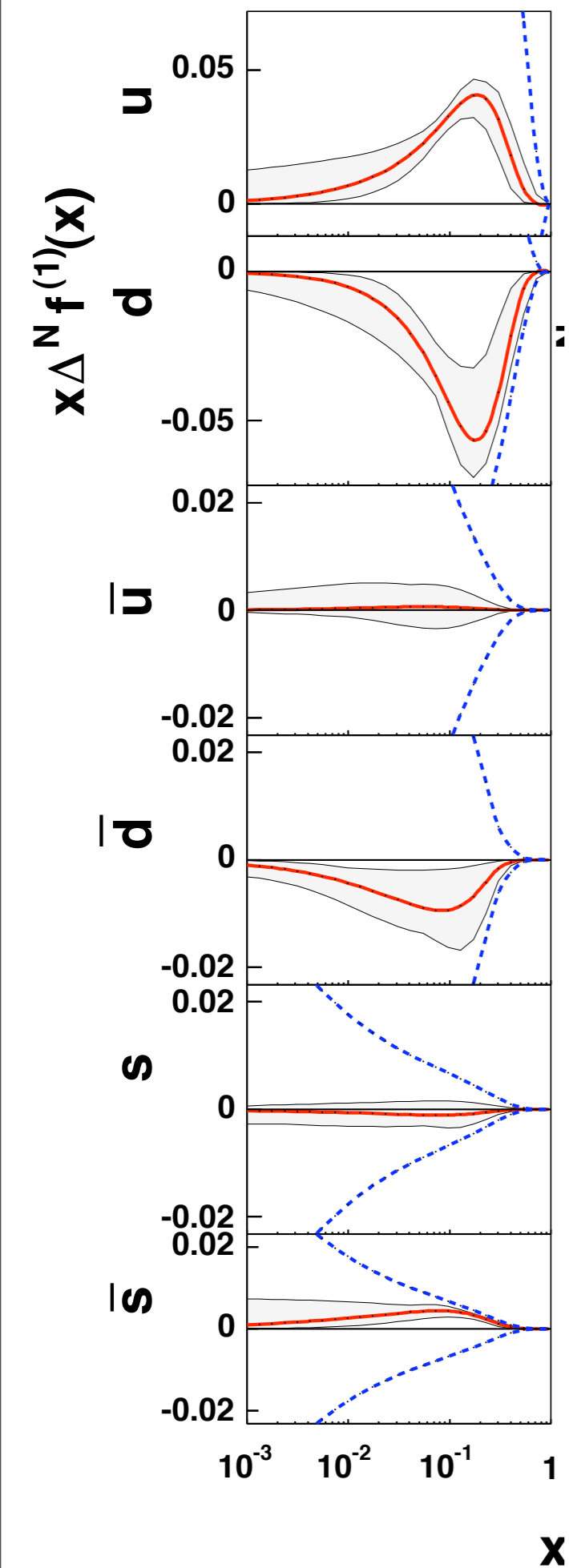
- Data from HERMES, COMPASS
- 96 data points (some correlations -- cf. 467 points for Δq fits)

Sivers functions



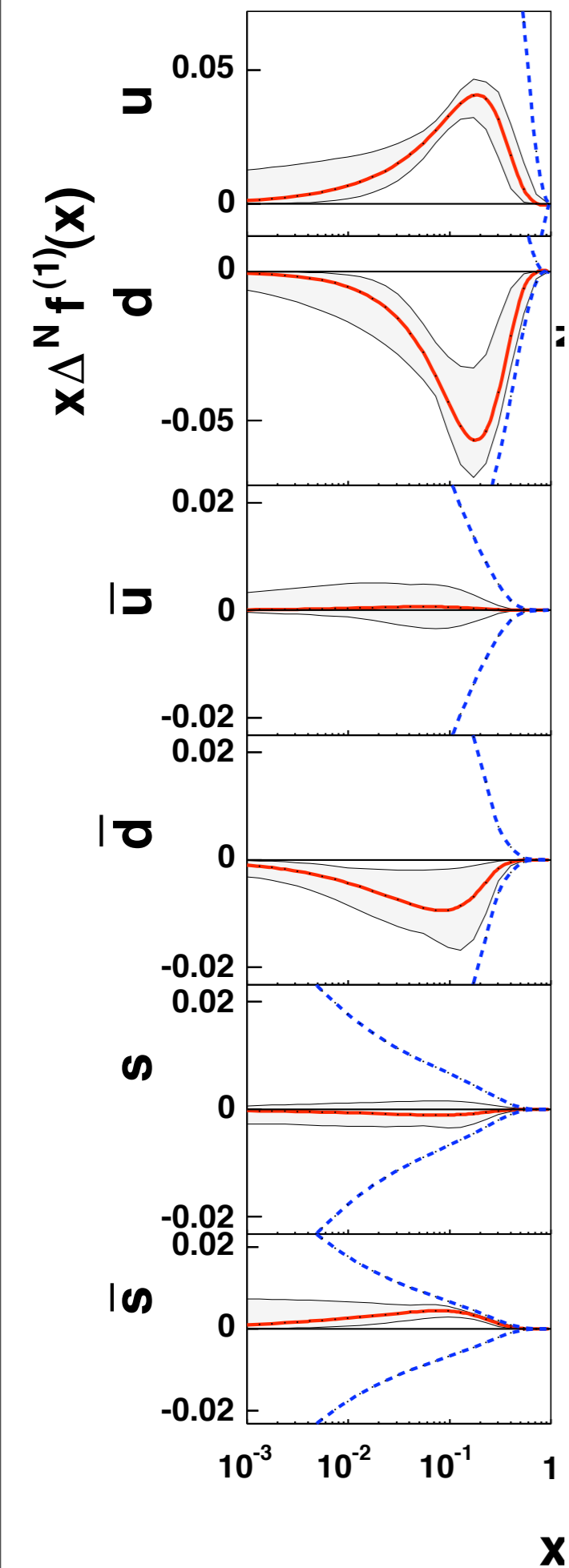
- Data from HERMES, COMPASS
- 96 data points (some correlations -- cf. 467 points for Δq fits)
- no sys errors

Sivers functions



- Data from HERMES, COMPASS
- 96 data points (some correlations -- cf. 467 points for Δq fits)
- no sys errors
- $\chi^2 \approx 1.0$

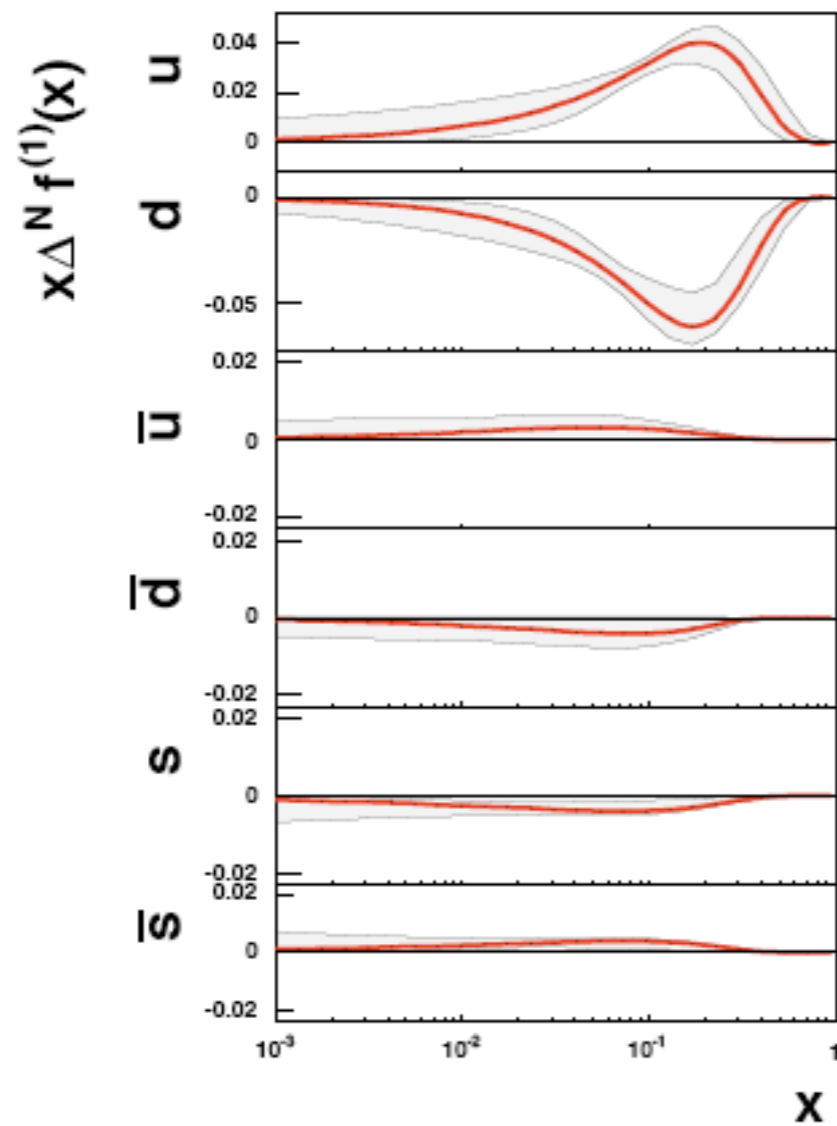
Sivers functions



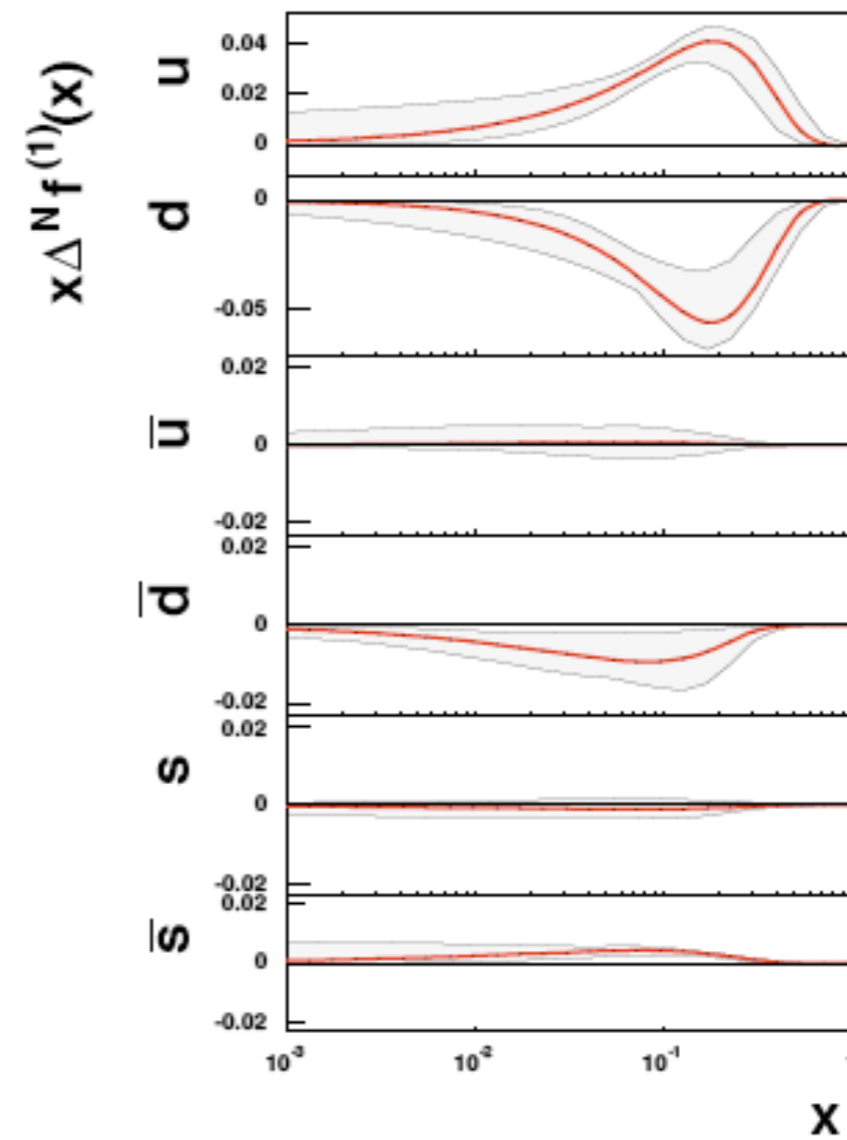
- Data from HERMES, COMPASS
- 96 data points (some correlations -- cf. 467 points for Δq fits)
- no sys errors
- $\chi^2 \approx 1.0$
- Statistical uncertainty only ($\Delta\chi^2 \approx 17$)

Sivers function - Torino

“Symmetric sea”



Free fit



Sivers function: Bochum

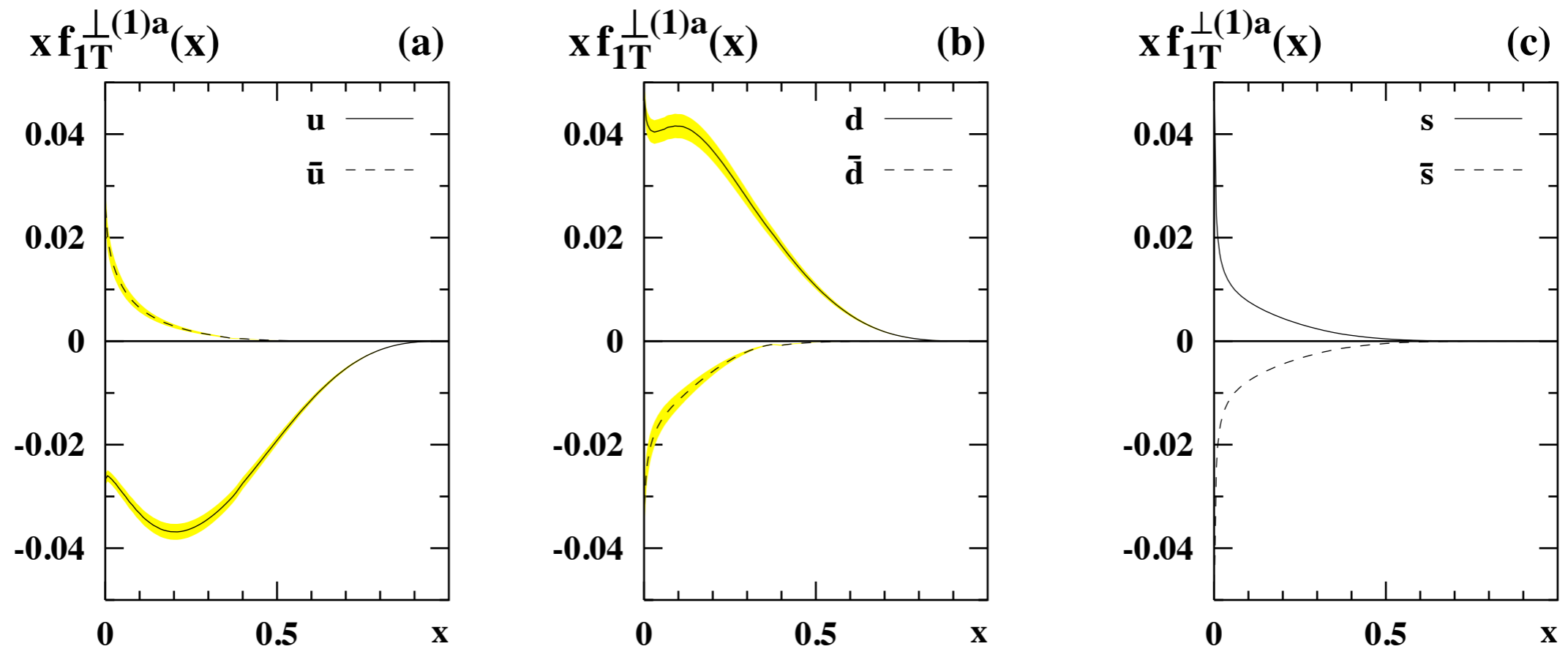


FIGURE 7. The $x f_{1T}^{\perp(1)a}(x)$ vs. x as extracted from preliminary HERMES and COMPASS data [10, 11]. (a) The flavours u and \bar{u} . (b) The flavours d and \bar{d} . (c) The flavours s and \bar{s} that were fixed to \pm positivity bounds (17) for reasons explained in Sec. 7, see also Eqs. (18, 19). The shaded areas in (a) and (b) show the respective 1- σ -uncertainties.

Model statement

$$(1 - x) f_{1T}^{\perp q}(x) = -\frac{3}{2} M C_F \alpha_S E^q(x, 0, 0)$$
$$\int_0^1 dx (1 - x) f_{1T}^{\perp q}(x) = -\frac{3}{2} M C_F \alpha_S \kappa^q$$

Burkardt, Hwang, PRD69 (04)

Lu, Schmidt, PRD75 (07)

A.B., F. Conti, M. Radici, arXiv:0807.0323

Model statement

$$(1 - x) f_{1T}^{\perp q}(x) = -\frac{3}{2} M C_F \alpha_S E^q(x, 0, 0)$$
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Burkardt, Hwang, PRD69 (04)

Lu, Schmidt, PRD75 (07)

A.B., F. Conti, M. Radici, arXiv:0807.0323

$$k^u = 1.67$$

$$k^d = -2.03$$

Model statement

$$(1 - x) f_{1T}^{\perp q}(x) = -\frac{3}{2} MC_F \alpha_S E^q(x, 0, 0)$$

$$\int_0^1 dx (1 - x) f_{1T}^{\perp q}(x) = -\frac{3}{2} MC_F \alpha_S \kappa^q$$

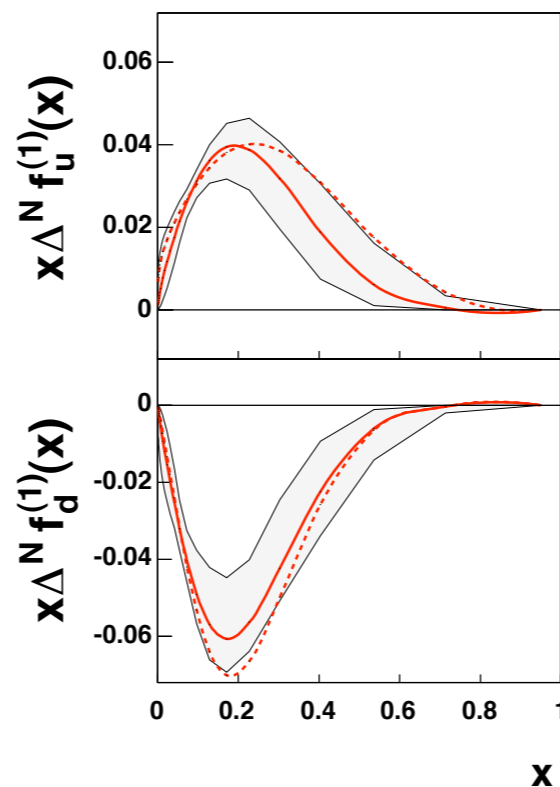
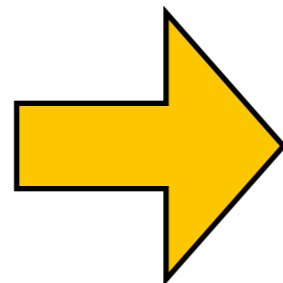
Burkardt, Hwang, PRD69 (04)

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$$k^u = 1.67$$

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Anselmino et al., 0805.2677,

Arnold et al., 0805.2137

Model statement

$$(1 - x) f_{1T}^{\perp q}(x) = -\frac{3}{2} M C_F \alpha_S E^q(x, 0, 0)$$

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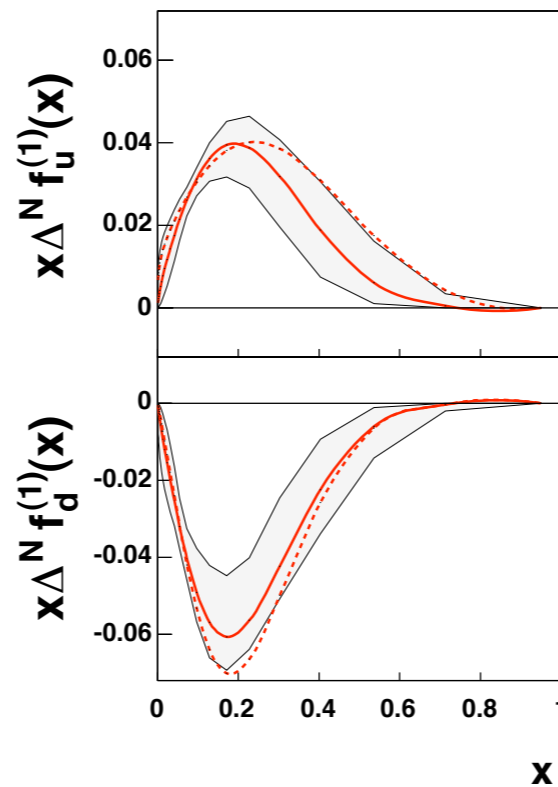
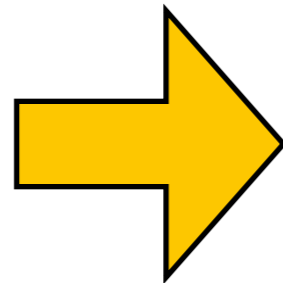
Burkardt, Hwang, PRD69 (04)

Lu, Schmidt, PRD75 (07)

A.B., F. Conti, M. Radici, arXiv:0807.0323

$$k^u = 1.67$$

$$k^d = -2.03$$

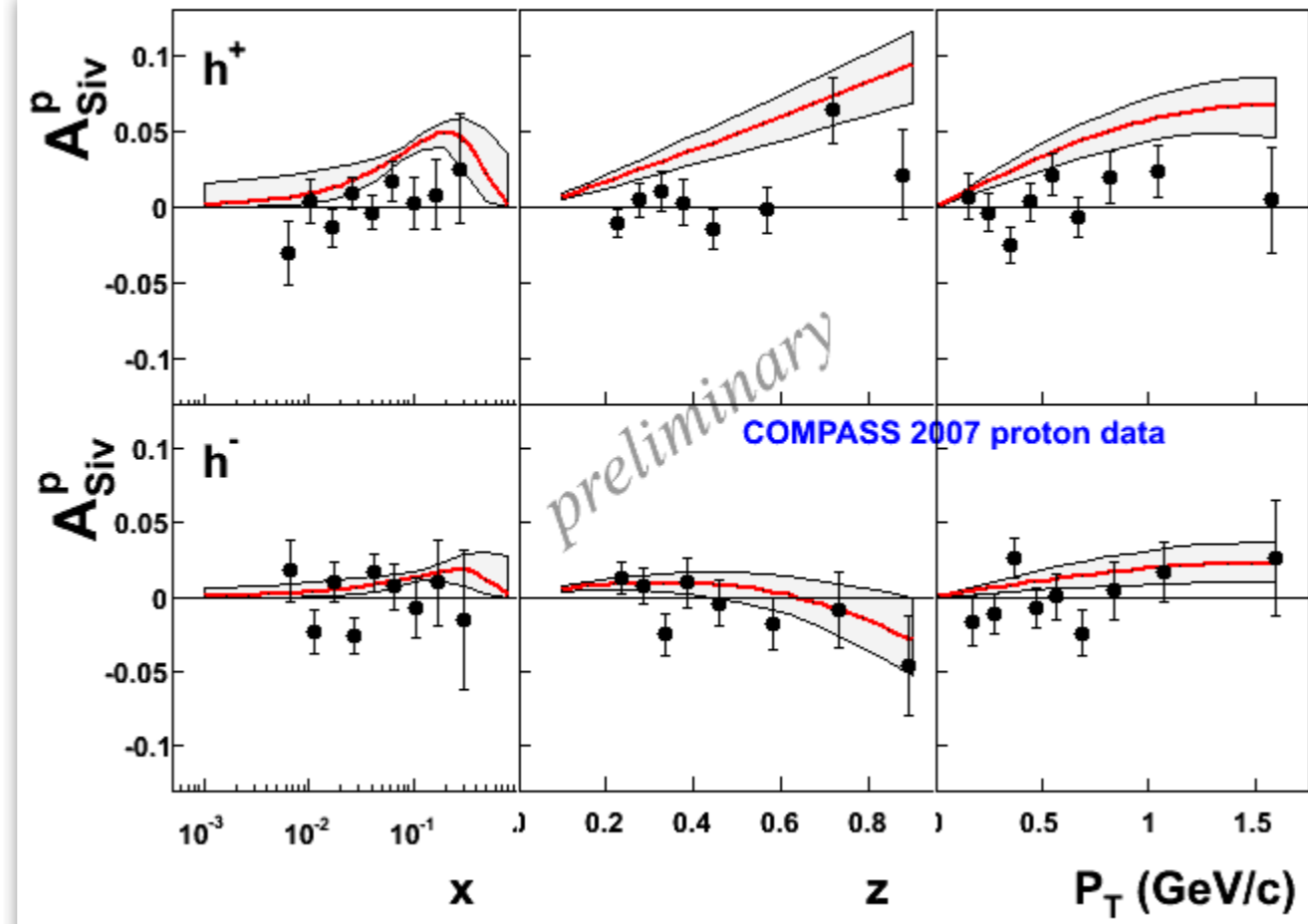


Anselmino et al., 0805.2677,

Arnold et al., 0805.2137

The relation is not general

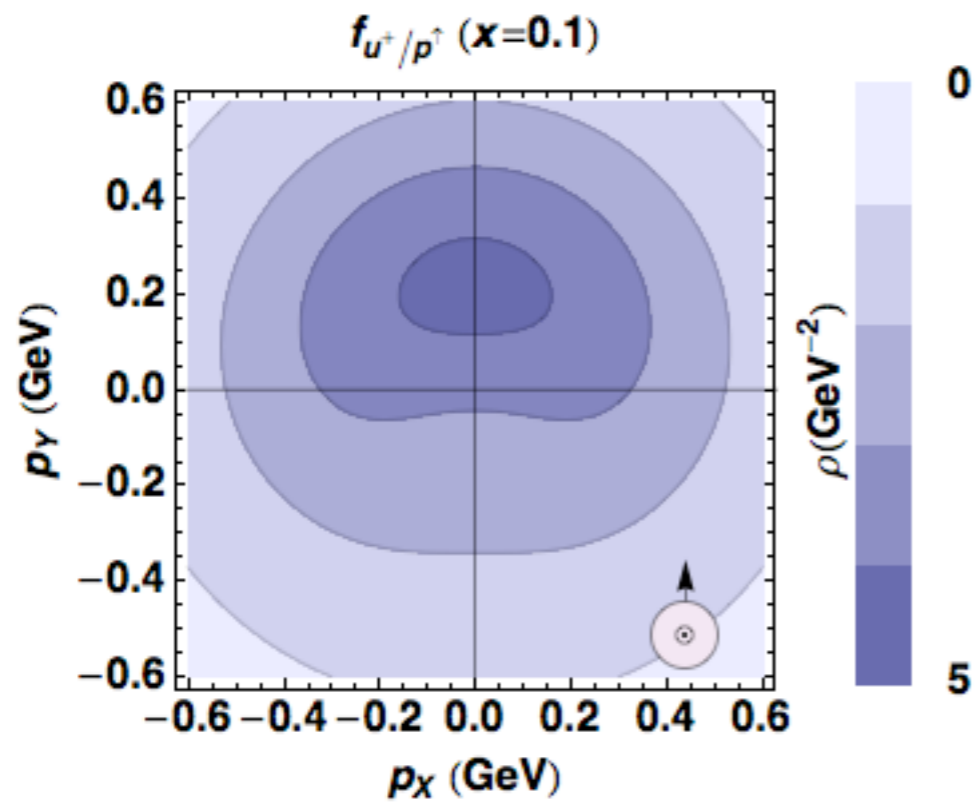
Sivers: COMPASS proton



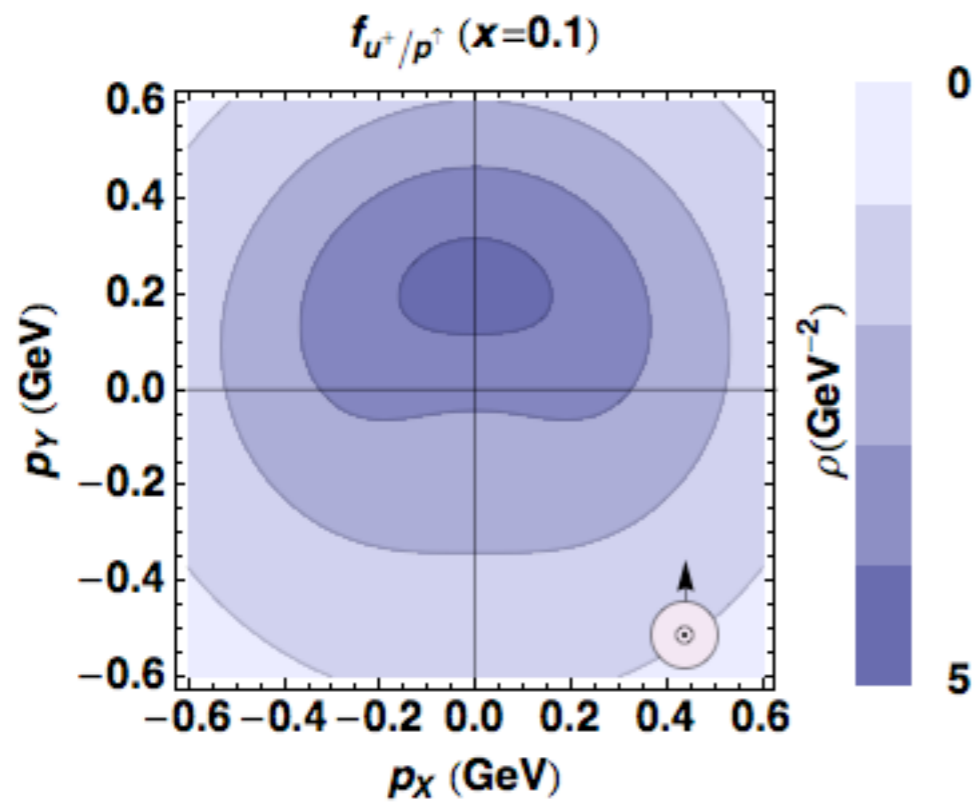
data: S. Levorato, Transversity 08
prediction: Anselmino et al., 0805.2677

More...

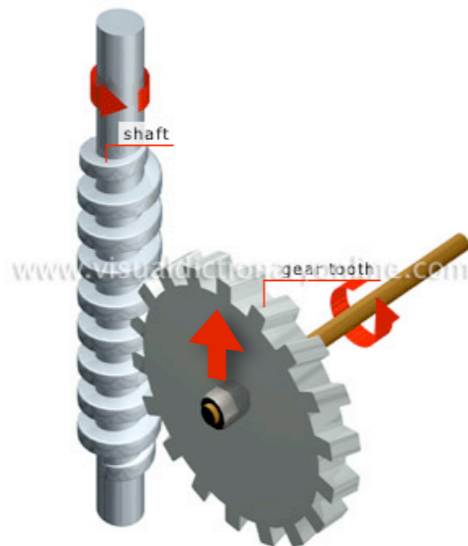
g_{1T} : another interesting function



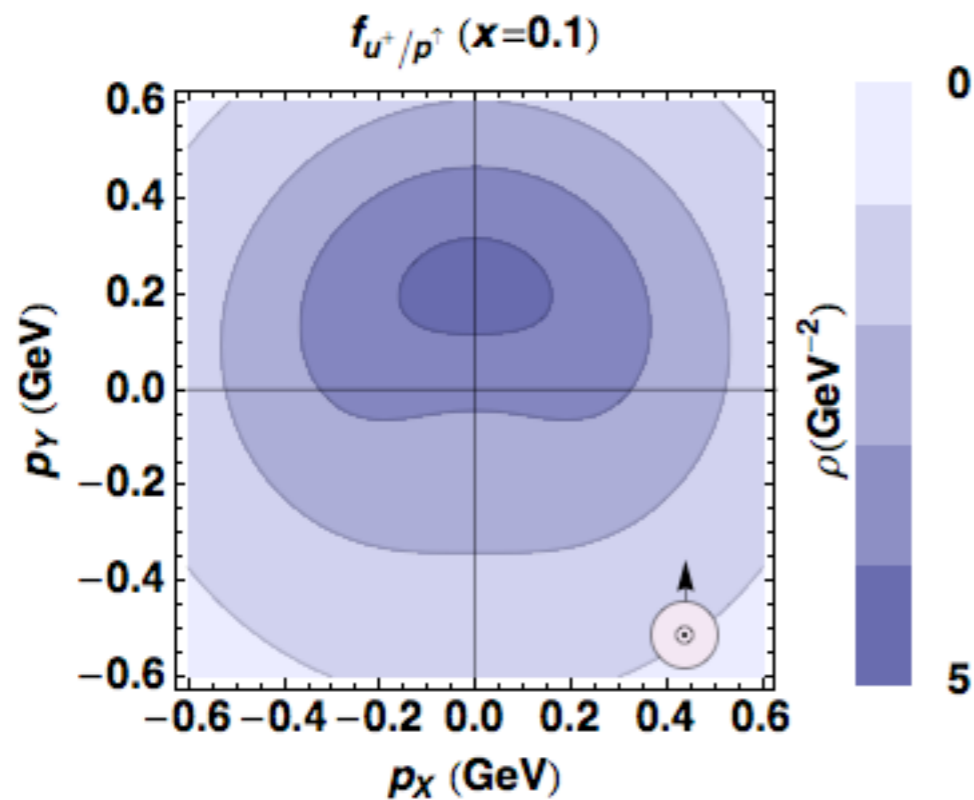
g_{1T} : another interesting function



Worm gear



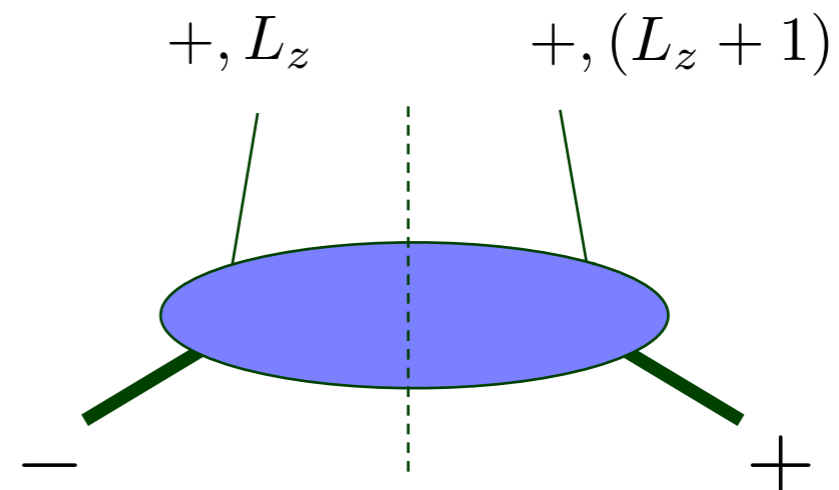
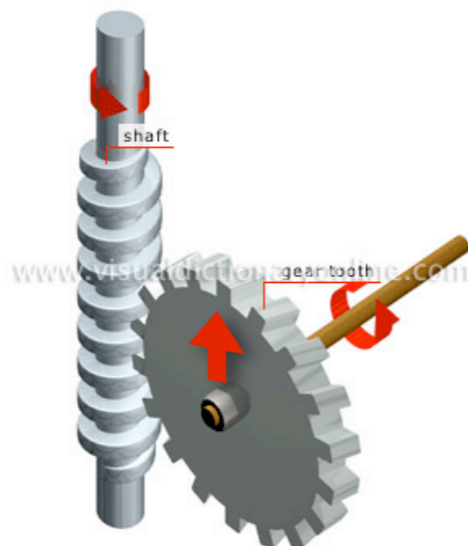
g_{1T} : another interesting function



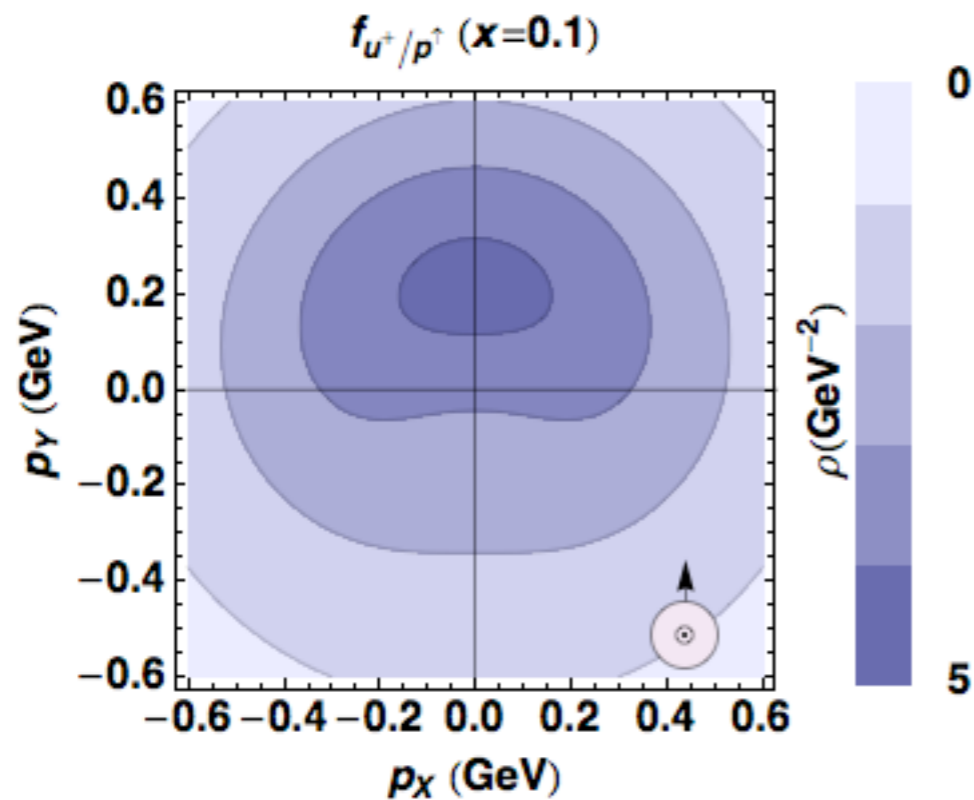
$$g_{1T} = \frac{1}{16\pi^3} \text{Re} [(\psi_+^+)^* \psi_+^- - (\psi_-^+)^* \psi_-^-]$$

$$f_{1T}^\perp = \frac{1}{16\pi^3} \text{Im} [(\psi_+^+)^* \psi_+^- + (\psi_-^+)^* \psi_-^-]$$

Worm gear



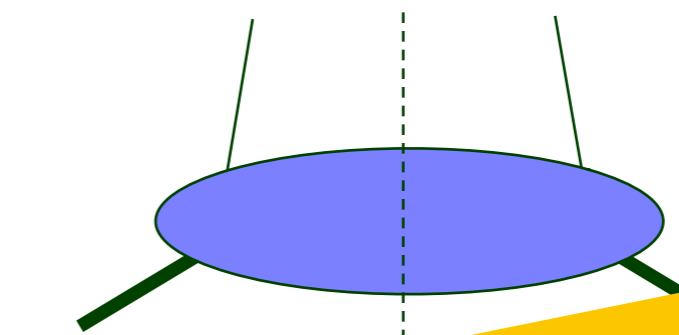
g_{1T} : another interesting function



$$g_{1T} = \frac{1}{16\pi^3} \text{Re} [(\psi_+^+)^* \psi_+^- - (\psi_-^+)^* \psi_-^-]$$

$$f_{1T}^\perp = \frac{1}{16\pi^3} \text{Im} [(\psi_+^+)^* \psi_+^- + (\psi_-^+)^* \psi_-^-]$$

$+, L_z$ $+, (L_z + 1)$



Another way to access angular-momentum information without final-state interactions

Worm gear

